

# First-principles Investigation on Fundamental Magnetism and Electronic Structures of $\alpha$ -Mn

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## 1. Introduction

Manganese is known to be the most complex metallic element and have four allotropic modifications exhibiting a complex phase diagram [1]. From the various experimental results,  $\alpha$ -Mn, which is the stable phase below 1000 K, orders in non-collinear antiferromagnetic (AFM) structure [2, 3]. The 29 atoms per primitive unit cell (58 atoms per cubic cell) are distributed over four crystallographically inequivalent sites (denoted as Mn<sub>I</sub>, Mn<sub>II</sub>, Mn<sub>III</sub>, and Mn<sub>IV</sub>) with complex simple cubic structure.  $\alpha$ -Mn undergoes a paramagnetic to AFM phase transition at the Néel temperature of  $T_N = 95$  K.

In density functional study, Hobbs *et al.* [4] exhausted extensively structural and magnetic properties of  $\alpha$ -Mn using first-principles calculations with reviews. The  $\alpha$ -Mn formed by strongly magnetic (Mn<sub>I</sub>, Mn<sub>II</sub>) and weakly magnetic (Mn<sub>III</sub>) or even nearly nonmagnetic (NM) (Mn<sub>IV</sub>) atoms in its AFM state. Note that a pseudopotential method very occasionally predicts erroneous higher magnetic moment than a real value due to disregarding the spin polarization of core electrons. For this reason, the studies for more reliable information to the electronic and magnetic properties of  $\alpha$ -Mn have been required. Therefore, we used the all-electron full-potential linearized augmented plane wave (FLAPW) method [5], well known for its most suitable in magnetic system calculation.

## 2. Computational Method

The Perdew-Burke-Ernzerhof form of the generalized gradient approximation (GGA) [6] for the exchange correlation potential was used. An energy cutoff of  $4.58 (2\pi/a)$ , where  $a$  is the lattice parameter, was employed for expanding the linearized augmented plane wave basis set. An  $18.44 (2\pi/a)$  star function cutoff was used for depicting the charge density and potential in the interstitial regions. Lattice harmonics with  $l \leq 8$  were employed to expand the charge density, potential, and wave functions inside each muffin-tin sphere, with radii of 2.0 a.u. for Mn atom. Integrations inside the Brillouin zone (BZ) were performed using the improved tetrahedron method over a  $15 \times 15 \times 15$  mesh within the three-dimensional (3D) BZ.

## 3. Results and Discussions

From previously reported literatures [2-4], the bulk  $\alpha$ -Mn for AFM phase crystallized in a tetragonal structure with the I-42m space group. However, the resultant  $c/a$  ratio estimated too small values which have 0.99955 and 0.9999 for experimental observation [3] and first-principles calculation [4], respectively. Therefore, our calculation was performed that the atomic structure of  $\alpha$ -Mn assumed as cubic symmetry (I-43m space group) for two magnetic states (NM and AFM).

As a result, the equilibrium lattice constant calculated to be 8.572 and 8.667 Å for NM and AFM states, respectively. In ferromagnetic (FM) state case, we could not determine equilibrium lattice constant since the calculated data did not fit well. As compared to experiment [3], these values are reduced to 3.31 and 2.37 % for NM and AFM states, respectively. Furthermore, the AFM state of  $\alpha$ -Mn is energetically favored by 33.55 meV/Mn over the NM state. Above mentioned, there are four inequivalent sites in a simple cubic system, of which the calculated magnetic moments per Mn atoms are listed in Table I. For comparison, the results for neutron diffraction experiment and another first-principles calculation also given. As shown in Table I, our results are in well agreement with theoretical results, but calculated the magnetic moments of Mn<sub>III</sub> and Mn<sub>IV</sub> are not in perfect agreement with experimental results.

Table I. The calculated spin magnetic moments (in units of  $\mu_B/\text{Mn}$ ) at the crystallographically four inequivalent sites of  $\alpha$ -Mn.

Site	Present work	Lawson <i>et al.</i> <sup>a</sup>	Hobbs <i>et al.</i> <sup>b</sup>
MnI	2.82	2.83	2.79
MnII	2.28	1.83	2.22
MnIII	1.34	0.55	1.00
MnIV	0.02	0.47	0.0

<sup>a</sup>Ref. [3] (neutron diffraction measurement)

<sup>b</sup>Ref. [4] (pseudopotential calculation)

#### 4. Summary

In this study, the magnetic and electronic properties of  $\alpha$ -Mn have been investigated using the all-electron FLAPW method based on the GGA. The local magnetic moment of Mn atoms are consistent with previously calculated results. Detailed discussion on the structural, magnetic, and electronic properties of  $\alpha$ -Mn will be given.

#### 5. References

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