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Computation for Deformation Modes of a Flexible Body in Multibody System using Experimental Modal Analysis

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Key Words : Experimental modal analysis(), Flexible multibody dynamic analysis(), Deformation mode(), Degree of freedom(DOFs,), Ortho-normalization(), (DOFs expansion)

Abstract

This paper presents a computational method for deformation modes of a flexible body in multibody system from the experimental modal analysis and an efficient method for flexible multibody dynamic analysis by use of the modes. It is difficult to directly use experimental modal parameters in flexible multibody dynamic analysis. The major reasons are that there are many inconsistencies between experimental and analytical modal data and experimental noises are inherent in the experimental data. So two methods, such as, a method for ortho-normalization of experimental modes and the other one for mode expansion, are suggested to gain deformation modes of a flexible body from the experimental modal parameters. Using the virtual work principle, the equation of motion of a flexible body is derived. The effectiveness of the proposed method will be verified in the numerical example of cab vibration of a truck by comparing analysis and test results.

1.

(noise)

가

CAE (Computer Aided

Engineering),

CAE

(modal

correlation)

(1),(2)

, CAE

(ortho-normalization method)

(DOFs expansion method)^(3,4,5)

(Experimental modal analysis)⁽⁵⁾

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. 2

$$\mathbf{C} = \Psi^{T+} \mathbf{c} \Psi^+ \tag{3.c}$$

3

(pseudo-inverse matrix)^(5,6) Ψ^+ Ψ

. 4

Cab

3.

. 5

, 6

2.

가
가

(4)

(3.5,6)

$$\mathbf{M} \ddot{\mathbf{v}} + \mathbf{C} \dot{\mathbf{v}} + \mathbf{K} \mathbf{v} = \mathbf{f} \tag{1}$$

$$\mathbf{v} \in R^{Na}, \mathbf{f} = \mathbf{f}_E + \mathbf{f}_I$$

\mathbf{v} Na

\mathbf{f}

\mathbf{f}_E

\mathbf{f}_I

가

3.1

(Ortho-normalization)

(1)

(Na)

(3)

(Nb)

(3.5,6)

(6),

Ψ_i ,

ω_i

ξ_i

\mathbf{v}_b

\mathbf{q}

Φ_b

$$\Psi = [\Psi_1 \dots \Psi_i \dots \Psi_{Ne}] \tag{2.a}$$

$$\mathbf{v}_b = \Phi_b \mathbf{q} \tag{4}$$

$$\mathbf{v}_b \in R^{Nb}, \Phi_b \in R^{Nb \times Ne}, \mathbf{q} \in R^{Ne}$$

$$\Lambda = [\omega_i^2] \tag{2.b}$$

b

가 Nb

$$\mathbf{c} = [2 \cdot \xi_i \cdot \omega_i] \tag{2.c}$$

Φ_b

(normalization)

\mathbf{M}_b

\mathbf{K}_b

Φ_b

(3.a)

(3.b)

$$\Psi \in R^{Nb \times Ne}, \Psi_i \in R^{Nb}, \Lambda \in R^{Ne \times Ne},$$

$$\mathbf{c} \in R^{Ne \times Ne}$$

Nb

Ne

Ψ Nb

Λ

Ne

(mass-normalization)

(1)

Ψ_b

(projection),

$\hat{\mathbf{M}}_e$

$\hat{\mathbf{K}}_e$

$$\mathbf{M} = \Psi^{T+} \Psi^+ \tag{3.a}$$

$$\hat{\mathbf{M}}_e = \Psi_b^T \mathbf{M}_b \Psi_b \tag{5.a}$$

$$\mathbf{K} = \Psi^{T+} \Lambda \Psi^+ \tag{3.b}$$

$$\hat{\mathbf{K}}_e = \Psi_b^T \hat{\mathbf{K}}_b \Psi_b \tag{5.b}$$

$$\hat{\mathbf{M}}_e \in R^{Ne \times Ne}, \hat{\mathbf{K}}_e \in R^{Ne \times Ne}, \Psi_b \in R^{Nb \times Ne}$$

$$\hat{\mathbf{M}}_e \quad \Psi_b \quad (\text{orthogonality})$$

$$\hat{\mathbf{M}}_e \quad \hat{\mathbf{M}}_e \quad \tilde{\mathbf{M}}_e$$

$$\hat{\mathbf{M}}_e \quad \tilde{\mathbf{S}}_e \quad \tilde{\mathbf{M}}_e$$

$$\tilde{\mathbf{S}}_e = \tilde{\mathbf{M}}_e^{-\frac{1}{2}} \quad (6)$$

$$\tilde{\mathbf{S}}_e \quad i \quad \tilde{s}_i \quad ,$$

$$\tilde{\Psi}_b \quad i \quad \tilde{\psi}_i \quad \Psi_b \quad i$$

$$\Psi_i \quad .$$

$$\tilde{\psi}_i = \tilde{s}_i \quad \Psi_i \quad (7)$$

$$\tilde{\Psi}_b \quad (5)$$

$$\tilde{\mathbf{K}}_e \quad \tilde{\mathbf{M}}_e$$

$$\tilde{\Phi}_e \quad ,$$

$$\Psi_b \quad (\text{projection})$$

$$\bar{\Psi}_b \quad \tilde{\Phi}_e$$

$$\bar{\Psi}_b = \Psi_b \tilde{\Phi}_e \quad (8)$$

$$\bar{\Psi}_b \in R^{Nb \times Ne} \quad , \quad \tilde{\Phi}_e \in R^{Ne \times Ne}$$

3.2 (Expansion)

$$(Nb)$$

$$\mathbf{v}_b \quad \mathbf{q}$$

$$\Phi_b \quad (4)$$

$$Nc$$

$$(Nt = Nb + Nc)$$

$$\Psi_f \quad (\text{mode})$$

expansion method)^(3,5,6)

$$\hat{\Psi}_f = \mathbf{T}_f \Psi_b \quad (9)$$

$$\hat{\Psi}_b = \mathbf{T}_b \Psi_b \quad , \quad \hat{\Psi}_c = \mathbf{T}_c \Psi_b$$

$$\hat{\Psi}_f = \begin{bmatrix} \hat{\Psi}_b \\ \hat{\Psi}_c \end{bmatrix} \quad , \quad \mathbf{T}_f = \begin{bmatrix} \mathbf{T}_b & \mathbf{0} \\ \mathbf{0} & \mathbf{T}_c \end{bmatrix}$$

$$(Nb) \uparrow$$

$$(Ne) \quad (\text{fitting})$$

$$\hat{\Psi}_b \quad (\text{smoothing})$$

$$\hat{\Psi}_c \quad \Psi_b$$

$$\mathbf{T}_c \quad .$$

4.

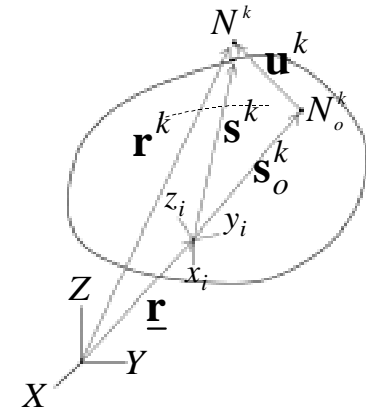


Fig. 1 Kinematics of a flexible body

$$1 \quad \{X - Y - Z\}$$

$$N^k \quad \{X - Y - Z\}$$

$$\mathbf{r}^k = \mathbf{r} + \mathbf{A} \mathbf{s}^k = \mathbf{r} + \mathbf{A} (\mathbf{s}_o^k + \mathbf{u}^k) \quad (10)$$

$$\mathbf{r} \quad \mathbf{A}$$

$$\{x_i - y_i - z_i\}$$

$$\mathbf{s}_o^k \quad \mathbf{u}^k$$

$$N^k$$

$$\mathbf{r} \quad \mathbf{r} \quad \mathbf{r} \quad \mathbf{r}$$

$$N^k \quad \omega^k \quad \dot{\omega}^k$$

$$\omega^k = \omega + \dot{\phi}^k \quad (11.a)$$

$$\dot{\omega}^k = \dot{\omega} + \tilde{\omega} \dot{\phi}^k + \ddot{\phi}^k \quad (11.b)$$

$$\phi^k \quad N^k$$

$$N^k \quad \mathbf{v}^k \quad \mathbf{u}^k$$

$$\mathbf{v}^k = \Psi^k \mathbf{q} \quad (12)$$

$$\mathbf{v}^k = (\mathbf{u}^{kT} \quad \phi^{kT})^T \quad , \quad \Psi^k = (\Psi_t^{kT} \quad \Psi_r^{kT})^T$$

$$\mathbf{u}^k = \Psi_t^k \mathbf{q}, \quad \mathbf{\phi}^k = \Psi_r^k \mathbf{q} \quad (Nb)$$

$$\mathbf{v} \quad (Nf) \quad 3 \quad (Nc)$$

$$(Nd) \quad N^k (k = 1, Nn)$$

$N^i (i = 1, Nm)$

$N^j (j = 1, Ns)$

$$\mathbf{v} = \begin{pmatrix} \mathbf{v}_m \\ \mathbf{v}_s \end{pmatrix}, \quad \Psi = \begin{pmatrix} \Psi_m \\ \Psi_s \end{pmatrix} \quad (13)$$

$$\mathbf{v}_m = \begin{pmatrix} \mathbf{v}_m^1 \\ \vdots \\ \mathbf{v}_m^i \\ \vdots \\ \mathbf{v}_m^{Nn} \end{pmatrix}, \quad \mathbf{v}_s = \begin{pmatrix} \mathbf{v}_s^1 \\ \vdots \\ \mathbf{v}_s^j \\ \vdots \\ \mathbf{v}_s^{Ns} \end{pmatrix},$$

$$\mathbf{v}_m^i = \begin{pmatrix} \mathbf{u}_m^i \\ \boldsymbol{\phi}_m^i \end{pmatrix}, \quad \mathbf{v}_s^j = \begin{pmatrix} \mathbf{u}_s^j \\ \boldsymbol{\phi}_s^j \end{pmatrix}$$

$m \quad s$

$$\mathbf{u}_m^i = \Psi_{mt}^i \mathbf{q} \quad (14.a)$$

$$\boldsymbol{\phi}_m^i = \Psi_{mr}^i \mathbf{q} \quad (14.b)$$

$$\mathbf{u}_s^j = \mathbf{0} \quad (15.a)$$

$$\boldsymbol{\phi}_s^j = \mathbf{0} \quad (15.b)$$

$$(11) \quad (14) \quad (15) \quad \underline{\mathbf{r}}_m^i, \quad \underline{\mathbf{r}}_s^j$$

$$\underline{\mathbf{r}}_m^i = \underline{\mathbf{r}} + \mathbf{A}(\mathbf{s}_{m0}^i + \Psi_{mt}^i \mathbf{q}) \quad (16.a)$$

$$\underline{\mathbf{r}}_s^j = \underline{\mathbf{r}} + \mathbf{A} \mathbf{s}_{s0}^j \quad (16.b)$$

가

$$\delta \pi_s^j \quad \text{가} \quad \delta \mathbf{r}_m^i, \quad \delta \mathbf{r}_s^j \quad \text{가} \quad \delta \pi_m^i, \quad \text{R10000 Cab}$$

$$\delta \underline{\mathbf{r}}_m^i = \delta \underline{\mathbf{r}} - \mathbf{A} \tilde{\mathbf{s}}_{mt}^i \delta \pi + \mathbf{A} \Psi_{mt}^i \delta \mathbf{q} \quad (17.a)$$

$$\delta \underline{\mathbf{r}}_s^j = \delta \underline{\mathbf{r}} - \mathbf{A} \tilde{\mathbf{s}}_{s0}^j \delta \pi \quad (17.b)$$

$$\delta \pi_m^i = \delta \pi + \Psi_{mr}^i \delta \mathbf{q} \quad (18.a)$$

$$\delta \pi_s^j = \delta \pi \quad (18.b)$$

가

(2)

$$\delta A + \delta E_d = \delta W_e \quad (19)$$

$$\delta A, \quad \delta E_d, \quad \delta W_e$$

가, 가, 가

$$\delta \mathbf{r}, \quad \delta \pi, \quad \delta \mathbf{q}$$

$$(\delta \underline{\mathbf{r}}^T \quad \delta \pi^T \quad \delta \mathbf{q}^T) \left\{ \hat{\mathbf{M}} \begin{pmatrix} \ddot{\underline{\mathbf{r}}} \\ \dot{\boldsymbol{\omega}} \\ \ddot{\underline{\mathbf{q}}} \end{pmatrix} + \hat{\mathbf{S}} + \hat{\mathbf{U}}_m - \hat{\mathbf{f}}_m \right\} = \mathbf{0} \quad (20)$$

$$\hat{\mathbf{M}} = \hat{\mathbf{M}}_m + \hat{\mathbf{M}}_s$$

$$\hat{\mathbf{S}} = \hat{\mathbf{S}}_m(\boldsymbol{\omega}, \mathbf{q}, \dot{\mathbf{q}}) + \hat{\mathbf{S}}_s(\boldsymbol{\omega})$$

$$\hat{\mathbf{M}}_m \quad \hat{\mathbf{M}}_s$$

$\hat{\mathbf{S}}_m$

$\hat{\mathbf{S}}_s$

$$\hat{\mathbf{U}}_m \quad \hat{\mathbf{f}}_m$$

(1)

5.

panel) Cab (back

가 (steering wheel) 가

MSC/NASTRAN⁽⁷⁾,
DADS⁽⁸⁾
CADA-X

SGI

R10000 Cab 2

Cab

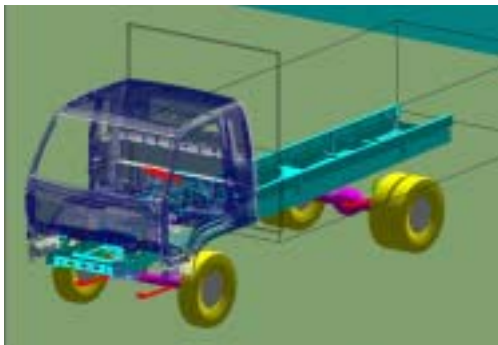


Fig. 2 Multibody truck model

Cab BIW(Body In White)

561 3 187
 X, Y Z 3 가
 50Hz 5

Cab BIW (back panel) 가

4

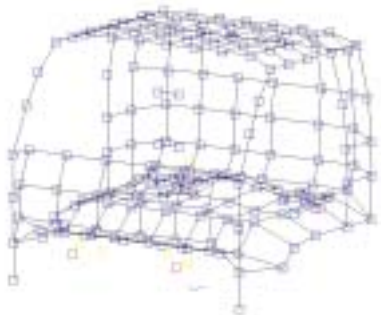


Fig. 3 Measuring points of Cab BIW

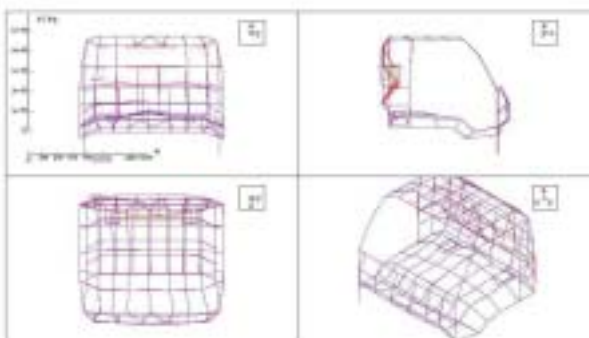


Fig. 4 An example of experimental identified mode shapes

가

5

MAC ⁽⁶⁾ 0.44
 (modal correlation)
 15,706 4 Cab BIW
 가 6



Fig. 5 Finite element model(MAC=0.44)

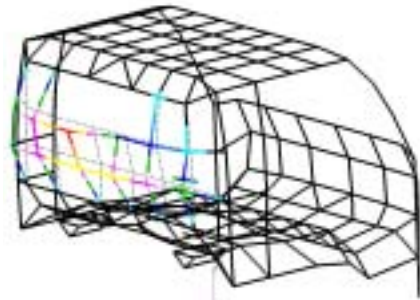


Fig. 6 An example of ortho-normalized experimental mode

가
 가

가

가 5 5
 (MAC=0.44)
 Cab BIW

가

7

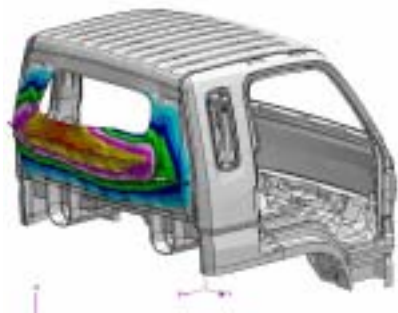


Fig. 7 An example of ortho-normalized and DOFs expanded experimental mode

6.

BIW
5
가
50Hz
Cab
가
7
가
15Hz
가
15Hz
가
Cab
가
MAC
가
0.44
MAC
0.85
(correlation level)

(1)

(2)

(modal correlation)

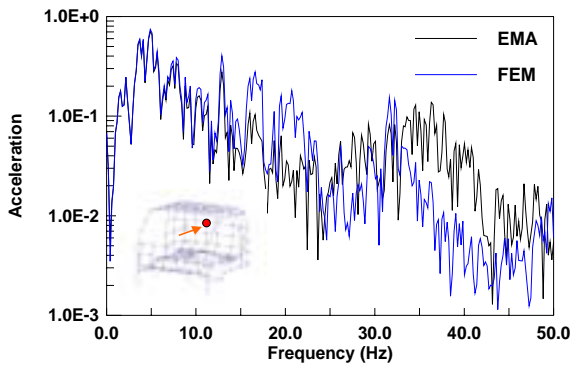


Fig. 8 Comparison of vibration of cab

Cab BIW

(door),

가

Cab

가

가

8

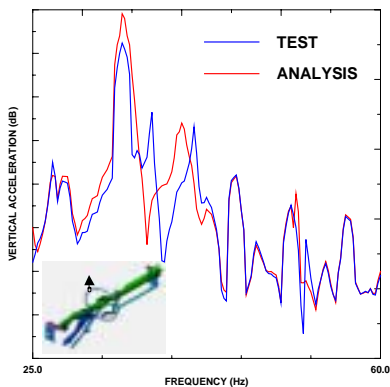


Fig. 9 Comparison of vibration of steering wheel

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