Dipole Moment Derivatives and Infrared Intensities of SiH₄ and SiD₄

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Dipole Moment Derivatives and Infrared Intensities of SiH₄ and SiD₄

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The complete neglect of differential overlap (CNDO/2) approximate wavefunctions have been applied to setect the preferred signs for the dipole moment derivatives of SiH₄ and SiD₄ in conjunction with the experimental alternatives. The apparent sign discrepancy from earlier report has been identified. The effective atomic charge for hydrogen was found to be $\chi_{H}/e = 0.229$, more than two times larger in comparison with the values of typical hydrocarbons like CH₄. The anomalously large effective hydrogen charge was interpreted based on a quantum mechanical model as well as the value of atom anisotropy relative to effective atomic charge.

Introduction

Of the many pioneers in molecular spectroscopy, Mulliken was possibly the first to emphasize the importance of infrared intensities'. He recognized that understanding this kind of data is essential for solving the central problem of chemistry; that is, for establishing the relationship between the properties of a material and its structure. However, during most of the period following Mulliken's paper, only limited progress was made in interpreting infrared intensities. Based on his paper, it was taken as self-evident that an interpretive model of intensities must be founded upon the chemical bond concept. Recent efforts to resolve dipole moment derivatives into derivatives of chemical bond moments have resulted in sets of terms in which those describing the interactions between different bonds are of the same magnitudes as those defining the properties of one particular bond². Thus, unlike molecular energies, infrared intensities cannot be adequately reduced to a sum of terms that can be assigned to particular chemical bonds because of the importance of the interaction terms.

The problem of interpreting infrared intensities has improved dramatically within the last 10 years. That was because of the emergence of the concept of dipole moment derivatives as properties of the atoms in a molecule, rather than as properties of its chemical bonds. The atomic properties derived from intensities are, then, contained in the so-called atomic polar tensors^{3.4} and effective atomic charges³. The atomic polar tensor for atom α in a molecule is defined as the conjugate (transposed) gradient of the molecular dipole moment vector, P, written in various notations as³

$$P_{x}^{\alpha} = \nabla_{\alpha}^{*} P = \begin{bmatrix} \frac{\partial P_{x}}{\partial X_{\alpha}} & \frac{\partial P_{x}}{\partial Y_{\alpha}} & \frac{\partial P_{x}}{\partial Z_{\alpha}} \\ \frac{\partial P_{y}}{\partial X_{\alpha}} & \frac{\partial P_{y}}{\partial Y_{\alpha}} & \frac{\partial P_{y}}{\partial Z_{\alpha}} \\ \frac{\partial P_{z}}{\partial X_{\alpha}} & \frac{\partial P_{z}}{\partial Y_{\alpha}} & \frac{\partial P_{z}}{\partial Z_{\alpha}} \end{bmatrix}$$
(1)

and the square of the effective atomic charge is defined as onethird of the sum of squares of the polar tensor components⁶, that is,

$$\boldsymbol{\chi}_{\boldsymbol{a}}^{*} \equiv (1/3) \, \boldsymbol{\nabla}_{\boldsymbol{a}}^{*} \boldsymbol{P} : \boldsymbol{\nabla}_{\boldsymbol{a}} \boldsymbol{P}. \tag{2}$$

This development has led to the discovery of surprising order in intensity data. The polar tensors for a few, but ubiquitous atoms like hydrogen and fluorine, seem to be transferable properties that are characteristic of these atoms to a good approximation⁷⁻¹². Furthermore, the analysis of the integrated intensities of a variety of hydrocarbons, fluorocarbons, and other materials with diverse structures revealed that the effective charges for the hydrogen and fluorine atoms in these systems fell within fairly narrow range of values^{5,13}.

Above observations encourage further testing of the atomic

polar tensor and effective charges for various hydrogen compounds. In this paper we report the interpretation of the intensities of silane, which is the extension of our works on other systems like HCN14, C2H215, SF616, CHF317, SO218, CHCl319, C2N220, and SiF421. Previously Prasad et al. 22 reported the effective hydrogen charge of SiH₄. However, their criterion for choosing the preferred signs for the dipole derivatives with respect to normal coordinates that the correct signs correspond to values of the atomic effective charges which show a maximum difference for the central and terminal atoms was criticized not to be valid in general by many investigators^{10,23}. Furthermore, according to prasad et al.,22 the effective hydrogen charge seems to be considerably larger in SiH₄ than those of usual hydrocarbons. Earlier, two exceptions were noted in the interpretation of intensities as atomic properties. The effective charges observed for the hydrogen atoms in C₂H₂ and HCN were found to be about 2 times larger than the values common to the other carbon-hydrogen systems^{14,15}. In the previous report, however, those anomalously large effective charges could be adequately explained by virtue of their rather ionically bonded protons24. We have, therefore, reinvestigated the polar tensor and effective charge of hydrogen atom in silane in order to determine definitely if the effective hydrogen charge in SiH4 is really different from those of typical hydrocarbons like CH₄.

Method of Calculation

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The experimental value of the integrated intensity of the kth fundamental mode of a molecule has been defined in two ways^{25,26},

$$A_{k} = (1/nl) f \ln (I_{0}/l) d\omega$$
(3)

$$\Gamma_{k} = (1/nl) - f \ln (I_{\bullet}/I) d \ln \omega$$

where, to a good approximation,

$$A_k = \omega_k \Gamma_k \tag{5}$$

(4)

In both, (nl) denotes the product of the concentration of the absorbing species and sample thickness, I_0 and I are the incident and transmitted light intensity, repectively, and ω_k is the wave number at the band center. In the harmonic oscillator linear dipole approximation, the intensity is related to molecular structure in SI units by²⁷;

$$A_{k} = (\pi N_{k}/3g_{k}) \quad (\partial \hat{P}/\partial Q_{k})^{*}$$
⁽⁶⁾

In this expression g_k denotes the degeneracy of the k-th mode, $(\partial \hat{P}/\partial K_k)$ is the derivative of the dipole vector, \hat{P} , with respect to the normal coordinate Q_k , and the other symbols have their customary meaning.

To obtain structural information from intensities it is necessary to transform from normal coordinates to some other more interpretable coordinate set. Until recently, bond and valence angle coordinates, $R \equiv \{R_i\}$, were always chosen, and intensities were interpreted in terms of bond moments. Using the chain rule of differentiation, the transformations are readily carried out,

$$(\partial \hat{P}/\partial Q) = (\partial \hat{P}/\partial R) \quad (\partial R/\partial Q) \tag{7}$$

$$(\partial P/\partial R) = (\partial P/\partial Q) \quad (\partial Q/\partial R) \tag{8}$$

These are equivalent to expressions in the more customarily used matrix notation introduced by Person³ and Wilson²⁷,

$$P_q = P_R L \text{ and } P_R = P_Q L^{-1} \tag{9}$$

In (9), for example, $(P_R)_{ij} \equiv (\partial P_i / \partial R_j)$ and $(L)_{kj} \equiv (\partial R_k / \partial Q_j)$. In 1961, however, Biarge, Herranz and Morcillo⁴ broke with tradition and chose, instead, an atom-centered, Cartesian coor dinate system, X_i ,

$$(\partial \hat{P}/\partial Q) = (\partial \hat{P}/\partial X) (\partial X/\partial Q)$$
(10)

$$(\partial \hat{P}/\partial X) = (\partial \hat{P}/\partial Q) (\partial Q/\partial X) + (\partial \hat{P}/\partial \tau) (\partial \tau/\partial X)$$
(1)

where τ denotes the set of coordinates describing rigid-body translation and rotation which must be included for completeness. Equation (10) can also be written in a matrix form like (9) as follows,

$$P_x = P_q L^{-1} B + P_\tau \beta \tag{12}$$

where B and β are the transformation matrices from the ordinary space fixed Cartesian coordinates to the internal coordinates and the τ coordinates in equation (11), respectively. The explicit implication of P_x is given above in equation (1), and equation (12) is, therefore, the master equation used in this work such that the so-called polar tensor P_x would be obtained from the experimental data by transforming from P_a to P_x .

We note that we may also transform from P_x to P_Q by using the inverse relation of equation (10) to obtain,

$$P_q = P_x A L, \tag{13}$$

where the matrix A is the inverse transformation from internal coordinates to Cartesian coordinates, defined so that BA = I, a square identity matrix. Equation (13) has particular interest in that it is especially easy to calculate the polar tensor P_x from quantum mechanical procedures. One simply calculates the dipole moment at equilibrium and again after a small displacement in the well defined space-fixed X direction of the α atom. The difference in the X component divided by the displacement is taken to be the approximately the derivative,

$$\partial P_x / \partial X_a \approx \Delta P_x / \Delta X_a$$

The change in the total dipole moment vector when the α atom is displaced in the X direction also gives $\partial P_r / \partial X_e$ and $\partial P_s / \partial X_e$. Similarly we can evaluate the other terms in the polar

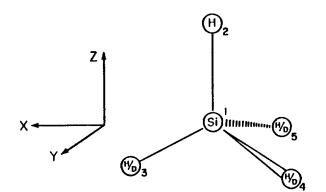


Figure 1. Coordinate axes and molecular orientation of silane used in normal coordinate calculation.

TABLE 1: Structural Data and Definition of Internal and Symmetry Coorrelinates of Silane

Masses (u)* : $m_{\rm SI} = 27.976928 \ m_{\rm H} =$	$1.007825 \ m_{\rm D} = 2.014102$
Structure [*] : R _{SiH} = 0.1481 nm	
Internal coordinates' : $R_1 = \delta r_{12}$	$R_{\phi} = \delta \alpha_{21 \phi}$
$R_2 = \delta r_{13}$	$R_7 = \delta \alpha_{215}$
$R_3 = \delta r_{14}$	$R_4 = \delta \alpha_{415}$
$R_4 = \delta r_{13}$	$R_{3} = \delta \alpha_{314}$
$R_5 = \delta \alpha_{213}$	$R_{10} = \delta \alpha_{315}$

Symmetry coordinates:

$$\begin{array}{cccc} C_{3*} & I_{4} \\ A_{1} & \begin{pmatrix} A_{1} & S_{1} = (I/2) & (R_{1} + R_{2} + R_{3} + R_{4}) \\ F_{1} & \begin{pmatrix} S_{2} = (I/\sqrt{12}) & (3R_{1} - R_{2} - R_{3} - R_{4}) \\ S_{3} = (I/\sqrt{12}) & (3R_{1} - R_{2} - R_{3} - R_{4}) \\ F_{2} & \begin{pmatrix} E_{x} & S_{4} = (I/\sqrt{12}) & (2R_{5} - R_{4} - R_{7} + 2R_{6} - R_{9} - R_{10}) \\ F_{x} & \begin{pmatrix} S_{5} = (I/\sqrt{12}) & (2R_{3} - R_{3} - R_{4}) \\ S_{5} = (I/\sqrt{12}) & (2R_{5} - R_{4} - R_{7} - 2R_{6} + R_{9} - R_{10}) \\ S_{5} = (I/\sqrt{12}) & (2R_{5} - R_{4} - R_{7} - 2R_{6} + R_{9} + R_{10}) \\ \end{array} \\ E_{y} & \begin{pmatrix} E_{y} & S_{7} = (I/2) & (R_{4} - R_{7} - R_{9} + R_{10}) \\ S_{9} = (I/\sqrt{2}) & (R_{3} - R_{4}) \\ S_{9} = (I/\sqrt{2}) & (R_{5} - R_{7} - R_{10}) \\ A_{1} & A_{1} & S_{red} = (I/\sqrt{5}) & (R_{3} + R_{6} + R_{7} + R_{9} + R_{9} + R_{10}) \end{array} \end{array}$$

*Ref. (38); *Ref. (39); *The subscripts refer to the atoms shown in Figure 1; r_{ij} is a Si_i – H_j bond and α_{ijk} is a H_iSi_jH_k angle.

tensor P_x , and combine them to obtain P_x . Using equation (13), we can then convert the calculated polar tensor to P_Q , which can be compared with the experimental value.

The polar tensor values of silane were calculated by means of equation (12) using P_{Q} values of Ball *et al*²⁸. The rotational and translational contribution to P_x , $P_x\beta$, is zero because of the null equilibrium dipole moment and charge. The Cartesian coordinate axes, numbering of atoms, and orientation of silane molecule are shown in Figure 1. The equilibrium structural data, and the definition of the internal and symmetry coordinates are listed in Table 1. The L matrices were calculated using the harmonic force field reported by Duncan²⁹. These values are given in Table 2. The B matrix was evaluated using Wilson's method²⁷.

Results and Discussion

G sum rule graphs employing abscissas and ordinates expressed in terms of squares of atomic effective charges are very useful in comparing the accuracies of infrared fundamental sum values for isotopically related molecules. The G sum rule for silane and its deuterated analogues is given by³⁰

$$(1/K) \sum A_{i} = \chi_{Si}^{2} / m_{Si} + (n_{R}/m_{R} + (4 - n_{R})/m_{D}) \chi_{R}^{2} \qquad (15)$$

where $K = N_A/4\epsilon_o c^2$ and ΣA_i is the fundamental intensity sum. X- and m_o are atomic effective charges and masses and n_H is equal to the number of hydrogens in the molecule under study. In Figure 2, graphical representations of the G sum rule for the intensity data of SiH₄, SiHD₃, and SiD₄ are presented. Since the v₅ band intensity of SiHD₃ was not reported in Bail's paper, it has been assumed here that his value is about 30% greater than that of Levin *et al*²³., for Ball's intensity data are 30% greater at a moderate estimate than those of Levin *et al.* for other bands in SiHD₃. The figure clearly shows that although the SiH₄, SiD₄, and SiHD₃ data of Ball *et al.* result in an in-

TABLE 2: Harmonic Force Field, Normal Coordinates, and Integrated Intensities of Silane

Harmoni	c force o	constants (i	Nm ⁻¹)";		
<i>A</i> ,	$K_{11} =$		F K ₂₃ =	285.7	
E	$K_{22} =$	42.7	$K_{34} =$	-9.6	
			K44 =	52.0	
Normal C	Coordina	ates (u ^{-1/2})*:	1		
SiH₄	F,*		Q,	Q_{\star}	
		S2	1.0184	0.0534	
		<i>S</i> ,	-0.1150	0.9892	
SiD₄	F,		Q,	Q_1	
		S ₂	0.7361	0.0480	
		S3	-0.1345	0.7222	
SiHD	· A,		Q_1	Q_2	Q_3
		S,	0.4925	0.6147	- 0.0056
		Sz	0.8858	0.3602	0.0391
		S3	- 0.0770	0.0683	0.7274
	E_s^s		Q.	Q_s	$Q_{\mathfrak{s}}$
		S.	-0.0211	0.7282	- 0.5638
		S,	0.7352	0.0487	0.0354
		<i>S</i> .	- 0.1551	0.6373	0.5282
Intensities	;(<i>Кт</i> ∙п	iole-'):			
			Ball & Mo	:kean" Levi	n & Kingʻ
SiH.		$A_3(v_3)$	303.7±	3.1 320	0.5±9.0
		4.60.)	300 8 -	4.0 206	3 - 21 7

		Dall of mercan	reau o ruñ.
SiH₄	$A_3(v_3)$	303.7 ± 3.1	320.5 ± 9.0
	$A_{\bullet}(v_{\bullet})$	399.8±4.0	296.3 ± 21.7
SiD₄	$A_3(v_3)$	176.6 ± 1.8	127.1 ± 3.4
	$A_4(v_4)$	210.2 ± 2.1	136.5 ± 8.3
SiHD,	$A_1(v_i)$	96.0±0.9	65.7 ± 1.3
	$A_2(v_2) + A_4(v_4)$	132.6 ± 1.3	122.1 ± 2.4
	$A_3(v_3) + A_6(v_6)$	135.9 ± 1.4	96.4±9.6
	$A_{s}(v_{s})$	_	80.5 ± 2.0

• Ref (29); • The indices labelling the normal coordinates correspond to the labels identifying the vibrational mode given in footnote(g) below; • The K and L elements for the F_x and F_y blocks are identical with those of F_x block; • The L elements for the E_y block are identical with those of E_x block; • The L elements for the E_y block are identical with those of E_x block. E_x in C_3 , point group corresponds to the combination of E_x and F_x in T_a point group. See the definition of symmetry coordinates in Table 1; • Ref (28); • Ref (31); • The indices labelling the vibrational modes correspond to the notations in ref (42).

tersection yielding positive values for χ_{si}^2 and the isotopically invariant quantities, χ_{H}^2 and χ_{D}^2 , the intersection of the G sum rule lines for the data of Levin *et al.* implies imaginary values for the effective charge of silicon atom. One must conclude that the intensity sums for the data of Levin *et al.* are less accurate and somewhat inconsistent with the sums for the data of Ball *et al.* In this respect we have employed Ball's intensity data for the subsequent analysis.

Prasad *et al*²², reported the preferred sign of dipole moment derivatives with respect to normal coordinates, $\partial P/\partial Q_3$ and $\partial P/\partial Q_4$, for SiH₄. However, as mentioned above recalculations are necessary in order to ensure that the sign conventions are consistent throughout the treatment. In Table 3 representative values for silicon atom, hydrogen atom 1, and hydrogen atom 2 of Figure 1 for the atomic polar tensors of SiH₄ and SiD₄ are given. The experimental errors for the individual polar tensor elements are given in parenthesis. The best agreement for the expected isotopically invariant elements of these ten-

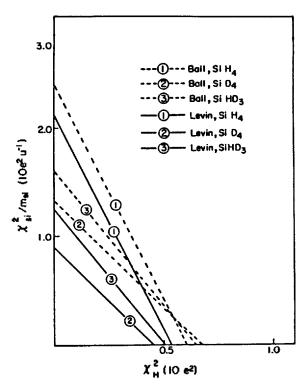


Figure 2. G-sum rule graphs for SiH₄, SiD₄, and SiHD₃, ----; Ball et al's data in ref. (28); -----; Levin *et al*'s data in ref. (31).

TABLE 3:	Atomic Polar	Tensors of Silane	Given in	Multiples of e
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sors occurs for the (\exists) sets for SiH₄ and the (\exists) sets for SiD₄. The differences between the respective polar tensor elements of these sets are either smaller than the sum of the experimental errors of these elements for SiH₄ and SiD₄ or they are slightly larger. The error estimates reported here are minimum values as they contain no contributions due to errors in the normal coordinates. Consideration of these errors could easily increase our error estimates for each of the polar tensor elements by 0.002 *e* which is sufficient to obtain agreement between all the individual elements of these sets.

In order to reach some decision about which of the several possible polar tensors are correct for silane, we may compare the different possible sets of the P, values from the experimental data with the calculated values from the CNDO/2 quantum mechanical calculations, which are given in Table 4. Comparison of the calculated results with the possible experimental results leads us to prefer one sign combination. The calculated values of $\partial P/\partial S_j$ agree reasonably well in magnitude and sign with the experimental dipole moment derivatives from the (-+) sign combinations ($\partial P/\partial Q_3$ negative and $\partial P/\partial Q_4$ positive) for both of SiH₄ and SiD₄. It is generally difficult however to predict quantitatively the dipole moment derivatives from approximate quantum mechanical treatments. Nevertheless, the $\partial P/\partial S_j$ values are large enough leaving no room for doubt about the proper sign choice. In particular any doubts remaining about

			P, ^{\$i}			P #/D(2) ⁶			P#/D(3)	
		(0.005)	0	0]	(^{∓0.207} (0.001)	0	•0	(±0.251 (0.001)	0	∓ 0.162 (0.001)
	(±±)*	0	± 0.141 (0.005)	0	o	∓0.207 (0.001)	0	0	∓ 0.207 (0.001)	0
SiH,•		0	0	± 0.141 (0.005)	0	0	± 0.309 (0.002)	∓ 0.162 (0.001)	0	∓0.150 (0.001)
5114		(^{∓0.920}	0	ر 0	(±0.227	0	0]	(±0.235	0	∓0.003 \
	(±∓)	(0.005)	∓0.920 (0.005)	0	(0.001) 0	± 0.227 (0.001)	0	(0.001) 0	± 0.227 (0.001)	(0.001) 0
		0	0	∓0.920 (0.005)	0	0	± 0.236 (0.002)	∓0.003 (0.001)	0	± 0.228 (0.001) ²
		(0.005)	0	0	7∓0.202 (0.001)	0	0	(0.002) ± 0.283	0	∓0.171 (0.001)
	(±±)	0	± 0.080 (0.005)	0	0	∓0.202 (0.001)	0	0	∓0.202 (0.001)	0
SiD.*		0	0	± 0.080 (0.005)	0	0	±0.344 (0.002)	∓0.171 (0.001)	0	∓0.141 (0.001) ∕
3104		(0.005) (0.005)	0	•)	± 0.227 (0.001)	0	0]	± 0.238 (0.002)	0	∓0.000 \ (0.001)
	(±∓)	0	∓0.910 (0.005)	0	0	± 0.227 (0.001)	0	0	± 0.227 (0.001)	0
		l °	0	∓0.910 (0.005)	0	0	± 0.228 (0.002)	∓0.000 (0.001)	0	±0.227 (0.001) ⁻
		(1.178	0	0 1		0	0)	<u>(</u> -0.267	0	-0.016
SiH	CNDO/2*		1.178 0	0 1.178		-0.311 0	0 -0.261	0	0.311 0	0 - 0.305

*Intensities of silane in ref. (28) were used in this calculation; "The signs are the signs of the $\partial P/\partial Q_i$'s. For example, $(\pm \pm)$ would mean that the signs of $\partial P/\partial Q_s$ and $\partial P/\partial Q_s$ are both either positive or negative; "The atomic polar tensor of hydrogen atom number 2 in Figure 1. "The value with upper sign (+0.141) is, for example, the tensor element obtained from the signs of $\partial P/\partial Q_i$'s corresponding to the upper sign combination (++) in two sets of sign choices (±±). See note b above; The values in parenthesis represent the uncertainties based on the estimated errors in the reported intensities; "These tensors were calculated using the CNINDO program 141 from QCPE. Dipole Moment Derivatives and Infrared Intensities of SiH, and SiD,

TABLE 4: Comparison of Experimental and Calculated Values of $\partial P/\partial S_i$'s for Silane in Units of e

			∂ <i>P,∕∂S</i> 2,	∂P,/∂S₃,
Exptl	SiH4	(±±)*	± 0.356	±0.355
			(0.002)	(0.002)
		(±∓)	± 0.273	∓ 0.389
	1		(0.002)	(0.002)
	SiD4	(±±)	±0.397	±0.345
			(0.002)	(0.002)
		(±∓)	± 0.263	±0.389
			(0.002)	(0.002)
Calcd	CNDO/2		- 0.302	+ 0.532

See the notes in Table 3.

the certainty of the (-+) sign choice may be dispelled by careful examination of Table 3, comparing the atomic polar tensors calculated by the quantum mechanical method with those obtained from the experimental data. Although there may still be some doubt on the possibility of signs of $\partial P/\partial Q_3$ and $\partial P/\partial Q_4$ being both positive, this sign choice gives the polar tensors not only considerably small in magnitude for silicon atom but also exact opposite in sign for the P_{si} element of $P_i^{H(2)}$. It is therefore quite clear that the values calculated agree with the (-+) sign choice and do not agree with the values derived from other sign choices. Thus we believe that the examination of intensity data in the form of atomic polar tensors may be useful in trying to decide such delicate matters as the sign choice to be preferred.

As described above prasad et al²², suggested that one criterion for choosing the preferred signs for the $\partial P/\partial Q_i$'s be that the signs should be preferred that resulted in a maximum value for the difference between the square of the effective charge χ^2_{Si} on the central atom (here silicon) and the sum of $\chi^2_{\rm H}$ values for the terminal atoms (here hydrogen)⁶. The preferred sign choices for SiH₄ and SiD₄ give χ^2_{Si} -4 $\chi^2_{H/D}$ be 0.635 and 0.621 e^2 , respectively which correspond to the maximum differences found by prasad et al. However, since we do not believe there is any physical reason to prefer a maximum or minimum value for this function, we suggest that this criterion be abandoned. Incidently, it is of some interest to note that prasad et al²² obtained the different sign choice (--) using their criterion although their values of effective charges were almost the same as we got. However, one must realize that the signs of $\partial P/\partial Q_i$ values are meaningless without the detailed knowledge of all the definitions used to obtain them. Comparing prasad et al.'s values of χ^2_{α} with ours shows that their (--) convention for the signs of $\partial P/\partial Q_i$'s corresponds to our (-+) convention. We believe there was an inconsistency in the definitions of their normal coordinate calculation.

The results reported here provides additional information on the nature of hydrogen atom effective charges. Since both elements of carbon and silicon belong to group IV in periodic table, it may be interesting to compare the effective hydrogen charge of silane with those of various hydrocarbons. Table 5 contains the effective charges of hydrogen atom for various compounds. This table reveals rather surprising feature that the effective hydrogen charges fall within the ranges

 TABLE 5: Effective Hydrogen Charges for Various Compounds in Natural Units(e)

SiH.	0.229-	C₃H₄	0.105
HCN	0.231*	CH₃F	0.095
C,H,	0.198*	CH3CI	0.068*
CH.	0.096*	CH ₃ Br	0.068
C₂H₄	0.106*	CH₃I	0.071=
C₂H₄	0.093/	CH ₂ F ₂	0.115*
C₄H₄	0.096*	CHF,	0.048°

*This work; *Ref (14); 'Ref (15); *Ref (10); 'Ref (40); 'Ref (3); *Ref (41); ' Ref (40); 'Ref (32); *Ref (32); 'Ref (32); "Ref (32); "Ref (32); "Ref (17).

$\chi_{\rm H} = 0.12 \pm 0.11 e$

in all of the systems listed in Table 5. These results suggest that the effective charge represents a particularly localized combination of chemical bond properties², whose magnitude is most sensitive to the nature of the particular atom and much less sensitive to the nature of other atoms in its vicinity or their geometrical arrangement. It is curious, however, that the effective hydrogen charge in silane shows significant difference from the "typical" value of about 0.1 e for all compounds in Table 5 except C₂H₂ and HCN. The anomalously large effective hydrogen charges in C₂H₂, HCN, and SiH₄ must be rationalized. Just as there is no obvious reason that the effective hydrogen charge in some compounds should be equal, there is no obvious reason that the effective charge for other compounds should deviate so sharply from the others. Indeed, it may not be clear which are the anomalous systems. Whichever point of view is chosen, one cannot resist pointing out one major difference between the properties of hydrogen atoms considered in Table 5. On the basis of author's recent finding²⁴ that the value of the atom anisotropy relative to the effective atomic charge is a very useful parameter in characterizing chemical bonds in terms of atomic properties, C₂H₂, HCN and SiH₄ fall into one group and other compounds in Table 5 fail into another group. The atom anisotropy, β^2 , has been defined as32

$$\chi_{\alpha}^{*} = \langle P_{\alpha} \rangle^{*} + \langle 2/9 \rangle \beta_{\alpha}^{*}$$
(16)

where χ_* is the effective charge of atom α in a molecule and \vec{P}_* is the so-called mean dipole derivative defined as³²

$$\overline{P}_{\alpha} = \frac{1}{3} T_{\tau} P_{x}^{\sigma} \qquad (17)$$

that is, one third of the trace of atomic polar tensor of atom α . The values of author's new parameter²⁴, $a_{\rm H}$ (\equiv | $\frac{\sqrt{2}\beta_{\rm H}}{3\chi_{\rm H}}$ |) for C₂H₂, HCN and SiH₄ are close to 0, the value for a fixed charge. On the other hand, the values of $a_{\rm H}$ for other molecules in Table 5 are rather close to 1. The differences in the values of $a_{\rm H}$ between these two groups of molecules may indicate the different extent of the mobility of the hydrogen atoms in the molecular systems considered here. According to the argument given in the previous report²⁴ for the cases of HCN and C₂H₂, the anomalously large effective hydrogen charge in SiH₄ may be ascribed to the largely ionic character of its bonded protons in comparison with typical hydrocarbons like CH₄. Indeed, semi-empirical CNDO/2 calculation has shown in this work that Mulliken's net hydrogen charge^{35,36} in SiH₄ is more than 10 times greater compared with that of CH₄. These observations would, perhaps, be indicative of the fact that the problem of interpreting infrared intensities can be treated in a more simple and precise way by using the so-called "atomic effective charge".

To further understanding of the anomalously large hydrogen atom effective charge in silane compared with those of hydrocarbons, it will be useful to consider a quantum mechanical model for the polar tensor. Formal expressions for the polar tensor are readily obtained by computing the gradient of the dipole moment. The dipole moment is a measure of the vector difference between the centroids of positive and negative charges in a molecule. For example, in the Born-Oppenheimer approximation this difference is defined, in natural unit³³, as

$$\hat{P}(\hat{R}) = \sum_{n} \hat{R}_{n} q_{n} - f \hat{r}_{o} (\hat{r} ; \hat{R}) d^{2} \hat{r}$$
⁽¹⁸⁾

in which \hat{R} denotes the set of nuclear position vectors, \hat{R}_n , q_n the atomic number of nucleus 7, and

$$\rho(\hat{r}; \hat{R}) = f \|\psi(\hat{r}, \hat{r}_{1}, \cdots, \hat{r}_{N})\|^{2} d^{2} \hat{r}_{1} \cdots d^{3} \hat{r}_{N}$$
(19)

the electron number density at point \hat{r} in an N-electron molecule. Any model dependence in a calculation of polar tensor is introduced by way of the representation chosen for the number density function, $\rho(\hat{r};\hat{R})$ or equivalently, the molecular wave function, $\psi(\hat{r};\hat{R})$, in (19). Since polar tensors are expressed in terms of the Cartesian coordinates of the atoms in a molecule, $\rho(\hat{r};\hat{R})$ is most conveniently represented as a multi-centered expansion in complete sets of orthonormal atomic orbitals centered on each nucleus; that is³⁴,

$$\rho\left(\hat{r}\;;\;\hat{R}\right) = \sum_{\alpha\beta} \sum_{ij} C_{\alpha\beta}^{ij} \psi_{i}^{*}\left(\hat{r}_{\alpha}\right) \psi_{j}\left(\hat{r}_{\beta}\right) \tag{20}$$

in which, for example, $\hat{r}_{\bullet} = (\hat{r} - \hat{R}_{\bullet})$, $\psi_i(\hat{r}_{\bullet})$ denotes the i-th orbital centerd on nucleus α , and $C_{\bullet\theta}^{ij}$ is the the one-electron density matrix element. To further partition (20) into independent atomic contributions, the cross-terms are eliminated by expanding the orbitals centered on one nucleus in terms of orbitals centered on another,

$$\boldsymbol{\psi}_{i}\left(\hat{\boldsymbol{r}}_{\boldsymbol{\sigma}}\right) = \sum_{k} S_{\boldsymbol{\sigma}\boldsymbol{\sigma}}^{ik}\left(\boldsymbol{R}_{\boldsymbol{\sigma}\boldsymbol{\sigma}}\right) \boldsymbol{\psi}_{\boldsymbol{x}}^{*}\left(\hat{\boldsymbol{r}}_{\boldsymbol{\sigma}}\right) \tag{21}$$

where $R_{\alpha\beta} \equiv |\hat{R}_{\alpha} - \hat{R}_{\beta}|$ is the internuclear distance and $S_{\alpha\beta}^{it} \equiv \langle \psi_i(\hat{r}_{\alpha}) | \psi_i(\hat{r}_{\beta}) \rangle$ is the overlap integral. Substitution of (21) into (20),

$$\rho(\hat{r}; \hat{R}) = \sum_{\star} \sum_{\mu} N_{\mu\rho}^{\prime\star} \psi_{\iota}^{\star}(\hat{r}_{\rho}) \psi_{\star}^{\star}(\hat{r}_{\rho})$$
(22)

where

$$N_{\beta\beta}^{ik} \equiv \sum_{\alpha} \sum_{j} C_{\beta\alpha}^{ij} S_{\alpha\beta}^{jk}$$

Integration of (22) over the position variables for an N electron system yields

$$N = f \rho \left(\hat{r} ; \hat{R} \right) d^3 r = \sum_{s} N_s \left(\hat{R} \right)$$
(23)

where

$$N_{\beta}(\hat{R}) \equiv \frac{1}{4} N_{\beta\beta}^{tt}(\hat{R})$$

(24)

is the gross population density defined by Mulliken^{35,36} Substituting (22) into (18), and making use of the relation $\hat{\mathbf{r}} = \hat{\mathbf{r}}_{\beta} + \hat{\mathcal{R}}_{\beta}$, yields the molecular dipole moment as a sum over atomic terms,

 $\hat{P}(\hat{R}) = \sum_{A} \hat{R}_{A} \chi_{A}(\hat{R}) - \sum_{A} \phi_{AA}(\hat{R})$

where

$$\zeta_{s}(\hat{R}) \equiv q_{s} - N_{s}(\hat{R}) \tag{25}$$

is Mulliken's net atomic charge, and

$$\boldsymbol{\Phi}_{\boldsymbol{\rho}\boldsymbol{\sigma}}\left(\boldsymbol{\hat{R}}\right) \equiv \sum_{i,\boldsymbol{\sigma}\boldsymbol{\kappa}} < \boldsymbol{\psi}_{i}\left(\boldsymbol{\hat{r}}_{\boldsymbol{\beta}}\right) \left| \boldsymbol{\hat{r}}_{\boldsymbol{\beta}} \right| \boldsymbol{\psi}_{\boldsymbol{\kappa}}\left(\boldsymbol{\hat{r}}_{\boldsymbol{\beta}}\right) > N_{\boldsymbol{\beta}\boldsymbol{\beta}}^{i\boldsymbol{\kappa}}\left(\boldsymbol{\hat{R}}\right)$$
(26)

Differentiation of (24) finally yields the polar tensor,

$$\nabla_{n}^{*}\hat{P} = \zeta_{n}\hat{I} + \sum_{s} (\nabla_{n}\zeta_{s})\hat{R} - \sum_{s} \nabla_{n}^{*}\Phi_{ss}(\hat{R})$$
(27)

Several models for interpreting infrared intensities can be identified with the terms in eq. (27). The first two terms, in particular, describe the polar tensor obtained in a classical atomic charge model³⁷. The first term describes the contribution of a "net atomic-charge" which follows the motion of the nucleus perfectly, and the second term describes the "charge flux" resulting from the transfer of charge from one nucleus to another as the result of nuclear displacement. The third term is strictly a quantum mechanical term which has no classical analogue. This term arises solely from interference phenomena resulting from the superposition of wave functions. Unfortunately, there is no experimental way of resolving polar tensors into these terms, and they must be estimated by calculation.

The results of such calculations for two representative systems, CH₄ and SiH₄, are summarized in Table 6. There, theoretically estimated polar tensors for the hydrogen atoms in CH₄ and SiH₄, obtained by CNDO/2 calculations, are compared with those obtained from experimental intensities. In both calculations the CH and SiH bonds are coincident with the Z coordinate axis. For axes oriented in this way, the polar tensors are diagonal by symmetry, so that the diagonal elements are listed.

TABLE 6: Comparison fo Hydrogen Polar Tensors in SiH, and CH. Obtained by CNDO/2 Calculations and by Experiments, in Natural Units(e)

CH₄	XX(=YY)	ZZ
<i>ζ</i> " <i>β</i>	0.012	0.012
ΣV _n ζ _ρ Ŕ,	0.046	0.093
−ΣV _H *Φ _{\$\$}	- 0.015	-0.218
V _H *P(calc)	0.043	-0.113
V _B * P (obs)⁴	0.064	- 0.139
	$\chi_{\rm s}({\rm calc})=0.074$	χ _H (obs)° = 0.096
SiH4	XX(=YY)	ZZ
tul.	-0.150	- 0.150
Σ⊽ _{nče} Ŕ,	0.036	0.037
-Σ₹#‡Φ ₩	-0.197	- 0.148
V _H *P(calc)	- 0.311	-0.261
V _H •Ê(obs)∘	-0.227	- 0.232
-	$\chi_{\rm M}({\rm calc}) = 0.295$	$\chi_{\rm ef}(\rm obs)^{\rm s} = 0.229$

*Ref (10); *Average of values derived from data in ref. (28). See Table 3.

Possibly the safest general conclusion to be drawn from these calculations is that all three of the constituent parts of the polar tensors, defined in eq. (27), are significant. Thus, none of the three groups of terms in eq. (27) can be completely neglected in these systems and presumably in others as well. In the two systems considered in Table 6, the "interference" term, $-\sum \nabla_{H_1} \phi_{\mu\mu}$, is a dominant one, but the other terms make comparable contributions. The "perfect following" term reflects, in part, the difference in the electronegativity between central (C or Si) and terminal (H) atoms. The excessively large value of this term in SiH₄ compared with that in CH₄ is consistent with the foregoing that SiH₄ is more ionic than typical hydrocarbons like CH4. Coupled with this first term, the fairly large XX(=YY) component of the "interference" term in SiH, seems to render the effective hydrogen charge of this molecule to be anomalously large. In addition, one may notice that, in SiH4, the XX(=YY) and ZZ components are nearly the same not only in magnitude but also in sign for the three groups of terms in eq. (27). These facts are, thus, accused of the finding that the value of the hydrogen anisotropy relative to the effective hydrogen charge in SiH4 is close to 0, contrary to the cases of typical hydrocarbons like CH, whose values are rather close to 1. The XX component of the "interference term" may reflect specifically the more labile character of electrons in SiH₄ compared with CH₄. Thus, as we suggested in previous report²⁴, the magnitude of the atom anisotropy relative to the effective atomic charge would potentially be a very useful parameter in characterizing chemical bonds in terms of atomic properties only from the infrared intensity data.

In conclusion we see that G sum rule is very useful in comparing the accuracies of infrared fundamental sum values for isotopically related molecules, and that it is very easy to have apparent inconsistencies in signs due to inconsistencies in the arbitrary sign conventions occurring in the calculation of dipole moment derivatives, unless one person carries through the entire calculation from start to finish. When the sign conventions are consistent, the values of $\partial P/\partial S_i$ or of polar tensor elements calculated by the quantum mechanical method are in surprisingly good agreement with experiment. The best values for the H- and Si-atom polar tensors in silane are believed to be given in the (-+) column of Table 3. The effective hydrogen charge was found to be $\chi_{\mu}/e = 0.229 \pm 0.002$, somewhat larger value compared with those of usual hydrocarbons. The large effective hydrogen charge in silane was ascribed to the largely ionic character of its bonded protons in comparison with typical hydrocarbons like CH₄. According to the quantum mechanical model, it was found that the "interference term" is excessively large in the polar tensors, leading to the more labile character of electrons in silane. Combined with above observations, it is likely that the value of the atom anisotropy relative to the effective atomic charge would potentially be a very useful parameter in understanding the chemical bonds solely from the vibrational intensity measurement.

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A Wittig Route to (Z)-13-Eicosen-10-one, the Pheromone of the Peach Fruit Moth, and Its Biological Activity Test

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(Z)-13-Eicosen-10-one, an active component of the sex pheromene of the peach fruit moth was synthesized from 4-oxo-tridecan-1-al and heptylidenetriphenylphosphonium ylide by Wittig reaction. The key intermediate, 4-oxo-tridecan-1-al, was synthesized by three different methods. The biological activity test of the synthetic pheromone as attractant for the male peach fruit moth was tested at several districts in Korea.

Introduction

(Z)-13-Eicosen-10-one, an active component of sex pheromone of the peach fruit moth, Carposina niponensis Walsingham, a major economic pest of apple, peach and other fruits was isolated by Tamaki' in 1977. Structurally, while most lepidopterous pheromones were characterized as unsaturated alcohols, acetates, or aldehydes of 12-, 14-, 16-, or 18-carbon chain length, the sex pheromone of the peach fruit moth is an exceptional unsaturated aliphatic ketone. Several syntheses of (Z)-13-eicosen-10-one have been reported². In 1982, Yoshida²⁴ reported the synthesis of (Z)-13-eicosen-10-one via salt-free Wittig reaction of heptylidenetriphenylphosphonium ylide and 4-oxo-tridecan-1-al(2). 4-Oxo-tridecan-1-al(2) was prepared from 1-(p-tolylsulfonyl) nonane and methyl 4,4-dimethoxybutanoate. Recently, 4-oxo-tridecan-1-al(2) was synthesized by Hernandez² by addition of n-nonyllithium to y-butyrolactone followed by PCC oxidation of the resulting alcohol in his synthesis of (Z)-13-cicosen-10-one(1). In 1981, Naoshima² reported a synthesis of (Z)-13-eicosen-10-one¹ via the Wittig olefination of 4-oxo-tridecan-1-al(2) with heptylidenetriphenylphosphonium ylide in toluene in the presence of 12-crown-4-ether. In this report, 4-oxo-tridecan-1-al(2) was prepared from diethyl 2-oxo-glutarate in five steps.

Institute of Agricultural Sciences in Suwon, Korea needed a fair amount of the pheromone of the peach fruit moth to conduct field test experiments in Korea. We therefore undertook to develop some practical mothods for the synthesis of the pheromone of the peach fruit moth. We wish to report a practical synthesis of (Z)-13-eicosen-10-one(1) via the Wittig olefination of 4-oxo-tridecan-1-al (2) with heptylidene-triphenylphosphonium ylide. The key intermediate, 4-oxo-tridecan-1-al(2) was prepared by three different synthetic mothods. Also we wish to report the results of the biological activity test as attractant for males of the peach fruit moth.

Results and Discussion

It has been well established that the Wittig reaction when carried out between aliphatic aldehyde and aliphatic non-stabilized triphenylphosphonium ylide in salt-free, nonpolar solvent or in polar aprotic solvents such as DMF, DMSO or HMPA gives Z-alkenes stereoselectively³. It has been known that only aldehyde reacts with phosphonium ylide in the presence of ketone⁴. A simple retrosynthetic analysis (Scheme 1) reveals that 4-oxo-tridecan-1-al(2) is the key intermediate.

We have prepared $4-\infty-\text{tridecan}-1-al(2)$, the key intermediate by three different methods and synthesized the pheromone of the peach fruit moth by olefination reaction of $4-\infty-\text{tridecan}-1-al(2)$.

(1) Grignard Route. 4-Oxo-tridecan-1-al(2) was prepared from commercially available acrolein and decanoyl chloride (Scheme 2).

1,4-Addition of HBr to acrolein, followed by protection of the aldehyde portion with 1,3-propanediol afforded 2-(2-bromoethyl)-1,3-dioxane(3)³. Grignard reagent⁶ from 2-(2-bromoethyl)-1,3-dioxane and Mg in THF was added to