# 새로운 커뮤테이션 기법을 갖는 단상 매트릭스 컨버터 

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# Single Phase Matrix Converter with Novel Commutation Strategy 

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#### Abstract

In this paper, a single phase matrix converter circuit with novel commutation technique is proposed. With commercial IGBT modules, the proposed converter is quite compact in structure and easy to build. The applied commutation strategy introduces a simple RC circuit as commutation aid without need for sensing information, leading to stable and reliable operation. The modulation method is explained; the detailed commutation procedure is illustrated. Finally, the simulation results show the validity and verification of the proposed single phase matrix converter.


## 1. Introduction

Direct $\mathrm{AC}-\mathrm{AC}$ converters based on matrix converter topology have received considerable researching interest in recent years, especially the three phase matrix converter. However, the single phase matrix converter has rarely been dealt with. The single phase matrix converter was first realized by Zuckerberger [1], there are also some works done by Xahirrudin in $[2,3]$. In this paper, with a smart arrangement of common-collector and common-emitter bidirectional switch structure, a single phase matrix converter circuit with four commercial available IGBT modules is built, leading to compact structure and relatively high power density.
In order to construct a reliable matrix converter, it is important to overcome the problem of commutation of the current path between the bidirectional switches. In the proposed converter, for commutation purpose, a simple RC circuit is added as commutation aid. With traditional dead time commutation technique applied, the operation is quite stable and robust.
In this paper, the modulation method in [3] is applied and reviewed; the commutation operation is described. Finally, simulation results support the validity and verification of the proposed converter circuit and commutation technique.

## 2. Sigle phase matrix converter circuit

Fig. 1 shows the practical circuit topology of a single phase to single phase matrix converter. As seen in Fig. 2, the converter mainly consists of four bidirectional switches. Namely, $S_{1}-S_{2}, S_{3}-S_{4}, S_{5}-S_{6}, S_{7}-S_{8}$ are noted as $S_{d+}, S_{d^{-}}, S_{b^{-}}$ and $S_{b+}$ respectively. $S_{a+}$ and $S_{b-}$ are of common emitter arrangement; $S_{a-}$ and $S_{b+}$ are of common collector structure. It also can be seen from Fig. 1 that in order to build such a converter, four commercial IGBT modules are needed. The modules are $S_{1}-S_{7}, S_{2}-S_{4}, S_{3}-S_{5}, S_{6}-S_{8}$. With these four IGBT modules smartly arranged, the circuit structure is very compact and the converter will be easy to build. Cf is input filter component, while $L$ and $R$ are loads. Extra elements $C_{s 1}, C_{s 2}, R_{s 1}, C_{s 3}, C_{s 4}$ and $R_{s 2}$ are added for commutation purpose. The gating signals for IGBTs are in the type of Pulse Width Modulation (PWM), and will be shown in Fig. 2. It should be noted that a short dead time $t_{d}$ is inserted. The generation of gating logic will be quite simple.

## 3. Modulating formulation

The input voltage $v_{s}(t)$, output current $i_{o}(t)$, and fundamental output voltage $V_{\text {ofum }}(t)$ are given by

$$
\begin{gather*}
v_{s}(t)=V_{s} \sin \left(\omega_{i} t\right)=V_{s} \sin (\theta)  \tag{1}\\
i_{o}(t)=I_{L} \sin \left(\omega_{o} t+\phi\right)  \tag{2}\\
v_{\text {ofin }}(t)=V_{o} \sin \left(\omega_{o} t+\psi\right) . \tag{3}
\end{gather*}
$$

In order to explain the modulation strategy, it is necessary to look into a single switching period. This is quite the same with the analysis of conventional voltage source converters. Under the assumption that the switching frequency $f_{s}$ is much higher than both input frequency $f_{i}$ and output frequency $f_{o}$, it is reasonable to treat the input voltage as a constant value $V_{i}$ in one switching period. Fig. 3 shows the input voltage, output voltage and output current waveform in one switching period. In Fig. 3, it is supposed that the instant input voltage has a positive value $V_{i}$. The output


Fig. 1 Single phase matrix converter circuit topology


Fig. 2 IGBT gating signals
current is also assumed to be positive.
In the first subinterval $0-d T_{s}, S_{a+}$ and $S_{b^{-}}$are on, $S_{a^{-}}$and $S_{b+}$ are off. The output voltage $V_{o}$ is equal to $V_{i}$. The circuit equations are

$$
\begin{gather*}
v_{o}=V_{i} \quad\left(0<t<d T_{s}\right)  \tag{4}\\
i_{o}=\frac{V_{i}}{L} \cdot e^{-\frac{R}{L} t} \tag{5}
\end{gather*}
$$

In the second subinterval $d T_{S}-T_{s}, S_{a^{+}}$and $S_{b^{-}}$are off, $S_{a^{-}}$ and $S_{b+}$ are on. The output voltage $v_{o}$ is equal to $-V_{i}$. The circuit equations are

$$
\begin{align*}
& v_{o}=-V_{i} \quad\left(d T_{s}<t<T_{s}\right)  \tag{6}\\
& i_{o}=-\frac{V_{i}}{L} \cdot e^{-\frac{R}{L} t} \tag{7}
\end{align*}
$$

The averaged output voltage in one switching period will be

$$
\begin{equation*}
\bar{v}_{o}=\frac{1}{T_{s}} \int_{0}^{T_{s}} v_{o}(t) d t=\frac{1}{T_{s}}\left[d T_{s} V_{i}-(1-d) T_{s} V_{i}\right]=\left(d-d^{\prime}\right) V_{i} \tag{8}
\end{equation*}
$$

where $d=1-d$.
(8) defines the relationship between input and output. Recognizing $\bar{v}_{o}$ as the instant sampled value of (3), the duty


Fig. 3 Synthesis of output voltage ratio $d$ can be determined for every switching period.

In this case, the expression of (3) will be treated as a reference command. Let $V_{\text {oref }}$ be the instant output command, then consider (8) again, (9) can be obtained,

$$
\begin{equation*}
v_{\text {oref }}=\left(d-d^{\prime}\right) V_{i} \tag{9}
\end{equation*}
$$

In (9), $V_{i}$ can be obtained by simultaneously sensing the input voltage through peripheral sensing circuit. Let $V_{\text {isen }}$ be the instantly sensed value of input voltage, then (9) can be written in (10),

$$
\begin{equation*}
d-d^{\prime}=\frac{v_{\text {oref }}}{v_{\text {isen }}}=q \tag{10}
\end{equation*}
$$

Considering $d=1-d$, the duty ratio for IGBTs can be finally calculated as

$$
\begin{equation*}
d=\frac{1+q}{2}, d^{\prime}=\frac{1-q}{2} . \tag{11}
\end{equation*}
$$

It is obvious that

$$
\begin{equation*}
0 \leq d, d^{\prime} \leq 1 \tag{12}
\end{equation*}
$$

Equivalently,

$$
\begin{equation*}
|q| \leq 1 \tag{13}
\end{equation*}
$$

(13) must exist for any time $t$, and this implies the input and the output wave forms must be synchronized and the fundamental of output voltage must cross zero more frequently than the input voltage. Hence, the single phase matrix converter will be a frequency step-up converter. The relation of input frequency $f_{i}$ and output frequency $f_{o}$ will be

$$
\begin{equation*}
f_{o}=r \times f_{i}, \quad \text { where } r=1,2,3 \ldots \tag{14}
\end{equation*}
$$

Based on the previous derivation, the switching pattern can be concluded and the four bidirectional switches will be controlled according to this pattern.

## 4. Commutation procedure

In order to explain the commutation procedure, the upper circuit branch containing $S_{1}, S_{2}, S_{3}$ and $S_{4}$ will be treated as an example. It is assumed that the load current $I_{0}$ flows in the direction shown in Fig. 1. Fig. 4 illustrates the commutation procedure. The bold line in Fig. 4 is used to show current path.

Mode I is the initial state. $S_{1}$ and $S_{2}$ are off, $S_{3}$ and $S_{4}$ are on. Load current Io flows through $D_{3}-S_{4}$. Then dead time begins, all the switches are turned off. Mode II will be the circuit state. Since $C_{S 1}$ and $C_{s 2}$ imply same impedance, $I_{0}$ will separate equally through $C_{s 1}$ and $C_{s 2}$. Hence, $C_{s 1}$ and $C_{s 2}$ will be both charged. When dead time ends, $S_{1}$ and $S_{2}$ will be turned on, Mode III starts. $I_{o}$ commentates to $S_{1}-D_{2}$ path. $C_{S 1}$ discharges and $C_{s 2}$ charges towards $V_{s}$. After the capacitors finishing charging and discharging, Mode IV is the final
state, $I_{0}$ flow through $S_{1}-D_{2}$.
Fig. 5 shows the reversed commutation procedure. Mode 1 is the initial circuit state. It is the same with Mode IV in Fig. 4. $S_{1}$ and $S_{2}$ are on, $S_{3}$ and $S_{4}$ are off. $I_{0}$ flows through


Mode III


Mode II


Mode IV

Fig. 4 Commutation procedure (Set I)


Fig. 5 Commutation procedure (Set II)
$S_{1}-D_{2}$. Then dead time begins and all the switches are turned off and Mode 2 begins. $I_{o}$ will also equally separate and flow through $C_{s 1}$ and $C_{s 2}$. Circuit enters Mode 3 after dead time ends. $I_{0}$ commutates to $D_{3}-S_{4}$. Finally, after the capacitors finishing charging and discharging, Mode 4 is the last state. $I_{0}$ flows through $D_{3}-S_{4}$.
With a simple RC circuit added as commutation aid, the commutation operation dose not require any sensed circuit information, leading to stable and reliable operation.

## 5. Simulation

In order to verify the operation of the designed single phase matrix converter, simulation is performed on PSIM platform. The circuit parameters are

$$
\begin{aligned}
& V_{s}=100 \mathrm{~V}, \mathrm{~L}=5 \mathrm{mH}, \quad R=2.5 \Omega, f_{s}=5 \mathrm{kHz}, \\
& R_{s}=4.7 \Omega, C_{s}=0.22 \mathrm{~F}, t_{d}=0.5 \mu \mathrm{~s} .
\end{aligned}
$$

Fig. 6 and Fig. 7 show the simulation result when output frequency $f_{o}=120 \mathrm{~Hz}$. It can be seen in the simulation figures that the designed single phase matrix converter operates well.

## 5. Conclusions

In this paper, single phase matrix converter is treated.

With smart arrangement of four IGBT modules, the circuit is quite simple and compact. The converter utilizes dead time


Fig. 7 Simulation results when $f_{o}=120 \mathrm{~Hz}$ ( $v_{s}(t): 50 \mathrm{~V} /$ div, $10 \mathrm{~ms} /$ div; $v_{o}(t): 50 \mathrm{~V} /$ div, $10 \mathrm{~ms} /$ div $)$



Fig. 8 Simulation results when $f_{0}=120 \mathrm{~Hz}$ ( $i_{o}(t): 5 \mathrm{~A} / \mathrm{div}, 10 \mathrm{~ms} /$ div; $i_{s}(t): 5 \mathrm{~A} /$ div, $10 \mathrm{~ms} /$ div $)$
commutation with RC commutation aid added, leading to stable and reliable operation. The modulation strategy is described. Commutation operation is also illustrated. Simulation results show the verification of the designed converter.

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## References

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