

# 합성 강 상자형 도로교의 체계신뢰성 해석 및 안전도평가

## Assessment of System Reliability and Capacity-Rating of Composite Steel Box-Girder Highway Bridges

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### 요 지

본 연구에서는 각종 합성 강상자형 도로교에 대한 체계신뢰성 및 이에 기초한 내하력평가를 위하여 실용적이고 합리적인 신뢰성 모형과 해석방법을 개발하고자 한다.

합성 강상자형교의 신뢰성해석을 위해서는 휨강도 뿐만 아니라 휨, 전단 그리고 비틀림을 동시에 고려한 강도식에 기초하여 한계상태함수를 모형화 하였으며, 체계신뢰성 문제는 각 거더의 주요 파손기구에 기초한 FMA(Failure Mode Approach)방법을 사용하여 직·병렬 조합체계로서 정식화 하고 수치해석기법인 중요도표본추출기법(Importance Sampling Technique ; IST)을 사용하여 해석하였다.

특히 본 연구에서는 추정된 체계신뢰성지수를 일반적인 제 1계 2차모멘트(First Order Second Moment ; FOSM)방법의 형태로 표현하여 유도한 등가의 시스템 내하력으로서 합성 강상자형교의 내하력을 평가하는 실질적이고 합리적인 방법을 제안하였다.

기설 교량에 대한 내하력 및 안전도평가 결과 전체시스템으로서의 보유안전도와 내하력은 교량의 부정정성이 높아질수록 개별 요소의 경우에 비해서 그 차이가 크게 됨을 알 수 있었으며, 제안된 체계신뢰성에 기초한 내하력평가 방법은 기설 합성 강상자형교의 실질적인 내하력평가 방법을 위하여 합리적으로 사용될 수 있을 것으로 사료된다.

### Abstract

This paper develops practical and realistic reliability models and methods for the evaluation of system-reliability and system reliability-based rating of various types of box-girder bridge superstructures.

The strength limit state model for box-girder bridges suggested in the paper are based on not only the basic flexural strength but also the strength interaction equations which simultaneously take into account flexure, shear and torsion. And the system reliability problem of box-girder superstructure is formulated as parallel-series models obtained from the FMA(Failure Mode Approach) based on major failure mechanisms or critical failure states of each girder. In the paper, an improved IST(Importance Sampling Technique) simulation algorithm is used for the system reliability analysis of the proposed models. This paper proposes a practical but rational approach for the evaluation

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of capacity rating in terms of the equivalent system-capacity rating corresponding to the estimated system-reliability index, which is derived based on the concept of the equivalent FOSM(First Order Second Moment) form of system reliability index.

The results of the reliability evaluation and rating of existing bridges indicate that the reserved reliability and capacity rating at system level are significantly different from those of element reliability or conventional methods especially in the case of highly redundant box-girder bridges.

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## 1. Introduction

The optimal decision on the bridge maintenance and rehabilitation involves tremendous economic and safety implication, and heavily depend upon the results of the evaluation of residual safety and carrying-capacity of the existing bridges. However, in spite of the remarkable advances in modelling and numerical or analytical techniques for response or behavior analysis and ultimate strength or stability analysis of highly redundant bridge system such as steel box-girder bridges, it is still extremely difficult to evaluate realistic residual system-safety or system carrying-capacity especially when these bridges are deteriorated or damaged to a significant degree.

It has to be noted that the cross beams and diaphragms as well as concrete decks of box girder bridge significantly contribute to redundancy, and also effectively provide transverse load distribution and the resistance to eccentric loads. Thereby, the capacity rating and safety evaluation of box-girder bridges based on system performance and system reliability are very important for the realistic prediction of residual carrying capacity of these highly redundant bridge system.

Recently, some practical system reliability models and methods for I-girder bridges<sup>(1,8,10)</sup> have been suggested with the emphasis on the system-level reliability rather than the element level. Also some practical approaches for reliability based safety assessment and capacity rating have been made by Cho and Ang.<sup>(2)</sup>

Various approaches to system redundancy measure have been proposed by several researchers.<sup>(5)</sup> However, no established practical approaches to the assessment of system redundancy or system

reliability are available especially for continuous, composite and multi-box steel girder bridges.

This paper develops practical reliability models and methods for the evaluation of system reliability and proposes a new method for the system reliability-based redundancy and capacity rating that incorporate the concept of non-codified equivalent system-capacity of existing bridges.

## 2. Limit State Model

### 2.1 Element Limit State Model

Since this study is concerned about the ultimate carrying-capacity of existing steel box-girder bridges, the ultimate limit state functions need to be considered in the modelling. The strength limit state models at element level for box-girder bridges suggested in the paper are based on the basic flexural strength as well as the strength interaction equations which simultaneously take into account flexure, shear and torsion.

#### 2.1.1 Bending strength limit state model

When the primary bending failure alone is considered, the linear bending strength equation becomes,

$$g(\cdot) = M_R - (M_D + M_L) \quad (1)$$

where,  $M_R$  = true moment strength;  $M_D$ ,  $M_L$  = true applied moment. The true moment strength  $M_R$  may be modelled as,

$$M_R = M_n N_M D_F \quad (2)$$

where,  $M_n$  = nominal moment strength specified in the code;  $N_M$  = the correction factor adjusting any bias and incorporating the uncertainties involved in the assessment of  $M_n$  and  $D_F$  (=MFDP),

in which, M=material strength uncertainties; F = fabrication and construction uncertainties; P=prediction and modelling uncertainties; D=the uncertainties involved in the assessment of damages and/or deterioration;  $D_F$ =damage factor= $K_D/K_I \approx \omega_D^2/\omega_I^2$ .

It may be noted that the nominal moment strength  $M_n$  specified in the code become either yield moment  $M_y$  in case of tension failure or buckling moment  $M_{cr}$  in case of compression failure.

Also, true applied moment  $M_D, M_L$  may be expressed in terms of respective random variate as follows,

$$M_D = m_D D_n N_D \quad (3a)$$

$$M_L = m_L L_n K N_L \quad (3b)$$

where,  $m_D, m_L$ =the influence coefficients of moment for dead and truck loads;  $D_n, L_n$ =the nominal dead and truck loads;  $K$ =response ratio= $K_S(1+I)$ ;  $N_D, N_L$ =correction factors(=AQ), in which,  $K_S$ =the ratio of the measured stress to the calculated stress;  $I$ =the impact factor;  $A$ =response random variables corresponding to dead or truck load;  $Q$ = random variable representing the uncertainties involved in dead or truck load.

### 2.1.2 Interactive failure limit state model

When the interaction type of combined failure limit state function needs to be considered, the interaction stress or strength failure limit in terms of bending, shear and torsion may be used in the form of the code specified interaction equation without applying the safety factors. The interaction failure criteria specified in both Korean and Japanese Standard Bridge Codes are based on the maximum distortion energy theory.<sup>(11)</sup> Thus, the nonlinear limit state function may be stated as follows,

$$g(\cdot) = 1.0 - \left[ \frac{\sigma_D + \sigma_L}{\sigma_R} \right]^2 - \left[ \frac{\tau_D + \tau_L}{\tau_R} \right]^2 \quad (4)$$

where,  $\sigma_R, \tau_R$ =true ultimate or critical bending and shear stress;  $\sigma_D, \sigma_L, \tau_D, \tau_L$ =true bending and shear stress, respectively.

Also in the similar form as Eq.2,  $\sigma_R$  and  $\tau_R$  may be given as follows,

$$\sigma_R = \sigma_n N_\sigma D_F \quad (5a)$$

$$\tau_R = \tau_n N_\tau D_F \quad (5b)$$

where,  $\sigma_n, \tau_n$ =nominal ultimate bending and shear stress specified in the code;  $N_\sigma, N_\tau$ =correction factors;  $D_F$ =damage factor.

Again,  $\sigma_D, \sigma_L, \tau_D$  and  $\tau_L$  may be expressed as,

$$\sigma_D = \underline{\sigma}_D D_n N_{D\sigma} \quad (6a)$$

$$\sigma_L = \underline{\sigma}_L L_n K N_{L\sigma} \quad (6b)$$

$$\tau_D = \underline{\tau}_D D_n N_{D\tau} \quad (6c)$$

where,  $\underline{\sigma}_D, \underline{\sigma}_L, \underline{\tau}_D, \underline{\tau}_L$ =the influence coefficients of bending and shear stress for stress for dead and truck loads;  $D_n, L_n$ =nominal dead and live loads;  $N_{D\sigma}, N_{L\sigma}, N_{D\tau}, N_{L\tau}$ ; correction factors.

## 2.2 Mechanism Failure Limit State Model

For the system reliability analysis based on the collapse mechanism of box girder bridges, the following limit state of failure mechanisms may have to be used,

$$g_i(\cdot) = \sum C_{ij} S_{Rij} - \sum (b_{Pik} S_{Dik} + b_{Lik} S_{Lik}) \quad (7)$$

where,  $S_{Rij}$ =true moment strength of  $j$ th section in  $i$ th mechanism;  $S_{Dik}, S_{Lik}$ = true applied load effects of  $k$ th loading in  $i$ th mechanism.

$C_{ij}, b_{Pik}, b_{Lik}$ =Coefficient that describe collapse mode.

In the paper, all the uncertainties of the basic random variables of resistance and load effects described above are obtained mainly from data available in the literature.<sup>(4,12)</sup>

## 3. System Reliability

### 3.1 Reliability Analysis

The structural reliability may be conceptually measured or numerically evaluated by the failure probability,  $P_F$ . However practically, relative reserve safety of a structural element or system may be best represented by the corresponding safety index  $\beta$ , i.e.,

$$\beta = -\Phi^{-1}(P_F) \quad (8)$$

where,  $P_F$ =probability of failure;  $\Phi^{-1}$ =inverse of the standard normal distribution function.

Various available numerical methods can be applied for the reliability analysis of the bridges at either element or system level using the limit state models proposed in the paper. For the evaluation of element reliability, the AFOSM algorithm<sup>(4)</sup> is used for bending limit state function, but an improved IST algorithm which is implemented as a computer code developed by the author<sup>(3)</sup> is used for the system reliability and interactive failure limit state analysis of the proposed models. As it is demonstrated in the references<sup>(7)</sup> the main advantage of using the IST may be attributed to the fact that the difficulties associated with the intractable problems such as interactive non-linear limit state functions, correlated non-normal variates and complexity or generality of reliability model do not appear to exist with the IST simulation and thus do not seem to significantly affect the convergence rate or result.

### 3.2 Practical System Reliability Assessment for Box-Girder Bridges

Obviously, the failure of a single element or member does not constitute a system failure of highly redundant bridge system such as steel box-girder bridges. As such, the collapse failure of a bridge-system is significantly different from element failures.

The realization of collapse failure state of an existing bridge may be defined as the limit state of system performance. Various descriptions for system failure or system resistance are possible based on either theoretical or practical approaches. Nowak<sup>(10)</sup> defined the system failure of girder type bridges as the attainment of either a prescribed large amount of permanent deformation or unstable singular system stiffness matrix, for which he used an incremental nonlinear analysis of grid model. However, in this study for the practical but efficient numerical solution of system reliability without involving extensive nonlinear structural analysis, it is assumed that the system failure state of box-girder bridge may be defined as the realization of collapse mechanism of major girders with or without considering the contribution of deck and cross beams. For this approach,

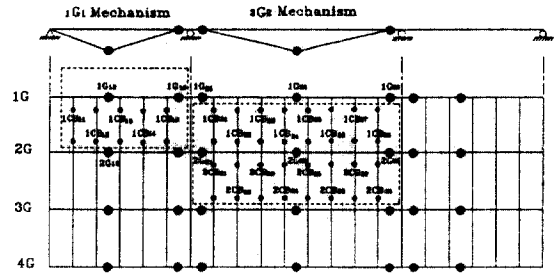


Fig. 1. collapse failure state of box-girder bridge.

an assumption is also made for the modelling of limit state such that approximate pseudo-mechanism analysis is possible by taking the critical buckling moment in compression failure zone or the yield moment in tension failure zone as the ultimate moment of box-girder section as shown in Fig.1. And thus, the system reliability problem of box-girder super-structure is formulated as parallel(mechanism)-series models obtained from the FMA based on major failure mechanisms. Fig.1 shows a typical illustrative example of some failure mechanisms of grid model for a 3-span continuous box-girder bridge. The system modelling of steel box-girder bridge can be made either by considering or neglecting the contribution of cross beams to ultimate strength of mechanisms. Also, it may be noted that at element reliability level the load effect of each girder is obtained from the linear elastic analysis of grid model for box-girder bridges.

### 3.3 Probabilistic System Redundancy and Reserve Safety

The collapse of a bridge occurs by taking multiple failure paths involving various intermediate damage or failure state after initial failure. Thus, the definition of system redundancy requires a measurement of the ultimate capacity of a bridge to resist collapse failure following the initial element failure.

Thereby, the results of system-reliability analysis in terms of system reliability index may be effectively used either as a probabilistic measure of system redundancy or reserve safety of existing bridges. So far, various approaches to the defini-

tion for the measure of the system redundancy or reserve safety have been suggested by several researchers.<sup>(6,9)</sup>

The following definitions for system redundancy and reserve safety in terms of reliability indices are adopted in the paper as a measure of system redundancy and reserve safety.<sup>(6)</sup>

$$\text{PSRF(Probabilistic System Redundancy Factor)} \\ : \text{PSRF} = \beta_s / \beta_i \quad (9a)$$

$$\text{PSReF(Probabilistic System Reserve Factor)} : \\ \text{PSReF} = \beta_s / \beta_e \quad (9b)$$

where,  $\beta_s$  = system reliability index;  $\beta_i$  = reliability index of initial-failure element;  $\beta_e$  = element reliability index.

Because, this study is primary concerned about the capacity rating of existing box-girder bridges PSReF will preferably be used in the numerical application.

#### 4. System Reliability-Based Rating

The conventional capacity rating of a bridge have been largely based on the WSR (Working Stress Rating) or LFR(Load Factor Rating) criteria which do not systematically take into any information on the repair, damage and specific to the bridge to be rated. Thus, unfortunately the nominal rating load or reserve capacity evaluated by the conventional code-specified formula, in general, fails to predict realistic carrying capacity or reserve capacity of deteriorated or damaged bridges. Recently, Moses<sup>(9)</sup> and the authors<sup>(12)</sup> have suggested reliability index to be used as a rating criterion to predict realistic relative reserve safety by incorporating actual bridge conditions and uncertainties.

For more realistic capacity rating utilizing the reserve safety of redundant bridge such as box-girder bridges, the system reliability index is suggested to be used as a  $\beta$ -rating criterion. Also, this paper propose a practical but rational approach for the evaluation of capacity-rating load  $P_n$  or rating factor(RF) in terms of the equivalent system-capacity rating load or factor, which is derived based on the concept of FOSM form of sys-

tem reliability index. For a comparative study with the codified LRFR(Load and Resistance Factor Rating) criteria previously developed by the author<sup>(12)</sup>, the LRFR rating criteria will also be given herein.

##### 4.1 Codified LRFR Criteria<sup>(2)</sup>

The following LRFR criterion may be developed corresponding to a specified target reliability index.

$$P_n = \frac{\phi' D_F R_n - \gamma_D' C_D D_n}{\gamma_L' C_L K} \quad (10)$$

$$\text{RF} = \frac{P_n}{P_r} \quad (11)$$

where,  $P_n$  = the nominal load carrying capacity;  $P_r$  = the standard design or rating load;  $\phi'$ ,  $\gamma_D'$ ,  $\gamma_L'$  = the normal resistance, dead load and live load factors, respectively.

The results of calibration for steel girder bridges corresponding to SLR(Service Load Rating,  $\beta_{e01} = 3.0$ ) and MOR(Maximum Overload Rating,  $\beta_{e02} = 2.5$ ) are shown in Table1.

Table 1. Load and resistance factor for rating of steel girder bridges

Target Rel.	$\phi'$	$\gamma_D'$	$\gamma_L'$
$\beta_{e01} = 3.0(\text{SLR})$	0.85	1.2	2.0
$\beta_{e02} = 2.5(\text{MOR})$	0.95	1.2	1.7

##### 4.2 Non-Codified System-Reliability-Based Equivalent-Capacity Rating

The system reliability index  $\beta_s$  may be conceptually expressed as the  $\ln$ - $\ln$  model of the FOSM form of 2nd moment reliability methods in the following way,

$$\beta_s \approx \frac{\ln(\bar{R}_s / \bar{Q}_s)}{\sqrt{V_{R_s}^2 + V_{Q_s}^2}} \quad (12)$$

where,  $\bar{R}_s$  = mean system resistance; and  $\bar{Q}_s$  = mean system load effects, which may be expressed in terms of nominal rating Load  $P_n$  and unit mean load effect( $Q_s = q_s P_n$ ). Therefore, it may be stated as follows ;

$$P_n = \frac{\bar{R}_s}{q_s} \text{EXP}(-\beta_s \sqrt{V_{R_s}^2 + V_{q_s}^2})$$

$$= Z_m \text{EXP}(-\beta_s \Omega_s) \quad (13)$$

where,  $Z_m$ =parameter that conceptionally represents the mean resistance safety ratio ( $\bar{R}_s/q_s$ ) ;  $\bar{Q}_s$ =parameter that conceptionally represents the system uncertainties.

As shown in Fig. 2 the relationship between  $P_n$  and  $\beta_s$  can be graphically represented by the exponential curve corresponding to Eq. 13.

Thus, the unknown parameter  $Z_m, \Omega_s$  of Eq.12 can be evaluated when the two distinct rating points( $P_{R1}, \beta_{S1}$ ) are substituted into Eq.13. Note that these are obtained as the system reliability indices  $\beta_{S1}, \beta_{S2}$  corresponding to the upper and lower standard rating load  $P_{R1}, P_{R2}$ , respectively. Thus, Eq. 13 becomes.

$$P_{R1} = Z_m \text{EXP}(-\Omega_s) \beta_{S1} \quad (14a)$$

$$P_{R2} = Z_m \text{EXP}(-\Omega_s) \beta_{S2} \quad (14b)$$

From Eq. 14a, 14b the parameters  $Z_m, \Omega_s$  can be derived as follows ;

$$Z_m = \left[ \frac{P_{R1} \beta_{S1}}{P_{R2} \beta_{S2}} \right]^{1/\Delta\beta} \quad (15)$$

$$\Omega_s = \frac{1}{\Delta\beta} \ln \left[ \frac{P_{R1}}{P_{R2}} \right] \quad (16)$$

where,  $\Delta\beta = \beta_{S1} - \beta_{S2}$

Finally, substituting Eq. 15 and 16 into Eq. 13,  $P_n$  may be derived in the following form;

$$P_n = \frac{P_{R2}^{\Delta\beta_1/\Delta\beta}}{P_{R1}^{\Delta\beta_2/\Delta\beta}} \quad (17)$$

where,  $P_n$ =nominal load carrying capacity;  $P_{R1}, P_{R2}$ =upper and lower rating loads, respectively;  $\Delta\beta_1 = \beta_{S1} - \beta_{S0}$ ;  $\Delta\beta_2 = \beta_{S2} - \beta_{S0}$ , in which,  $\beta_{S1}, \beta_{S2} = \beta_{sys}$  corresponding to  $P_{R1}, P_{R2}$ , respectively;  $\beta_{S0}$ =target reliability.

The equivalent system-rating factor proposed in the paper is a new concept which enables the bridge engineers to easily understand the reserve carrying capacity of a bridge system in terms of the maximum system-capacity rating load  $P_n$  at SLR( $\beta_{S01}=3.0$ ) or MOR( $\beta_{S02}=2.5$ ).

### 4.3 Deterministic System Redundancy and Reserve Strength

Once the ultimate system-capacity in terms of the equivalent system rating load  $P_n$  is obtained from Eq.17, the deterministic measure of system redundancy and reserve strength corresponding to those of probabilistic measure may be defined as follows,

$$\text{DSRF(Deterministic System Redundancy Factor)} : \text{DSRF} = P_{ns}/P_{ni} \quad (18a)$$

$$\text{DSReF(Deterministic System Reserve Factor)} : \text{DSReF} = P_{ns}/P_{ne} \quad (18b)$$

where,  $P_{ns}$ =nominal load of ultimate system-capacity corresponding to system reliability index ;  $P_{ne}$ =nominal load of element-capacity corresponding to element reliability index;  $P_{ni}$ =nominal load of initial-faliure capacity corresponding to reliability index of initial-failure element.

## 5. Application

### 5.1 Applicability of the System Reliability Model

At first, the applicability of the proposed models and methods for system reliability analysis is demonstrated by comparing the results for an illustrative example with those of the Nowak's approach.<sup>(10)</sup> The example bridge that Nowak used for system reliability evaluation was a 18-m composite steel girder bridge with 5W33×135 girder spaced at 2.4-m. It may be observed that at the element reliability level, two results are identical

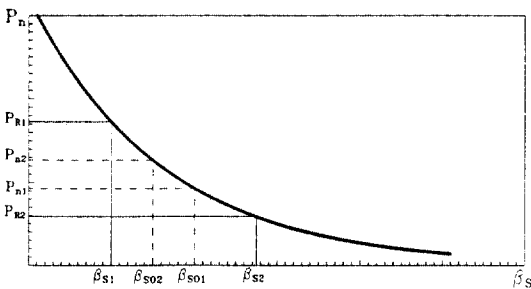


Fig. 2.  $\beta_s$  versus  $P_n$ .

Table 2. comparisons with Nowak's evaluation

Approach	$\beta_c$	$\beta_s$
Nowak	3.80	4.95 ( $\rho=1$ ) 6.20 ( $\rho=0$ )
Proposed	3.80(Ext.G) 5.23(Int.G)	5.86

as expected, but at the system level, the results of the proposed method fall between the extreme results corresponding to the Nowak's assumed correlation, which apparently indicates the appropriateness of the proposed approach. Table 2 shows the results of element and system reliabilities evaluated by two approaches.

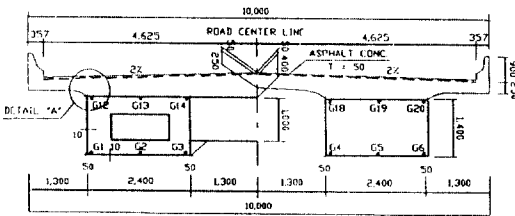


Fig. 3. Cross section of Haman bridge.

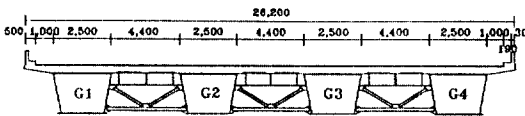


Fig. 4. Cross section of Sangil bridge.

Table 3. Bridge data

Bridge	Sang-il	Ham-an
Type	Continuous box with 3 span	Continuous box with 3 span
Span Length	30.3+45.5+30.3 = 116.12 m	29.95+35+29.91 = 95 m
Design Load	DB-24, DB-18	DB-24
Girder Space	6.9 m	5.0 m
No. of Girder	4	2
$\sigma_{test}/\sigma_{cal}$	0.4826	0.6847
Material Type	SWS 50	SWS 50
Impact Factor	1.250(1,3span) 1.211(2 span)	1.250(1,3span) 1.235(2 span)
Damage Factor	1.0	1.0

## 5.2 Example Bridges

The modelling and analysis methods for the system reliability proposed in this paper are applied to two existing steel-box girder bridges. Some of measured and analysis results with bridge data are given in Table 3.

## 5.3 System Redundancy and Reserve Safety /Strength

The results of the system redundancy measures based on the reliability assessment for the example bridges are summarized in Table 4 and 5. First of all, it can be clearly observed that considerable differences exist between the element and system reliabilities, and thus, in turn, it results in relatively high values in the measures of both probabilistic and deterministic system redundancy and residual safety/strength over the wide range of 1.3~3.0 for both bridges. These results apparently indicate that the decks, cross beams and secondary members significantly contribute to the system redundancy. Therefore, it may be argued that system reliability approaches may have to be used for the evaluation of realistic reserve safety and capacity rating of highly redundant bridges. Next, as seen in Table 4, it may be noted that the element reliability based on the interactive failure limit state are significantly lower by 10~12 % compared to those based on the bending strength limit state.

Furthermore, it can be noted in Table 5 that the effect of the number of girders on the system redundancy in the case of Sangil bridge with 4-box-girder renders a lot more significant results with(1.56~3.0) compared to those with(1.09~2.06) in the case of Haman bridge with 2-box-girder. Also, it can be seen from Table 4 that the system reliabilities based on the failure mechanism considering the effect of the cross beams are about 10~28% higher than those without considering it. Again, it may be emphasized that the cross beams significantly contribute to the collapse strength of the structure.

## 5.4 Rating of Example Bridges

The results of capacity rating of the example

Table 4. Reliability of example bridges

Bridge	Element Reliability $\beta_e(P_F)$		System Reliability $\beta_s(P_F)$		Initial-Failure Reliability $\beta_i(P_F)$
	Bending Strength Limit State	Interactive Failure Limit State	Without Cross beam Effect	With Cross beam Effect	
Sangil (4-Box)	3.11 (0.9354E-3)	2.83 (0.2327E-2)	4.86 (0.5632E-6)	6.73 (0.1023E-10)	2.38 (0.8672E-2)
Haman (2-Box)	4.78 (0.9318E-5)	4.22 (0.1222E-4)	5.20 (0.9551E-7)	5.76 (0.4129E-8)	3.93 (0.4242E-4)

bridges are summarized in Table 6. As it was shown in the reliability assessment above, it can be observed that the non-codified capacity ratings based on system reliability is a lot higher by 20~30% than Noncodified or LRFR rating based on the element reliability. It is also interesting to observe that the results of Non-codified and LRFR capacity ratings are about similar. However, it can be seen that, at element level, the conventional WSR provides unreasonably higher results than the reliability-based capacity rating, whereas the AASHTO-LFR rating gives about similar results at the element level.

Based on these comparative observations, it may be suggested that the reliability and capacity-rating evaluated at the system level are significantly different from those evaluated at the element level, especially in the case of highly redun-

Table 5. System redundancy and reserve safety/strength

Bridge		PSRF	PSReF	DSRF	DSReF
Sangil	• Without cross girder effect	2.04	1.56	2.12	1.61
	• With cross girder effect	2.83	2.16	3.01	2.03
Haman	• Without cross girder effect	1.32	1.09	1.87	1.41
	• With cross girder effect	1.47	1.21	2.06	1.61

dant box-girder bridges. Finally, it may be stated that the non-codified equivalent system-capacity formula derived on the basis of system reliabilities proposed in the paper can be successfully applied

Table 6. Capacity rating of example bridges

Basis-Capacity Rating	Method		Sangil		Haman	
			$P_n(t)$	RF	$P_n(t)$	RF
System Reliability-Based	Non-Codified	SLR	140.9	3.26	184.9	4.28
		MOR	229.4	5.31	257.3	5.95
Element Reliability-Based	Non-Codified	SLR	95.5	2.21	147.3	3.41
		MOR	142.2	3.29	182.3	4.21
	LRFR	SLR	109.2	2.53	147.1	3.41
		MOR	155.6	3.60	200.0	4.63
	WSR	MOR	150.8	3.49	194.4	4.50
	LFR(AASHTO)	LR	104.7	2.42	122.1	2.83
OR		174.5	4.04	203.5	4.71	



to assess the system-redundancy or reserved system-capacity of existing bridges in practice.

## 6. Conclusion

Because of the redundancy and effective load sharing provided by the decks and cross beams in composite steel box-girder bridges, system reliability is significantly different from element reliability. And thus it provides a more precise measure for the system safety, redundancy and capacity rating of existing steel box-girder bridges.

The equivalent system reliability-based capacity rating proposed in the paper can be effectively used in practice for the capacity rating of deteriorated or damaged bridges to pick up reserve system-safety or strength for the optimal decisions in maintenance and rehabilitation.

In the case of composite steel box-girder bridges, the interactive failure limit state provides more critical element reliability than bending strength limit state.

## 7. Acknowledgments

This research was supported by the Korea Research Foundation. The writers gratefully acknowledge this support.

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(接受 : 1993. 1. 13)