

# A New Approach to Direct Torque Control for Induction Motor Drive Using Amplitude and Angle of the Stator Flux Control

Yuttana Kumsuwan\*, Suttichai Premrudeepreechacharn\* and Hamid A. Toliyat\*\*

**Abstract** – This paper proposes the design and implementation of a direct torque controlled induction motor drive system. The method is based on control of decoupling between amplitude and angle of reference stator flux for determining reference stator voltage vector in generating PWM output voltage for induction motors. The objective is to reduce electromagnetic torque ripple and stator flux droop which result in a decrease in current distortion in steady state condition. In addition, the proposed technique provides simplicity of a control system. The direct torque control is based on the relationship between instantaneous slip angular frequency and rotor angular frequency in adjustment of the reference stator flux angle. The amplitude of the reference stator flux is always kept constant at rated value. Experimental results are illustrated in this paper confirming the capability of the proposed system in regards to such issues as torque and stator flux response, stator phase current distortion both in dynamic and steady state with load variation, and low speed operation.

**Keywords:** Direct torque control, Induction motor, Space vector modulation, Stator flux control

## 1. Introduction

Direct torque control (DTC) of induction motor drives offers high performance in terms of simplicity in control and fast electromagnetic torque response. With dominant characteristics, the direct torque controlled induction motor drive is alternative in industrial applications. As shown in Fig. 1, the principle of the classical DTC is decoupled control between stator flux and electromagnetic torque using hysteresis control of stator flux and torque error and stator flux position. A switching look-up table is included for selection of voltage vectors feeding the induction motor [1]. However, the main problem is that when operating at steady state, the DTC produces high level of torque ripple, variable switching frequency of inverter over a fundamental period, and stator flux droop of adjacent vector during a voltage vector change. Moreover, particularly when the induction motor with DTC operates under heavy load condition in low speed region, distortion of the motor phase current is increased due to stator flux droop leading to reduced drive system efficiency [2, 3].

Development of DTC for overcoming drawback of the classical DTC is voltage modulation application replacing the look-up table of the voltage vector selection on the basis of a 2-level inverter. The voltage modulation is based on space vector modulation (SVM) with constant switching

frequency for application to the induction motor. This technique can be classified into 4 main types according to the control structure as follows. The first method is called DTC-SVM control [4]. This method is based on deadbeat control derived from the torque and stator flux errors. It offers good steady state and dynamic performance reduction in phase current distortion and fast response of torque. However, the limitation of this technique is that it is computationally intensive. The second method is called Adaptive Neural Fuzzy Inference System (ANIS) [5]. This method is based on fuzzy logic and artificial neural network for decoupled stator flux and torque control. Voltage vectors are performed in polar coordinates. Good steady-state and dynamic performance is achieved.

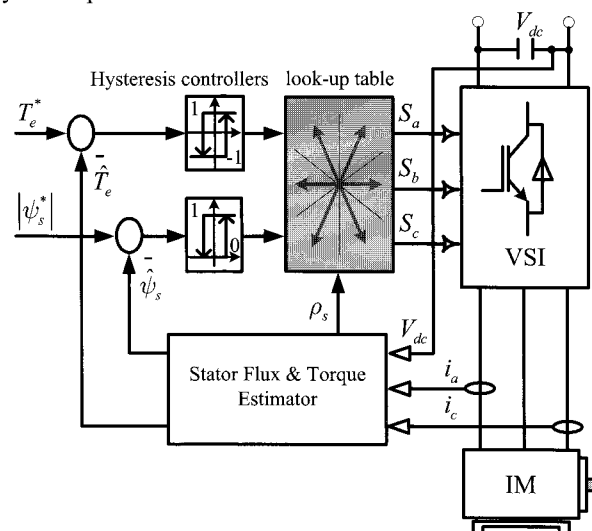


Fig. 1. Block diagram of classical direct torque control

\* Department of Electrical Engineering, Faculty of Engineering, Chiang Mai University, Chiang Mai, 50200, Thailand. (g4766008@doel.eng.cmu.ac.th)

\*\* Department of Electrical and Computer Engineering, Texas A&M University, College Station, TX 77843-3128 USA. (toliyat@ece.tamu.edu)

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The third method is called stator flux oriented control (SFOC): The technique uses two proportional-integral (PI) controllers instead of hysteresis controllers for generating direct and quadrature components from stator flux and torque, respectively. Voltage vectors are preformed in Cartesian coordinates. This method provides good transient performance, robustness, and reduced steady-state torque ripple [6, 7]. The last method is called DTC-SVM with closed loop torque control and it uses only one output of PI controller. The stator flux positions are derived from estimation, and amplitude of reference stator flux is kept constant for determining reference stator flux vector. Then the resultant error between the actual stator flux and the reference stator flux is used for voltage vector calculation. Performance of the control system depends on design of the PI torque controller [8, 9].

In this paper, DTC based on decoupled control of both stator flux and torque is proposed, which is different from DTC-SVM [4-9]. This technique uses the relationship between torque, slip angular frequency, and rotor angular frequency for controlling stator flux angle while the amplitude of the reference stator flux is kept constant at rated value. Then, the reference stator flux vector in polar form is determined.

This paper is organized as follows. Section 2 describes the dynamic model of an induction motor in two-phase stationary reference frame. Section 3 derives the proposed direct torque control by decoupling the amplitude and angle of the stator flux vector (DTC-AAS). This section also describes the design of the PI torque controller, and determination of reference voltage vector derived from resultant error between the actual and required stator flux vectors. In addition, the improvement of stator flux estimation is also discussed. Experimental results are then presented in Section 4. Finally, the main features and advantages of the proposed technique are summarized in the conclusions.

## 2. Induction Motor Model

The dynamic model of an induction motor in the stationary reference frame can be written in  $\alpha\beta$  frame variables. Stator voltage vector  $\bar{v}_s$  of the motor can be expressed as follows.

$$\begin{aligned} v_{\alpha s} &= \frac{d}{dt} \psi_{\alpha s} + R_s i_{\alpha s} \\ v_{\beta s} &= \frac{d}{dt} \psi_{\beta s} + R_s i_{\beta s} \\ \bar{v}_s &= \frac{d}{dt} \bar{\psi}_s + R_s \bar{i}_s. \end{aligned} \quad (1)$$

The stator flux vector  $\bar{\psi}_s$  and components can be written as

$$\begin{aligned} \psi_{\alpha s} &= L_s i_{\alpha s} + L_m i_{\alpha r} \\ \psi_{\beta s} &= L_s i_{\beta s} + L_m i_{\beta r} \\ \bar{\psi}_s &= L_s \bar{i}_s + L_m \bar{i}_r. \end{aligned} \quad (2)$$

and the rotor flux vector  $\bar{\psi}_r$  and components in the stationary reference frame are

$$\begin{aligned} \psi_{\alpha r} &= L_r i_{\alpha r} + L_m i_{\alpha s} \\ \psi_{\beta r} &= L_r i_{\beta r} + L_m i_{\beta s} \\ \bar{\psi}_r &= L_r \bar{i}_r + L_m \bar{i}_s. \end{aligned} \quad (3)$$

where  $v_{\alpha s}$  and  $v_{\beta s}$  are the stator voltages;  $i_{\alpha s}$  and  $i_{\beta s}$  are the stator currents;  $i_{\alpha r}$  and  $i_{\beta r}$  are the rotor currents;  $\psi_{\alpha s}$  and  $\psi_{\beta s}$  are the stator fluxes;  $\psi_{\alpha r}$  and  $\psi_{\beta r}$  are the rotor fluxes;  $\bar{i}_s$  and  $\bar{i}_r$  are the stator and rotor current vectors;  $R_s$  is the stator winding resistance; and  $L_s, L_r, L_m$  are stator, rotor self inductance, and mutual inductance, respectively.

The electromagnetic torque  $T_e$  developed by the induction motor in terms of stator and rotor flux vectors can be expressed as

$$\begin{aligned} T_e &= \frac{3}{2} P \frac{L_m}{\sigma L_s L_r} \bar{\psi}_s \times \bar{\psi}_r = \frac{3}{2} P \frac{L_m}{\sigma L_s L_r} |\bar{\psi}_s| |\bar{\psi}_r| \sin(\rho_s - \rho_r) \\ &= \frac{3}{2} P \frac{L_m}{\sigma L_s L_r} |\bar{\psi}_s| |\bar{\psi}_r| \sin(\delta). \end{aligned} \quad (4)$$

where  $\sigma = 1 - L_m^2 / L_s L_r$  is the leakage factor;  $P$  is the number of pole pairs;  $\rho_s, \rho_r$  are stator and rotor flux angles, respectively, and  $\delta$  is the torque angle.

From the above equation, clearly, the electromagnetic torque is a cross vector product between the stator and rotor flux vectors. Therefore, generally torque control can be performed by controlling torque angle  $\delta$  with constant amplitude of the stator and rotor fluxes.

## 3. Proposed Control Method

Fig. 2 shows the block diagram of the DTC-AAS drive system. The control system consists of four basic functions, namely torque control, PI torque controller, the polar-to-rectangular transformation of direct stator flux control, a stator voltage calculation block, and the stator flux and torque estimator block. The description of each block is as follows.

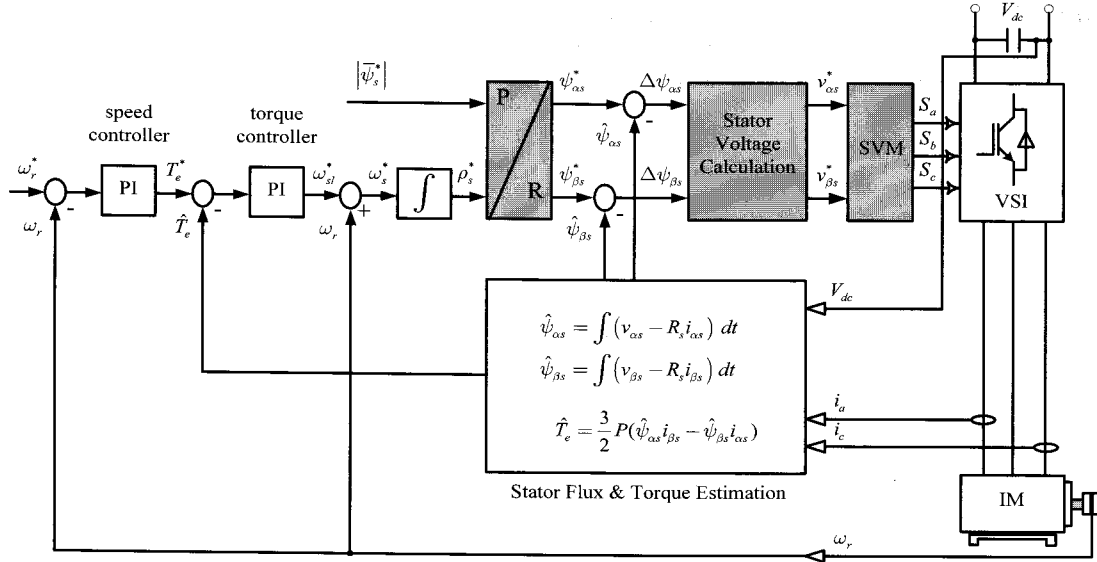


Fig. 2. Block diagram of DTC-AAS drive system

### 3.1 Torque Control

In this method, the torque control is performed by defining the constant amplitude of reference stator flux  $|\bar{\psi}_s^*|$ . When considering (4), rotor flux vector rotates after the stator flux vector with torque angle  $\delta$  at constant amplitude. Torque control is directly performed by controlling a torque angle  $\delta$  change, which is the angle between stator and rotor flux vectors. According to (2) and (3), with constant amplitudes of both stator and rotor fluxes, stator and rotor flux vectors in terms of stator angular frequency  $\omega_s$  and rotor angular frequency  $\omega_r$  and the position of both flux vectors rotating with angle  $\rho_s$  and  $\rho_r$  with respect to real axis in the stationary reference frame, respectively, as shown in Fig. 3, are written as follows.

$$\bar{\psi}_s = |\bar{\psi}_s^*| e^{j\rho_s} = |\bar{\psi}_s^*| e^{j\omega_s t} \quad (5)$$

$$\bar{\psi}_r = |\bar{\psi}_r| e^{j\rho_r} = |\bar{\psi}_r| e^{j\omega_r t} \quad (6)$$

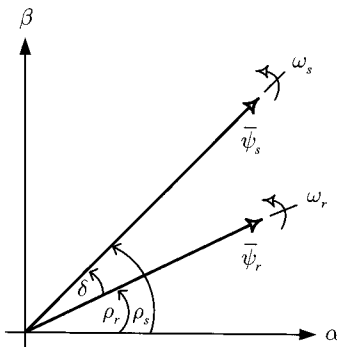


Fig. 3. Stator and rotor flux vectors

With the same principle in [9], by substituting (5) and (6) into (4), the instantaneous electromagnetic torque can be derived as

$$\begin{aligned} T_e(t) &= \frac{3}{2} P \frac{L_m}{\sigma L_s L_r} |\bar{\psi}_s^*| e^{j\omega_s t} \times |\bar{\psi}_r| e^{j\omega_r t} \\ &= \left[ \frac{3}{2} P \frac{L_m^2}{R_r L_s^2} |\bar{\psi}_s^*|^2 \right] \left[ 1 - e^{-\frac{t}{T_M}} \right] (\omega_s - \omega_r). \end{aligned} \quad (7)$$

where  $R_r$  is the rotor winding resistance, and  $T_M = \sigma \frac{L_r}{R_r}$  is the time constant.

From (7), the quantity  $(\omega_s - \omega_r)$ , which is the relationship between stator angular frequency  $\omega_s$  and rotor angular frequency  $\omega_r$ , is slip angular frequency  $\omega_{sl}$  and can be written as

$$\omega_{sl} = \omega_s - \omega_r. \quad (8)$$

By substituting (8) into (7), the instantaneous electromagnetic torque is given by,

$$T_e(t) = \left[ \frac{3}{2} P \frac{L_m^2}{R_r L_s^2} |\bar{\psi}_s^*|^2 \right] \left[ 1 - e^{-\frac{t}{T_M}} \right] \omega_{sl}. \quad (9)$$

From the above equation, the relationship between torque and slip angular frequency is quite clear. Dynamic torque response depends on instantaneous slip angular frequency

while the stator flux reference is kept constant. The torque can be controlled by using only one PI controller instead of a hysteresis regulator (the classical DTC) for calculating error between reference and estimated torque. Then, the output of the PI torque controller will be used for calculating the stator flux angle. From (1) and (4), the estimated torque  $\hat{T}_e$  of the motor in terms of stator flux and the stator current in  $\alpha\beta$  stationary reference frame can be written as

$$\hat{T}_e = \frac{3}{2} P (\hat{\psi}_{\alpha s} i_{\beta s} - \hat{\psi}_{\beta s} i_{\alpha s}). \quad (10)$$

Finally, the estimated stator flux components are

$$\begin{aligned} \hat{\psi}_{\alpha s} &= \int (v_{s\alpha} - i_{\alpha s} R_s) dt \\ \hat{\psi}_{\beta s} &= \int (v_{s\beta} - i_{\beta s} R_s) dt. \end{aligned} \quad (11)$$

### 3.2 Design of the PI Torque Controller

As shown in Fig. 2, the reference torque  $T_e^*$  is obtained from the output of the PI speed controller. Then, the reference torque is compared with the estimated torque  $\hat{T}_e$  to generate an error signal. This signal is the input of the PI torque controller that computes the value of the instantaneous slip angular frequency  $\omega_{sl}^*$  required to adjust the stator flux angle. The output of the PI torque controller can be expressed as

$$\omega_{sl}^* = k_p \left[ \Delta T_e + \frac{1}{T_i} \int \Delta T_e dt \right]. \quad (12)$$

The input of the polar-to-rectangular transformation of direct stator flux control is the reference stator angular frequency  $\omega_s^*$ , which is obtained by adding electrical rotor angular frequency  $\omega_r$  with instantaneous slip angular frequency  $\omega_{sl}^*$  and can be expressed as

$$\omega_s^* = \omega_r + \omega_{sl}^* \quad (13)$$

The block diagram of the torque control loop is illustrated in Fig. 4.

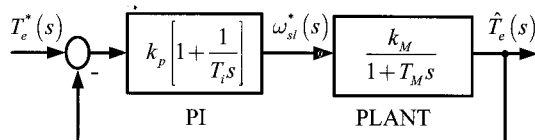


Fig. 4. Block diagram of the torque loop

By taking Laplace transformation of (9) in order to determine  $M(s)$ , which is the relationship between the slip angular frequency  $\omega_{sl}^*(s)$  and the actual torque  $\hat{T}_e(s)$ , the following equations can be achieved:

$$M(s) = \frac{\hat{T}_e(s)}{\omega_{sl}^*(s)} = \frac{k_M}{1 + T_M s}. \quad (14)$$

where  $k_M = \frac{3}{2} P \frac{L_m^2}{R_s L_s^2} |\bar{\psi}_s^*|^2$  is constant.

For PI controller design, the type of the system becomes one, which guarantees zero position steady-state error. With regard to pole placement, the output  $\omega_{sl}^*(s)$  of the controller is obtained by Laplace transform of (12) and can be written as

$$\omega_{sl}^*(s) = k_p \left[ 1 + \frac{1}{T_i s} \right] (T_e^*(s) - \hat{T}_e(s)). \quad (15)$$

where  $k_p$  is the proportional gain;  $T_i$  is the integration time and  $\Delta T_e = (T_e^*(s) - \hat{T}_e(s))$  is the error.

From Fig. 4, by combining (14) and (15), the closed-loop transfer function  $H(s)$  of the torque control system can be expressed as

$$H(s) = \frac{\hat{T}_e(s)}{T_e^*(s)} = \frac{\frac{k_M k_p}{T_M} s + \frac{k_M k_p}{T_i T_M}}{s^2 + \left( \frac{1}{T_M} + \frac{k_M k_p}{T_M} \right) s + \frac{k_M k_p}{T_i T_M}}. \quad (16)$$

For a unit-step command ( $T_e^*(s) = 1/s$ ), the actual torque is

$$\hat{T}_e(s) = \frac{\frac{k_M k_p}{T_M} s + \frac{k_M k_p}{T_i T_M}}{s^2 + \left( \frac{1}{T_M} + \frac{k_M k_p}{T_M} \right) s + \frac{k_M k_p}{T_i T_M}} \frac{1}{s}. \quad (17)$$

The characteristic polynomial is

$$s^2 + \left( \frac{1}{T_M} + \frac{k_M k_p}{T_M} \right) s + \frac{k_M k_p}{T_i T_M} = 0. \quad (18)$$

The general form of the characteristic polynomial of a second-order system is given by,

$$s^2 + 2\zeta\omega_n s + \omega_n^2 = 0. \quad (19)$$

where  $\omega_n$  is the natural angular frequency for  $\zeta \leq 1$ ;  $\zeta$  is the damping ratio.

Therefore, the natural angular frequency of the torque controller system is given by,

$$\omega_n = \sqrt{\frac{k_M k_p}{T_i T_M}}, \quad (20)$$

and the damping ratio is

$$\zeta = \left[ \frac{1}{T_M} + \frac{k_M k_p}{T_M} \right] \sqrt{\frac{T_i T_M}{4k_M k_p}}. \quad (21)$$

The parameters of the PI controller might be calculated as

$$k_p = \frac{2\zeta\omega_n T_M - 1}{k_M} \quad (22)$$

$$T_i = \frac{2\zeta\omega_n T_M - 1}{\omega_n^2 T_M}. \quad (23)$$

### 3.3 Direct Stator Flux Control

The main task of the direct stator flux control is decoupling the amplitude and the angle of the stator flux vector. The reference stator flux vector in polar form is given by  $\bar{\psi}_s^* = |\bar{\psi}_s^*| \angle \rho_s^*$ . The calculation of angle of the reference stator flux vector is obtained by integrating stator angular frequency  $\omega_s^*$  as indicated in (13). As a consequence, the stator flux angle  $\rho_s^*$  is derived from

$$\rho_s^* = \int \omega_s^* dt. \quad (24)$$

By polar-to-rectangular transformation of the stator flux vector, the reference stator flux components are expressed as follows:

$$\begin{aligned} \psi_{\alpha s}^* &= |\bar{\psi}_s^*| \cos \rho_s^* \\ \psi_{\beta s}^* &= |\bar{\psi}_s^*| \sin \rho_s^*. \end{aligned} \quad (25)$$

Finally, from (1), the reference stator voltages  $v_{\alpha s}^*$  and  $v_{\beta s}^*$  in the  $\alpha\beta$  frame are calculated based on forcing the stator flux error ( $\Delta\psi_{\alpha s}$  and  $\Delta\psi_{\beta s}$ ) to zero at next sampling period  $(k+1)$ . The next reference stator voltages  $v_{\alpha s}^*(k+1)$  and  $v_{\beta s}^*(k+1)$  are given by

$$\begin{aligned} v_{\alpha s}^*(k+1) &= \left( \frac{\psi_{\alpha s}^*(k) - \hat{\psi}_{\alpha s}(k)}{\Delta T_s} \right) + R_s i_{\alpha s}(k) \\ v_{\beta s}^*(k+1) &= \left( \frac{\psi_{\beta s}^*(k) - \hat{\psi}_{\beta s}(k)}{\Delta T_s} \right) + R_s i_{\beta s}(k). \end{aligned} \quad (26)$$

where  $\Delta T_s$  is the sampling interval, and  $k$  represents the actual discretized time.

From (26), the next reference stator voltages  $v_{\alpha s}^*(k+1)$  and  $v_{\beta s}^*(k+1)$  are applied to the induction motor using a SVM controlled inverter.

### 3.4 Direct Stator Flux Control

The drawbacks of the estimation of the stator flux based on voltage model using open-loop integration as shown in (11) are dc drift and saturation problems. In this paper, improved stator flux estimator by integrating algorithm with an amplitude limiter in polar coordinates is used to overcome the problems associated with the pure integrator [10]. The stator flux estimator is given in Fig. 5.

In Fig. 5, the stator flux is transformed to polar coordinates and after limiting its amplitude it is transformed back to Cartesian coordinates. The limitation in Cartesian coordinates is performed as follows. The limited amplitude of the stator flux is defined as

$$Z_L = \begin{cases} \sqrt{\hat{\psi}_{s\alpha}^2 + \hat{\psi}_{s\beta}^2} & \text{if } \sqrt{\hat{\psi}_{s\alpha}^2 + \hat{\psi}_{s\beta}^2} < L \\ L & \text{if } \sqrt{\hat{\psi}_{s\alpha}^2 + \hat{\psi}_{s\beta}^2} > L. \end{cases} \quad (27)$$

where  $Z_L$  is the output of the limiter and  $L$  is the limit value.  $L$  should be equal to the stator flux reference

The limited components of the stator flux are then simply scaled with the ratio of the limited amplitude and unlimited amplitude

$$\begin{aligned} Z_{L\alpha} &= \frac{Z_L}{\sqrt{\hat{\psi}_{s\alpha}^2 + \hat{\psi}_{s\beta}^2}} \hat{\psi}_{s\alpha} \\ Z_{L\beta} &= \frac{Z_L}{\sqrt{\hat{\psi}_{s\alpha}^2 + \hat{\psi}_{s\beta}^2}} \hat{\psi}_{s\beta}. \end{aligned} \quad (28)$$

where  $Z_{L\alpha}$  and  $Z_{L\beta}$  are the limited output of the stator fluxes.

Finally, for a discrete-time implementation, the stator flux estimator can be written as

$$\begin{aligned} \hat{\psi}_{s\alpha}(k+1) &= \hat{\psi}_{s\alpha}(k) + (v_{s\alpha}(k) - R_s i_{s\alpha}(k)) \Delta T_s + \omega_c \Delta T_s (Z_{L\alpha} - \hat{\psi}_{s\alpha}(k)) \\ \hat{\psi}_{s\beta}(k+1) &= \hat{\psi}_{s\beta}(k) + (v_{s\beta}(k) - R_s i_{s\beta}(k)) \Delta T_s + \omega_c \Delta T_s (Z_{L\beta} - \hat{\psi}_{s\beta}(k)). \end{aligned} \quad (29)$$

where  $\omega_c$  is the cutoff frequency of the low pass filter.

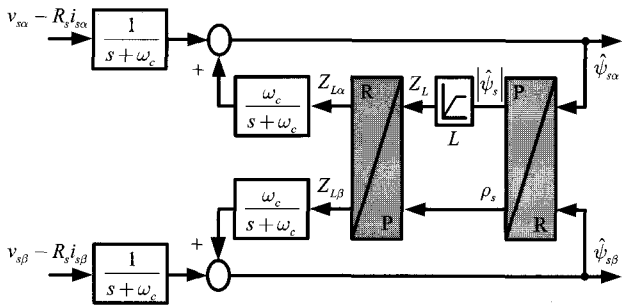


Fig. 5. Block diagram of the improved integrator algorithm with limited amplitude [10]

#### 4. Experimental Results

The experimental setup of the proposed control system is represented by the block diagram shown in Fig. 6. It consists of a dSPACE DS1104 controller board with TMS320F240 slave processor, ADC interface board CP1104, and a four-pole induction motor with parameters listed in Table 1. A three phase VSI inverter is connected to supply 550V dc bus voltage, with the switching frequency and the dead time of 5 kHz and 4  $\mu$ s, respectively. The DS1104 board is installed in a Pentium IV 1.5 GHz PC for software development and results visualization. The control program is written in MATLAB/Simulink real time interface with sampling time of 100  $\mu$ s.

Table 1. Induction motor parameters.

3-phase	0.37 kW	$R_s = 30\Omega$
50Hz	4-poles	$R_r = 31.49\Omega$
230/400V	1.8/1.05A	$L_s = 1.0942H$
$N_r = 1360$ rpm	$L_m = 1H$	$L_r = 1.0942H$

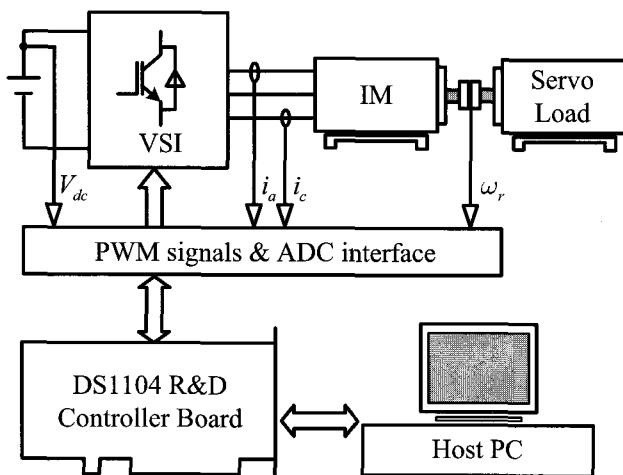


Fig. 6. Block diagram of experimental setup

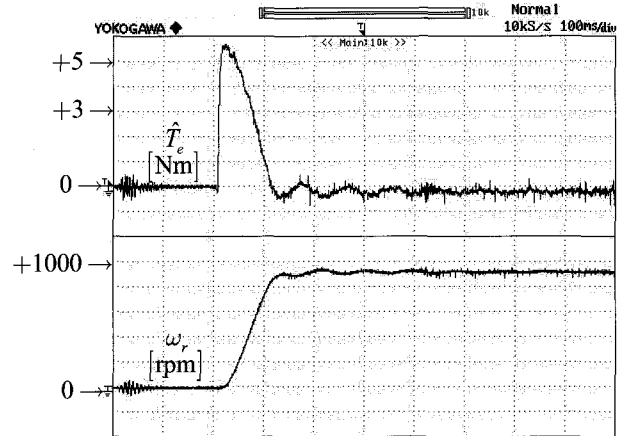


Fig. 7. Experimental results: Estimated torque and speed when the motor start-up to 900 rpm.

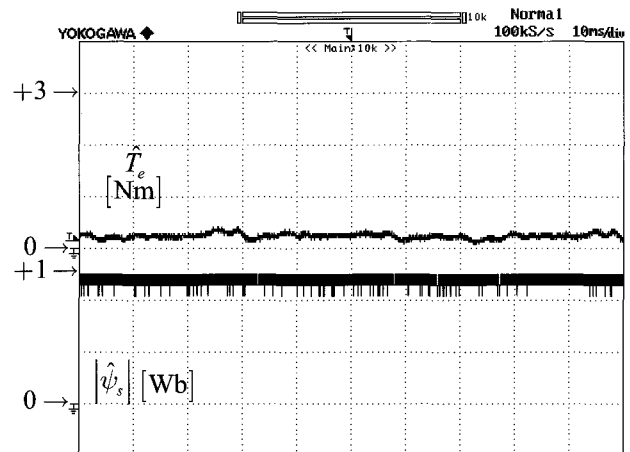


Fig. 8. Experimental results: Estimated torque and stator flux in the no-load steady state with the speed of 900 rpm.

The no-load starting transient performance is presented in Fig. 7. The estimated torque ripple is drastically reduced, while the fast response is preserved.

Figs. 8 and 9 reveal the steady-state responses of the proposed DTC-AAS for no-load and full load operation at 900 rpm. It can be seen that it reduces the torque and stator flux ripple noticeably. It is noted that stator flux droop evidently occurs for the classical DTC which is the problem as mentioned before [3]. As shown in Fig 9, the stator current is nearly distorted by the sector changes as in the classical DTC and the stator current trajectory is evidently circular.

As presented in Fig. 10, stator flux waveform and its circular trajectory, line-to-line SVM motor voltage with 5 kHz switching frequency, causes nearly sinusoidal stator current waveform.

Fig. 11 indicates the torque transients step load change from no-load to full load and from full load to no-load. It can be seen that there is a small change in the stator flux amplitude.

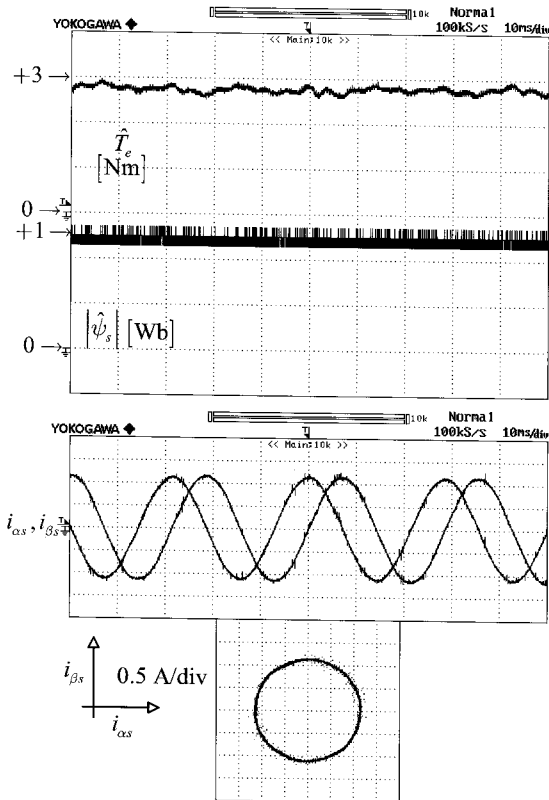


Fig. 9. Experimental results: Estimated torque, stator flux,  $\alpha\beta$  axis, and stator current trajectory at 900 rpm under full load.

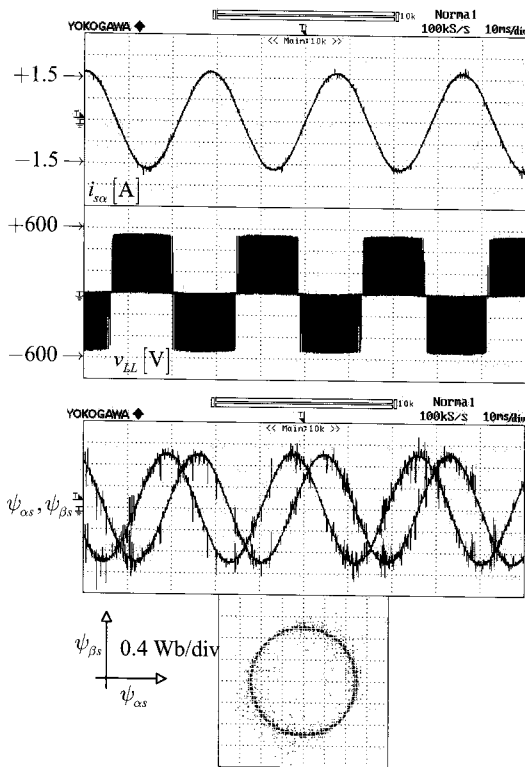


Fig. 10. Experimental results: Stator current, line to line stator voltage,  $\alpha\beta$  axis and stator flux trajectory at 900 rpm under full load.

Fig. 12 shows the speed reversal from -750 rpm to +750 rpm and from +750 rpm to -750 rpm. Some small stator flux oscillations can be observed. The stator current increases during reversal operation. This performance confirms that decoupling operation between amplitude and angle of stator flux vector is able to deal with four quadrant operation.

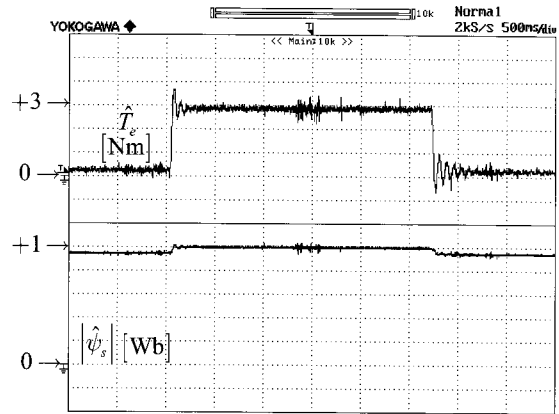
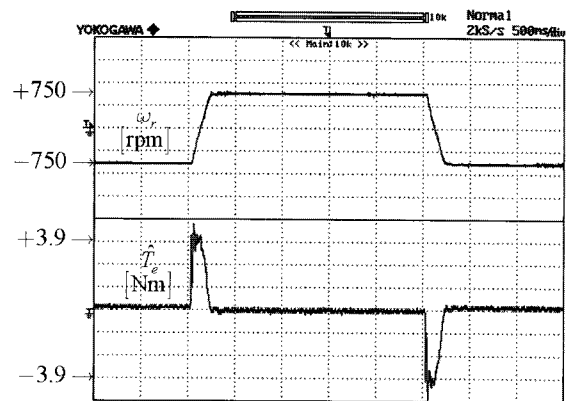
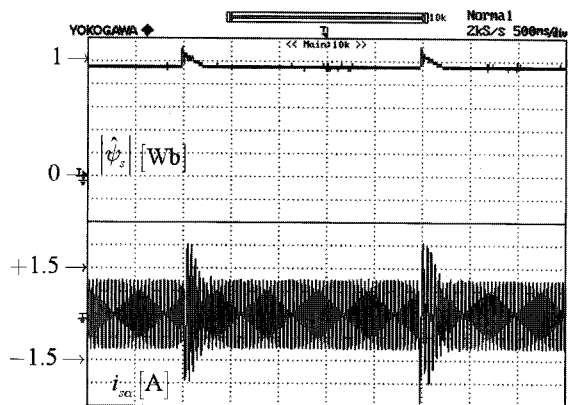


Fig. 11. Experimental results: Estimated torque response and stator flux amplitude when step load torque change from no-load to full load (0 to 2.6 Nm).



(a) Speed and estimated torque



(b) Estimated stator flux and stator current  $\alpha$ -axis

Fig. 12. Experimental results during speed reversal operation from -750 rpm to +750 rpm.

Fig. 13 presents the stator flux angle  $\rho_s$  and  $\alpha$  axis stator flux waveform during speed reversal at low speed operation. It is quite clear that decoupling control between stator flux amplitude and stator flux angle occur since the stator flux amplitude is constant whilst the stator flux angle changes rapidly during speed reversal operation. Also, the stator flux trajectory is still circular after a change in speed direction.

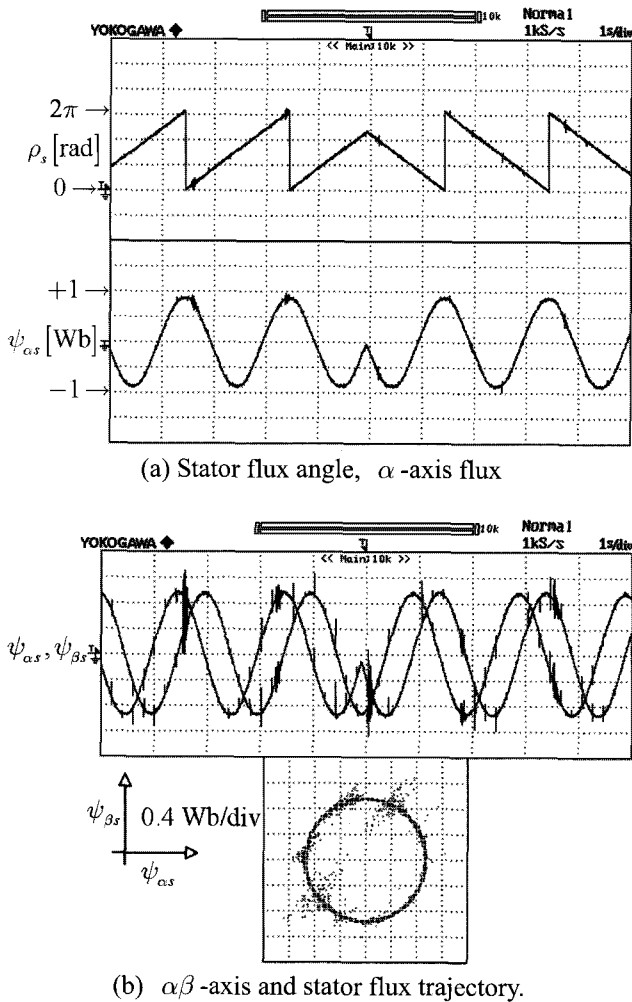


Fig. 13. Experimental results during speed reversal operation at 0.5Hz ( $\pm 15$ rpm).

## 5. Conclusion

This paper has presented the design and the implementation of the SVM controlled inverter fed induction motor. The paper has proposed a decoupling between amplitude and angle of reference stator flux for determining reference stator voltage vector in generating PWM output voltage for induction motors. The experimental results have shown that the proposed strategy has many advantages and features such as reduced torque ripple, reduced stator flux droop during

sector change, no problems during low speed operation, simple control with only one PI torque controller, decoupling operation between stator flux amplitude and stator flux angle, nearly sinusoidal stator current, and constant switching frequency. However, this technique requires accurate rotor speed, which requires a high resolution encoder.

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## Appendix

By Laplace transform (9),

$$\begin{aligned}\hat{T}_e(s) &= \mathcal{L}\left\{k_M\left(1 - e^{-\frac{t}{T_M}}\right)\omega_{sl}\right\} \\ &= k_M\omega_{sl}\mathcal{L}\left(1 - e^{-\frac{t}{T_M}}\right) = k_M\omega_{sl}\left(\frac{T_M s + 1 - T_M s}{s(1 + T_M s)}\right) \quad \text{A.1} \\ &= k_M\left(\frac{1}{(1 + T_M s)}\right)\frac{\omega_{sl}}{s}.\end{aligned}$$

where

$$\omega_{sl}^*(s) = \frac{\omega_{sl}}{s} \quad \text{A.2}$$

Thus, the transfer function of the torque loop  $M(s)$  can be written as

$$M(s) = \frac{\hat{T}_e(s)}{\omega_{sl}^*(s)} = \frac{k_M}{1 + T_M s}. \quad \text{A.3}$$



### Yuttana Kumsuwan

He received his M.Eng degree in Electrical Engineering from the King Mongkut's Institute of Technology, Ladkrabang (KMUTL) in 2001, Bangkok, Thailand. He is currently studying to obtain his Ph.D. degree in Electrical Engineering at the Chiang Mai University. Currently, he is a Lecturer with the Faculty of Engineering, Rajamangala University of Technology, Ianna. His research interests include electric drives, power electronics, and power quality.



### Suttichai Premrudeepreechacharn

(S'91-M'97) received his B.Eng degree in Electrical Engineering, from Chiang Mai University, Chiang Mai, Thailand, in 1988 and his M.S. and Ph.D. degrees in Electric Power Engineering from Rensselaer Polytechnic Institute, Troy, NY, in 1992 and 1997, respectively. Currently, he is an Associate Professor with the Department of Electrical Engineering, Chiang Mai University. His research interests include electric drives, power electronics, power quality, high-quality utility interfaces, and artificial-intelligence-applied power systems.



### Hamid A. Toliyat

(S'87-SM'96) received his Ph.D. degree in Electrical Engineering, from the University of Wisconsin-Madison, in 1991. Currently, he is a Professor of Electrical Engineering, Texas A&M University, College Station. His main research interests and experience include multiphase variable speed drives, fault diagnosis of electric machinery, analysis and design of electric machines, and sensorless variable speed drives. He is an Editor with the IEEE TRANSACTIONS ON ENERGY CONVERSION, an Associate with the IEEE TRANSACTIONS ON POWER ELECTRONICS, and a member of the Editorial Board of the Electric Power Components and Systems Journal. He is also Vice-Chairman of the Electric Machines Committee of the IEEE Industry Applications Society and a Member of Sigma Xi. He is a Senior Member of the IEEE Industry Applications, IEEE Industrial Electronics, IEEE Power Electronics, and IEEE Power Engineering Societies, as well as the recipient of the 2007 IEEE Power Engineering Society Prize Paper Award.