

무정전 전원공급장치 적용을 위한 PWM 인버터의 Digital 실시간 제어

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Real Time Digital Control of PWM Inverter for Uninterruptible Power Supply(UPS) application

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**Abstract** - This paper presents the high performance real time control system of PWM inverter for uninterruptible power supply(UPS). This system is based on a digital control scheme which calculates the pulse widths of the inverter switches for the next sampling time in digital signal processor(DSP). A PI compensator is used to eliminate the voltage error caused by the difference between the actual values of LC filter and those designed. Double regulation loops which are the inner current loop and the outer voltage loop are used to make the transient response time reduce in load disturbance and nonlinear load. This method makes it possible to obtain better response in comparison to conventional digital control system. The proposed scheme provides good performance such as stable operation, low THD of the output voltage, and good dynamic response for load variations and nonlinear load.

1. INTRODUCTION

The uninterruptible power supply(UPS) has been widely used as the emergency power system for the critical load such as computer system. This system consists of a rectifier which supplies the storage energy to the battery tank and an inverter with LC filter which converts a DC source to the sinusoidal AC output. The output performances of the UPS are determined according to the characteristics of the inverter. Nowadays, the harmonic components of the output voltage of an inverter which has nonlinear loads and the dynamic response in case of sudden load change are important factors to estimate the performance of the inverter. From these view points, the PWM techniques are preferred to suppress the harmonic components and to improve the dynamic response.

The sinusoidal PWM or the optimal PWM[1-2] techniques are used to control the fundamental component and to suppress the harmonic components of the output voltage. They are simple and have good characteristics under the steady state. But they operates with poor transient response and the total harmonic distortion factor(THD) of the output voltage increases as the nonlinear load is added. To overcome these problems, the instantaneous feedback control techniques such as hysteresis

control[3] or dead-beat control[4-6] were presented. These techniques improve the several drawbacks of the conventional control schemes. Nevertheless, they can not eliminate the steady state errors completely, and their THD are still serious to make trouble in case of nonlinear loads. And also, the digital control approaches offer some problems like that the available maximum pulse width should be guaranteed to some wider value caused by the computation time delay in microprocessor. The difference between the LC filter values used in actual system and the designed values deteriorates the performance of the controller. In this paper, a new real time digital control technique of the PWM inverter for UPS is presented. This proposed scheme has two variables to control the output voltage. One is the output voltage of the filter capacitor, and the other is the capacitor current. These are formed to double control loop as like as the DC motor controller to get the fast dynamic response of the capacitor output voltage control. They are measured at every sampling time, and used to calculate the on/off time of the PWM pulse at the next sampling time in digital signal processor(DSP). So the PWM pulse patterns are determined one step ahead. Specifically, this system uses a PI compensator to eliminate the output voltage errors caused by the sudden change of load or the deviation of the actual values of LC filter from those designed. The system configuration of the power circuit and control circuit, the digital system modeling, and the results of simulations and experiments are described in this paper. From the simulation and experimental results, the proposed control scheme well provides the low THD of the output voltage and excellent

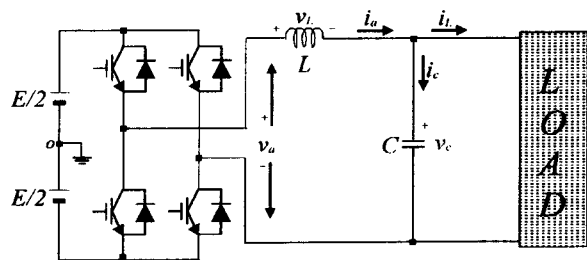


Fig. 1 Circuit diagram of the single phase inverter.

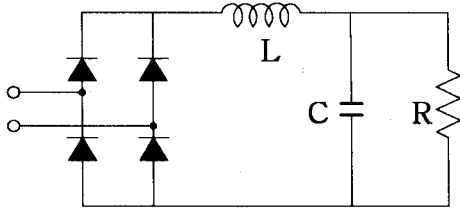


Fig. 2 Power circuit of nonlinear load.

dynamic response in case of sudden load change or nonlinear. The experimental implementation of the system is established using the TMS320C25 DSP.

## 2. SCHEME OF THE PROPOSED CONTROLLER

### 2.1 Plant Modeling

Fig. 1 shows the configuration of the power circuit of the single phase PWM inverter for UPS. The power circuit consists of the full bridge inverter and LC filter. Fig. 2 shows the typical nonlinear load such as diode rectifier. From the Fig. 1, the state equation of the system can be derived as follows:

$$\mathbf{X} = \begin{bmatrix} V_c \\ I_c \end{bmatrix} \quad \mathbf{X} = \mathbf{A}\mathbf{X} + \mathbf{B}U \quad (1)$$

where,

$$\mathbf{A} = \begin{bmatrix} 0 & 1 \\ w^2 & -2w\xi \end{bmatrix}$$

$$\mathbf{B} = \begin{bmatrix} 0 \\ w^2 \end{bmatrix}$$

$$w = \frac{1}{\sqrt{LC}}$$

$$\xi = \frac{1}{2R} \sqrt{\frac{L}{C}}$$

$$U = V_{in}$$

The sampling interval of the control system,  $T$ , is 50[us]. So one period of 60[Hz] reference sine wave is divided into 334 equidistant intervals. The switches are turned on and off once every interval. The inverter output voltage,  $V_{in}$ , takes the value of  $E$ ,  $-E$ , or 0 as the switching state of the devices. Accordingly, the state variables of the output voltage,  $V_c$ , and the capacitor current,  $I_c$ , at the next sampling instant,  $t = (k+1)T$ , is,

$$\mathbf{X}(k+1) = \exp(AT)\mathbf{X}(k) + \int_{(k-1)T}^{(k+1)T} \exp[A(T-\tau)]\mathbf{B}U d\tau \quad (2)$$

From Eq. (2), the sampled data state equation of the plant is presented as the following Eq. (3). The terms which are higher order than pulse width  $U(k)$  in Eq. (3) is neglected, as the magnitude of the pulse width  $U(k)$  is smaller

than the sampling interval. The sampled data state equation of plant is obtained as follows:

$$\mathbf{X}(k+1) = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix} \mathbf{X}(k) + \begin{bmatrix} b_1 \\ b_2 \end{bmatrix} U(k) \quad (3)$$

where

$$a_{11} = \exp(\alpha T) \left( \cos \beta T - \frac{\alpha}{\beta} \sin \beta T \right)$$

$$a_{12} = \exp(\alpha T) \frac{\sin \beta T}{\beta}$$

$$a_{21} = -w^2 \exp(\alpha T) \frac{\sin \beta T}{\beta}$$

$$a_{22} = \exp(\alpha T) \left( \cos \beta T + \frac{\alpha}{\beta} \sin \beta T \right)$$

$$b_1 = Ew^2 \exp\left(\frac{\alpha T}{2}\right) \frac{1}{\beta} \sin \frac{\beta T}{2}$$

$$b_2 = Ew^2 \exp\left(\frac{\alpha T}{2}\right) \left( \cos \frac{\beta T}{2} + \frac{\alpha}{\beta} \sin \frac{\beta T}{2} \right)$$

$$\alpha = -\zeta w, \quad \beta = w\sqrt{1-w^2}$$

### 2.2 Digital control Algorithm

The power circuit is considered as the plant of a closed-loop digital feedback system with a sinusoidal reference. And the controller has only two measuring datas of the output voltage,  $V_c$ , and the capacitor current,  $I_c$ . The basic idea consists in predicting the current,  $I_c$  flowing through the filter capacitor in order to regulate the output voltage, given the linear dependance between the two quantities.

From Eq. (3), the sampled data state equations of the output voltage and the capacitor current are expressed as Eq. (4) and Eq. (5).

$$V_c(k+1) = a_{11} V_c(k) + a_{12} I_c(k) + b_1 U(k) \quad (4)$$

$$I_c(k+1) = a_{21} V_c(k) + a_{22} I_c(k) + b_2 U(k) \quad (5)$$

Combining Eq. (4) and Eq. (5), and replacing the output voltages  $V_c(k+1)$  and  $V_c(k+2)$  by the reference voltages  $V_{cref}(k+1)$  and  $V_{cref}(k+2)$  respectively, the appropriate state of the inverter output voltage is represented,

$$U(k+1) = T_1 V_{cref}(k+2) - T_2 V_{cref}(k+1) - T_3 V_c(k) - T_4 I_c(k) - T_5 U(k) \quad (6)$$

where

$$T_1 = \frac{1}{b_1}, \quad T_2 = \frac{a_{11}}{b_{11}}, \quad T_3 = a_{12} \cdot \frac{a_{21}}{b_1},$$

$$T_4 = a_{12} \cdot \frac{a_{22}}{b_1}, \quad T_5 = a_{12} \cdot \frac{b_2}{b_1}$$



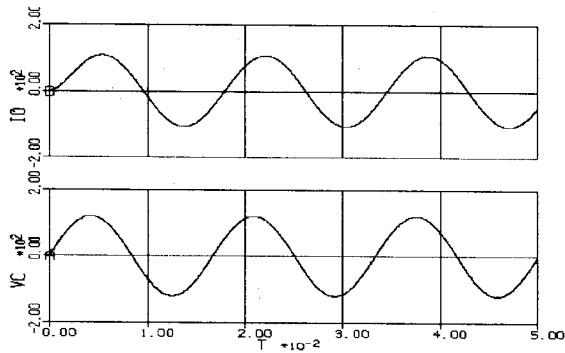


Fig. 6. Simulation result of output waveforms ( $V_c, I_o$ ) with R-L load.

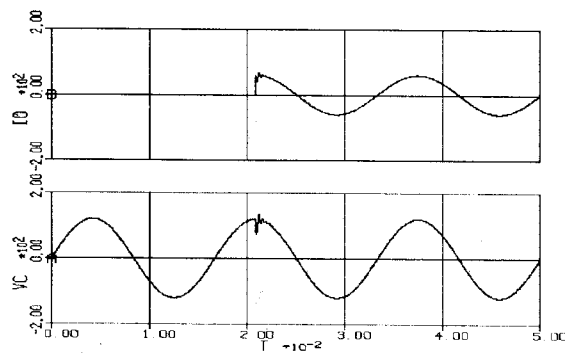


Fig. 7. Simulation result of output waveforms ( $V_c, I_o$ ) with load change (increasing)

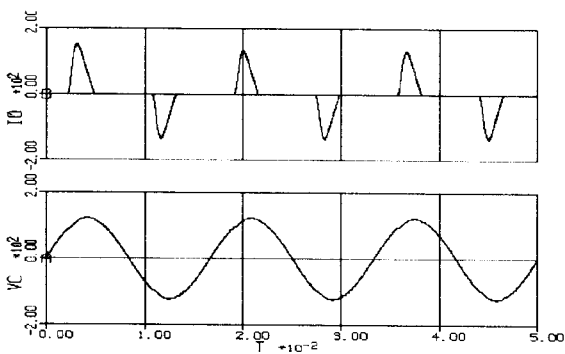


Fig. 8. Simulation result of output waveforms ( $V_c, I_o$ ) with rectifier load.

shown as follows

- [Step 1] Processor initiation and parameter set up.
- [Step 2] Set timer interrupt.
- [Step 3] Get the k-th reference table ( $V_c^*$ ).
- [Step 4] Measure stable variables ( $V_c(k), I_c(k)$ ).
- [Step 5] Calculate Eq. (8) and (9).
- [Step 6] Output the operated  $U(k+1)$ .
- [Step 7] Increment k and return [step 3].

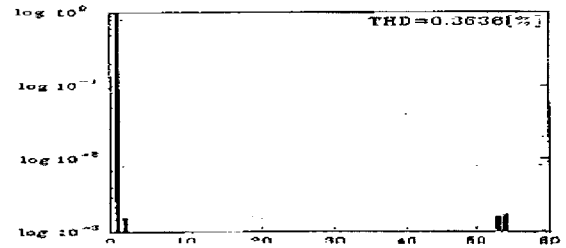


Fig. 9 Simulation spectrum of output voltage ( $V_c$ ) with R-L load.

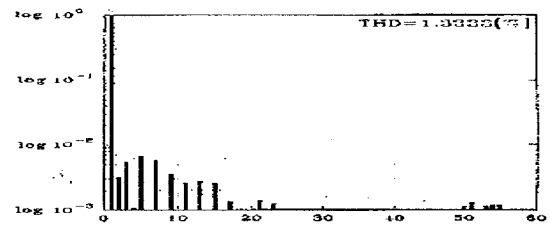


Fig. 10 Simulation spectrum of output voltage ( $V_c$ ) with rectifier load.

This algorithm from [Step 1] to [Step 7] is carried to every  $50(\mu\text{sec})$ , that is, inverter switching frequency  $20(\text{kHz})$ .

#### 4. SIMULATED AND EXPERIMENTAL RESULTS

Characteristics of this new principle of single phase PWM inverter were investigated using digital computer. The proposed digital algorithm was simulated by Advanced Continuous Simulation Language (ACSL) and carried out to study harmonic contents of output voltage under R-L load and rectifier load, respectively. The circuit constants of the system used to simulation are:

Sampling interval	$T = 50(\mu\text{sec})$
Switching frequency	$20(\text{kHz})$
DC link voltage	$160(\text{V})$
Rated load	$5(\text{KVA})$
Output frequency	$60(\text{Hz})$
Output voltage	$120(\text{V})$
Maximum current	$90(\text{A})$
Filter inductance	$200(\mu\text{H})$
Filter capacitance	$100(\mu\text{F})$

In case of R-L load, the simulation result for the output voltage  $V_c$  and the load current  $I_o$  is shown in Fig. 6. Fig. 7 shows the simulation result for the output voltage  $V_c$  and the load current  $I_o$  waveforms when the load is changed from the no load to the rated load. From Fig. 7, there are small transient interval and fast response in load variations. Fig. 8 shows the simulated output voltage  $V_c$  and the load current  $I_o$  waveforms for nonlinear load

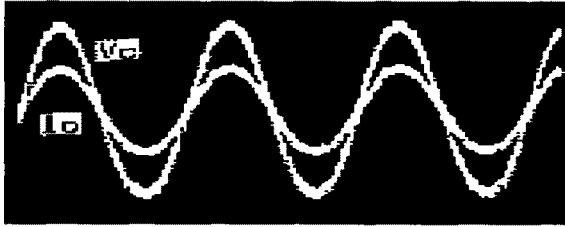


Fig. 11 Experimental result of output waveforms ( $V_c, I_o$ ) with resistor load. (20V/div, 20A/div)



Fig. 12 Experimental result of output waveforms ( $V_c, I_o$ ) with rectifier load. (20 V/div, 20A/div)

with diode rectifier, respectively. The distortion of output voltage is very small, even feeding high di/dt output current. As shown in Fig. 9, spectrum of output voltage is obtained a very low THD 0.3636[%] in R-L load. In case of rectifier load, Fig. 10 shows very low THD 1.3333[%] in spectrum of output voltage. Consequently, it is easy to understand that the proposed control technique well performs excellent response and robustness for various cases such as sudden load variation and rectifier load.

In order to confirm the validity of the theory, experiments were carried out for two types. Fig. 11 shows the experimental output voltage  $V_c$  and the load current  $I_o$  waveforms for linear load. Fig. 12 shows the experimental output voltage  $V_c$  and the load current  $I_o$  waveforms for nonlinear load with diode rectifier. From the experimental results, the output waveforms are nearly close to the sinusoidal waveform such as nonlinear load.

## 5. CONCLUSION

This paper describes a new real time digital controller which is used prediction method of capacitor current and a PI compensator for a UPS inverter. Specifically, this system uses a PI compensator to eliminate the output voltage deviation. Output voltage and capacitor current are formed to double control loop as like as the DC motor controller to get the fast dynamic response of the capacitor output voltage control.

From the simulation and experimental results, it is shown that the proposed scheme has good

performance such as stable operation, very low THD of the output voltage, and good dynamic response for the nonlinear load such as diode bridge rectifier. The experimental implementation of the system is established by using the TMS320C25 DSP. This type of PWM inverter system is particularly suitable for solar cell and fuel cell energy converters.

## (REFERANCES)

- [1] G. S. Buja, "Optimum Output Waveform in PWM Inverters", IEEE Trans. Ind. Appl. Vol. IA-16 pp.830-836, 1980.
- [2] P. Zigas, "Delta Modulation Technique in Static PWM Inverters", IEEE Trans. Ind. Appl. Vol. IA-17, pp. 289-295, 1981.
- [3] A. Kawamura and R.G.Hoft, "Instantaneous feedback controlled PWM inverter with adaptive hysteresis", IEEE Trans. Ind. Appl., Vol. IA-20, pp. 769-775, 1984.
- [4] I. Takahashi and M. Nunokawa, "Prediction Control for a Cycloconverter of a Power Distortion Compensation System", Conf. Rec. IEEE IAS Ann. Meeting, pp. 766-777, 1987.
- [5] A. Kawamura, R. Churayapratip, and T. Haneyoshi, "Deadbeat Controller PWM Inverter with Modified Pulse Patterns for Uninterruptible Power Supply", IEEE Trans. Ind. Elec., Vol.35, No.2 May, pp 295-300, 1988.
- [6] T. Kawabata, T. Miyashita, and Y. Yamamoto, "Digital control of three phase PWM inverter with L-C filter", IEEE Trans. Pow. Elec., Vol. 6, No.1, pp229-239, 1991