

## Thermodynamic Properties of Bismuth Trifluoride from Vapour Pressure Measurements

J. H. Kim and S. Blairs\*

Institute of Ceramic Technology, NITI  
\*School of Materials Science and Engineering  
University of New South Wales, Australia  
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### 증기압 측정으로부터 BiF<sub>3</sub>의 열역학적 계산

김준학 · S. Blairs\*

국립공업기술원 요업기술원  
\*호주 NSW대학 재료공학과  
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#### ABSTRACT

Sublimation vapour pressures and sublimation enthalpy of anhydrous bismuth trifluoride have been measured by the continuous gravimetric Knudsen-effusion method from 639.7 to 782.8 K. Additional effusion measurements have also been made from 750.6 to 863.1 K by the torsion-effusion method. Based on a correlation of  $\Delta_{\text{sub}}H^{\circ}_{298.15}$  and  $\Delta_{\text{sub}}S^{\circ}_{298.15}$ , a recommended P(T) equation has been obtained for BiF<sub>3</sub>(s);

$$\log P = -C/T + 5.2375 \log T - 3.205 \times 10^{-3} T + 4.661 \times 10^4 / T^2 + 1.348$$

where P is in Pa, T in Kelvin,  $\Delta_{\text{sub}}H^{\circ}_{298.15}$  in kJ mol<sup>-1</sup> and  $C = (\Delta_{\text{sub}}H^{\circ}_{298.15} - 13.5149) / 1.9146 \times 10^{-2}$ . Condensation coefficients and their temperature dependence have been derived from the effusion measurements.

#### 요 약

BiF<sub>3</sub>의 승화압과 엔탈피를 639.7에서 782.8 K까지 Knudsen 유출법을 사용하여 측정하였고, 또한 750.6에서 863.1 K까지 Torsion 유출법에 의해 추가 실험을 하였다. 평형 승화압도 이 안정상태 데이터로부터 구하였다.  $\Delta_{\text{sub}}H^{\circ}_{298.15}$ 와  $\Delta_{\text{sub}}S^{\circ}_{298.15}$ 의 상관관계를 이용하여, 추천할 수 있는 P(T)식을 BiF<sub>3</sub>(s)에 대해 아래의 같이 구하였다

$$\log P = -C/T + 5.2375 \log T - 3.205 \times 10^{-3} T + 4.661 \times 10^4 / T^2 + 1.348$$

여기서 P는 파스칼, T는 절대온도,  $\Delta_{\text{sub}}H^{\circ}_{298.15}$ 의 단위는 kJ mol<sup>-1</sup>이고,  $C = (\Delta_{\text{sub}}H^{\circ}_{298.15} - 13.5149) / 1.9146 \times 10^{-2}$ 이다. 응축상수와 그것의 온도의존성도 위의 두 방법에 의한 실험으로부터 유도하였다.

#### 1. Introduction

The need for accurately known thermodynamic data and structural information on metal halides is becoming increasingly important as a result of their increasing uses, especially in the field of materials, semiconductors, heat transfer media, reaction media for both

electrochemical and chemical processes and as a fuel carrier in nuclear reactors. The physico-chemical properties of an increasing number of metal halides are being examined in order to assess their suitability for these applications.

Two sets of vapour pressure are reported in the literature of BiF<sub>3</sub>. Cubicciotti<sup>1)</sup> measured the vapour

pressure using the transpiration method in the temperature ranges 756~853 K. The vapour pressure may be represented by the equation;  $\log P(\text{Pa}) = -9753/T + 9.60$ . Standard sublimation enthalpy calculated from this equation is  $186.73 \text{ kJ mol}^{-1}$ . Also, Maria and co-workers<sup>2)</sup> determined the vapour pressure values on the temperature ranges 569~838 K utilizing the Knudsen effusion-microcalorimetric technique. The data relative to the sublimation process are  $\log P(\text{Pa}) = -(9797 \pm 0.07)/T + (13.915 \pm 0.09)$  and sublimation enthalpy  $(201.154 \pm 0.975) \text{ kJ mol}^{-1}$ . The present study has been undertaken to re-examine the sublimation vapour pressures and enthalpy for  $\text{BiF}_3$  using the continuous gravimetric Knudsen and torsion effusion techniques.

## 2. Experimental and Results

Samples of anhydrous  $\text{BiF}_3$  by Johnson Matthey Ltd. of Puratronic grade (10 p.p.m. total metal impurities) were vaporized in this study. Effusion cells, based essentially on a design by Blairs et al.<sup>3)</sup> and fabricated with type-304 stainless steel, were filled inside a nitrogen dry box (moisture level  $\leq 20$  v.p.m.). A series of interchangeable push-fit effusion cell lids, each carrying an orifice of different size and having right-circular cylindrical geometry were used in the measurements.

Effusion orifice parameters, orifice Clausing Factors<sup>5)</sup>  $W_B$  and recoil force factors<sup>1)</sup>  $f$  used in the gravimetric and torsion effusion measurements were reported in the previous papers<sup>6,7)</sup>. And the base of both methods and experimental apparatus was also described.

### 2.1. Gravimetric Knudsen Effusion

Gravimetric Knudsen effusion system was made via a port in the dry box wall, to attach loaded gravimetric effusion cells directly to a calibrated Ni-Span-C 902 spring balance ( $11.222 \pm 0.012 \text{ cm g}^{-1}$ ) inside the effusion apparatus. Spring contractions during effusion runs were measured by cathetometer ( $\pm 0.001 \text{ cm}$ ). Steady-state effusion rates at each temperature,  $W$  ( $\text{mg h}^{-1}$ ), were derived from linear least squares plots of spring contraction vs. time data. Effusion cells were maintained in a fixed position in the constant zone ( $\pm 0.5 \text{ K}$ ) of laboratory tube furnaces. Dynamic vacua better than  $1.33 \times 10^{-5} \text{ Pa}$  were maintained during effusion runs. Effusion cell temperatures ( $\pm 0.25 \text{ K}$ ) were

measured with calibrated NiCr/NiAl thermocouples with their hot junctions located in close proximity to the effusion cells.

Steady-state Knudsen effusion vapour pressures for solid  $\text{BiF}_3$  in the range 639.7 to 782.8 K are reported in Table 1 and are plotted in Fig. 1 for five different effective orifice areas.

### 2.2. Torsion Effusion

Moment arms of the torsion effusion cells were measured by cathetometer as  $(0.843 \pm 0.001) \text{ cm}$ . A null point torsion effusion apparatus employing a geared stepper motor and electronic driver was also used to measure vapour pressures. Each stepper motor pulse corresponded to a torsion angle of  $0.05^\circ$  and a deflection of  $(2.88 \pm 0.09) \text{ mm}$  was measured using an optical lever and a He-Ne laser. The torsion constant  $k$ ,  $(2.1504 \pm 0.1486) \times 10^{-7} \text{ N m}^{-1} \text{ rad}^{-1}$ , of a 0.005 cm diameter tungsten wire was determined from changes of oscillation period after addition of inertia masses of known moments of inertia. A laser switch and interfaced computer were used as a precision timer ( $\pm 0.0001 \text{ s}$ ). The design of the torsion effusion apparatus precluded direct mounting of loaded effusion cells from the dry box. Instead, a procedure suggested by McCreary and Thorn<sup>8)</sup> was used. Orifices of matched pairs of torsion cells were sealed with drops of naphthalene inside the dry box. On solidification, naphthalene sealed the orifices and protected the halide from hydrolysis during transfer to the torsion effusion apparatus. On evacuation, naphthalene was sublimed clearly from the orifices.

Steady-state torsion effusion vapour pressures, measured in the range from 750.6 to 853.9 K are reported in Table 2 and are plotted in Fig. 2 for four different orifice areas.  $P(T)$  equations derived by least squares treatment of the steady-state vapour pressures for each orifice size are summarized in Table 3.

## 3. Discussion

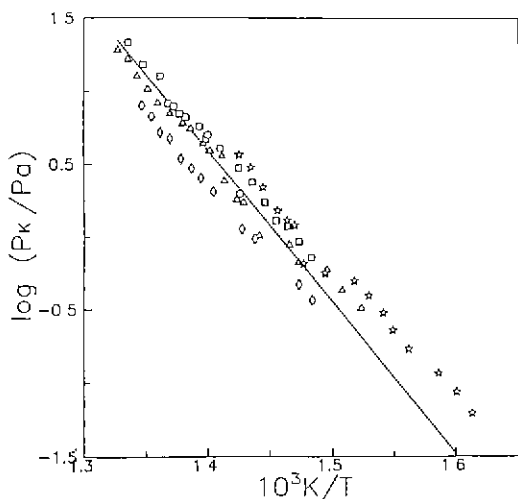
Steady-state vapour pressures from both effusion techniques were found to be dependent on effective orifice area  $aW_B$ . Isothermal plots of inverse steady-state vapour pressure versus effective orifice were linear and were extrapolated to obtain inverse values

**Table 1.** Steady-State Vapour pressure  $P_K$ (Pa) and Third-Law Standard Molar Enthalpy  $\Delta_{\text{sub}}H_{298.15}^{\circ}$  for  $\text{BiF}_3(\text{s})$  Determined by Knudsen Effusion Method.  $W$ =Steady-State Effusion Rate ( $\text{mg h}^{-1}$ ). ( $p^{\circ}=101325$  Pa)

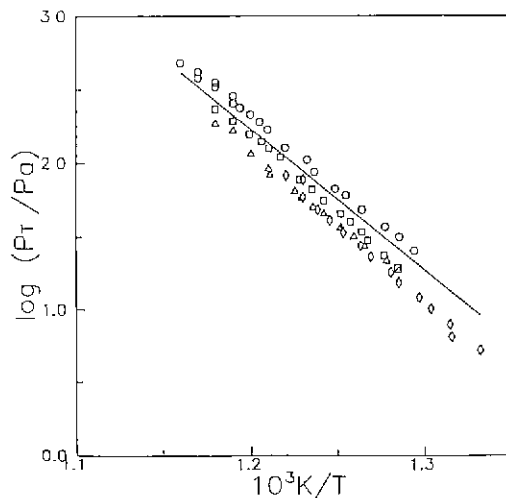
Orifice No.	T (K)	W ( $\text{mg h}^{-1}$ )	$P_K$ (Pa)	$\Delta_{\text{sub}}H_{298.15}^{\circ}$ ( $\text{kJ mol}^{-1}$ )	Orifice No.	T (K)	W ( $\text{mg h}^{-1}$ )	$P_K$ (Pa)	$\Delta_{\text{sub}}H_{298.15}^{\circ}$ ( $\text{kJ mol}^{-1}$ )
1	727.1	0.38789	1.986077	206.75		763.7	11.74270	8.515606	207.28
	740.9	0.98218	5.034546	204.72		768.4	14.47802	10.559272	207.13
	744.6	1.12537	5.770165	204.85		773.4	17.69713	12.910604	207.07
	750.8	1.30090	6.673144	205.53		777.9	23.00292	16.827441	206.47
	756.3	1.54867	7.947186	205.86		782.8	26.47201	19.423641	206.77
2	697.9	0.45059	0.723620	204.75	4	697.4	1.24074	0.368996	208.53
	702.9	0.58012	0.934790	204.64		702.6	1.59061	0.474721	208.54
	707.4	0.73345	1.185462	204.49		720.8	3.23944	0.978653	209.32
	712.1	0.79890	1.295350	205.26		726.3	3.76600	1.141839	209.89
	716.6	1.06781	1.736550	204.74		738.5	6.73064	2.056924	209.61
	721.8	1.46963	2.398256	204.20		743.9	8.34514	2.559109	209.69
	727.5	1.82581	2.990607	204.38		748.0	9.70393	2.983594	209.83
	735.5	2.47785	4.079891	204.61		752.9	11.21188	3.457969	210.20
	741.7	2.85146	4.713639	205.33		758.0	15.38311	4.759635	209.52
	753.5	4.21052	7.012703	205.92		762.6	16.89314	5.241822	210.10
	758.9	4.97595	8.315849	206.23		766.6	21.71819	6.755617	209.50
	762.7	7.60108	12.732978	204.49		771.1	25.69587	8.014967	209.54
	770.5	9.03042	15.200508	205.31		5	639.7	0.44294	0.062608
777.9	12.67227	21.426556	204.91	644.8	0.61952		0.087899	201.16	
3	678.7	0.48253	0.330853	203.81	650.9	0.83190	0.118564	201.39	
	686.1	0.63727	0.439191	204.30	661.5	1.20558	0.173146	202.43	
	692.0	0.88029	0.609163	204.10	667.1	1.60641	0.231648	202.45	
	702.9	0.97998	0.683210	206.47	670.6	2.11399	0.305602	201.93	
	706.6	1.29154	0.902726	205.89	676.0	2.75463	0.399754	201.98	
	719.0	1.47715	1.040954	208.43	681.4	3.47139	0.505692	202.19	
	725.6	2.47540	1.752056	207.11	692.6	3.86998	0.568140	204.67	
	728.4	2.59424	1.839582	207.58	700.9	4.48111	0.661626	206.13	
	733.6	3.50388	2.493035	207.12	704.5	8.18894	1.212007	203.58	
	734.6	5.17743	3.686030	204.99	707.6	8.80454	1.305826	203.98	
	740.0	5.57624	3.983885	205.94	711.4	10.30583	1.532367	204.07	
	742.9	6.25934	4.480058	205.95	717.4	14.86780	2.219537	203.49	
	748.5	7.87253	5.655081	205.98	722.5	20.30099	3.040790	202.95	
	752.1	8.51496	6.130295	206.39	727.3	24.71903	3.714281	203.02	
	758.0	9.94658	7.187622	206.91					

of the equilibrium vapour pressures for zero effective orifice area. From the equilibrium sublimation pressures, the following  $P(T)$  equations were obtained from the Knudsen and torsion effusion measurements respectively:  $\log P_h(\text{Pa}) = -(10121 \pm 75)/T + (14.244 \pm 0.097)$  and  $\log P_T(\text{Pa}) = -(9625 \pm 80)/T + (13.816 \pm 0.099)$ .

These equilibrium  $P(T)$  equations are shown with experimental points on Figs. 1 and 2 and with literature vapour pressures<sup>1,2)</sup> for comparison in Fig. 3. Extrapolated Knudsen effusion equilibrium vapour pressures are in good agreement with those reported in references 1 and 2.



**Fig. 1.** Steady-state vapour pressures for  $\text{BiF}_3(\text{s})$  measured by Knudsen effusion method.  
 ○, orifice 1; □, orifice 2; △, orifice 3; ◆, orifice 4; ★, orifice 5; —, equilibrium line.



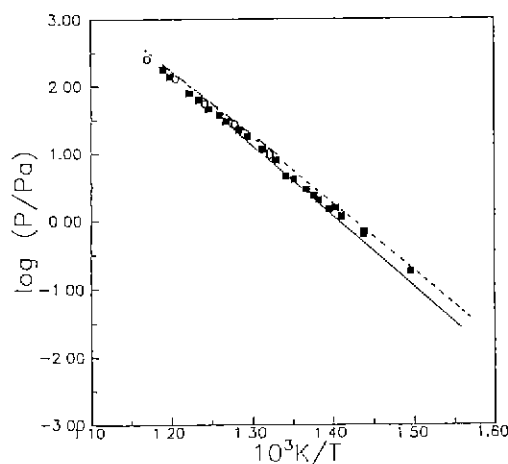
**Fig. 2.** Steady-state vapour pressures for  $\text{BiF}_3(\text{s})$  measured by torsion effusion method.  
 ○, orifice 1; □, orifice 2; △, orifice 3; ◆, orifice 4; —, equilibrium line.

From literature value for  $\text{BiF}_3(\text{s})$  vapour pressures, equations of form  $\log P(\text{Pa}) = -A/T + B$  were derived and the coefficients  $A$  and  $B$  are given in Table 4. Second-law values of  $\Delta_{\text{sub}}H_{298}^\circ$  and  $\Delta_{\text{sub}}S_{298}^\circ$  also given in Table 6 were calculated by assuming the coefficients  $A$  and  $B$  apply at the mean temperatures of the various ranges together with the following  $C_p(T)$  for  $\text{BiF}_3(\text{s})$  and  $\text{BiF}_3(\text{g})$ . Polynomial expressions<sup>1)</sup>  $C_p^\circ (\text{J mol}^{-1} \text{K}^{-1}) = 38.97 + 123.17 \times 10^{-3}T + 8.95 \times 10^5 T^{-2}$  and  $C_p^\circ (\text{J mol}^{-1} \text{K}^{-1}) = 82.51 + 0.46 \times 10^{-3}T - 8.90 \times 10^5 T^{-2}$ , for  $\text{BiF}_3(\text{s})$  and  $\text{BiF}_3(\text{g})$  respectively were employed in this research.

All the structural and spectroscopic quantities used in the thermodynamic calculations are presented in Table 5. Thermodynamic functions  $\Delta[(G^\circ_T - H_{298.15}^\circ)/T]$  for  $\text{BiF}_3(\text{g})$  were computed for a rigid-rotator harmonic-oscillator ideal gas monomer and pyramidal  $C_{3v}$  symmetry.

Thermodynamic functions  $\Delta[(G^\circ_T - H_{298.15}^\circ)/T]$  and  $S_{298.15}^\circ$  for  $\text{BiF}_3(\text{s})$  were derived from  $\Delta_{\text{sub}}S_{298.15}^\circ = (194.97 \pm 3.35) \text{ J mol}^{-1} \text{K}^{-1}$ , and  $S_{298.15}^\circ = 317.65 \text{ J mol}^{-1} \text{K}^{-1}$  for  $\text{BiF}_3(\text{g})$  computed as outlined above and  $C_p^\circ (\text{J mol}^{-1} \text{K}^{-1}) = 38.97 + 123.17 \times 10^{-3}T + 8.95 \times 10^5 T^{-2}$  for  $\text{BiF}_3(\text{s})$ <sup>1)</sup>. Thermodynamic functions for  $\text{BiF}_3(\text{s})$  at selected temperatures are presented in Table 5.

Third-law  $\Delta_{\text{sub}}H_{298.15}^\circ$  at each effusion temperature



**Fig. 3.** Comparison of  $\text{BiF}_3$  vapour pressures.  
 ○, Cubicciotti<sup>1)</sup>; ■, Maria and co-workers<sup>2)</sup>; —, Knudsen effusion equilibrium line; ---, torsion effusion equilibrium line; ···, recommended  $P(T)$

are also reported in Tables 1 and 2 and shown in Fig. 4 for both effusion techniques. Individual  $\Delta_{\text{sub}}H_{298}^\circ$  values obtained using effusion methods are independent of temperature and effective orifice area.

The average third-law  $\Delta_{\text{sub}}H_{298.15}^\circ$ ,  $(206.38 \pm 0.014) \text{ kJ mol}^{-1}$ , shown in Fig. 4 together with its standard

**Table 2.** Steady-State Vapour Pressure  $P_1$ (Pa) and Third-Law Standard Molar Sublimation Enthalpy  $\Delta_{\text{sub}}H_{298.15}^\circ$  for  $\text{BiF}_3(\text{s})$  Determined by Torsion Effusion Method

Cell No.	T (K)	PT (Pa)	$\Delta_{\text{sub}}H_{298.15}^\circ$ (kJ mol <sup>-1</sup> )	Cell No.	T (K)	PT (Pa)	$\Delta_{\text{sub}}H_{298.15}^\circ$ (kJ mol <sup>-1</sup> )
1	772.8	25.547808	202.54		822.0	110.581863	204.44
	778.0	31.741234	202.40		826.4	127.038094	204.48
	782.9	37.181644	202.56		829.3	141.520020	204.40
	791.2	48.435085	202.79		833.8	158.098022	204.66
	796.9	60.625656	202.68		3	778.2	19.103920
	800.8	67.373726	202.88	782.3		22.163235	205.79
	808.7	87.806023	202.95	790.3		27.769369	206.24
	811.6	105.806931	202.36	794.2		32.283962	206.18
	820.1	128.469254	202.97	798.8		37.233524	206.36
	826.8	170.815033	202.55	805.0		46.258907	206.37
	830.0	192.919205	202.42	809.1		51.132515	206.67
	833.5	216.516373	202.39	813.8		58.916679	206.82
	837.6	239.540009	202.60	816.2		65.829697	206.64
	839.8	259.387939	202.54	826.0		84.734634	207.17
	843.2	286.717682	202.59	4	750.6	5.295873	206.93
848.3	329.199188	202.73	760.2		6.600476	208.01	
851.2	358.017639	202.76	760.7		7.975427	206.95	
853.9	381.401154	202.89	767.2		10.276388	206.97	
2	778.5	19.535908	205.66		771.2	12.268122	206.84
	783.3	23.887911	205.54		778.1	15.529016	207.06
	789.0	30.084953	205.42		780.9	18.241421	206.70
	791.2	34.172871	205.11	788.0	23.319967	206.83	
	795.3	40.104599	205.03	791.6	27.540911	206.62	
	798.8	45.376152	205.03	797.8	33.852264	206.76	
	805.0	55.784843	205.13	802.8	41.055187	206.66	
	809.6	66.588478	205.01	807.4	48.496510	206.63	
	814.4	77.783432	205.09				

**Table 3.** Coefficients with Standard Deviations of the Equation  $\log P(\text{Pa}) = -A/T + B$  Derived from  $\text{BiF}_3$  Steady-State Knudsen and Torsion Effusion Vapour Pressure Measurements Determined in the Temperature Range  $T_1$  to  $T_2$ 

Method	Orifice No.	$T_1$	$T_2$	Number of Points	A	B
Knudsen	1	727.1	756.3	5	11301 ± 1528	15.891 ± 2.054
	2	697.9	777.9	14	9684 ± 219	13.752 ± 0.298
	3	678.7	782.8	20	9243 ± 286	13.057 ± 0.568
	4	697.4	771.1	12	9683 ± 171	13.433 ± 0.340
	5	639.7	727.3	16	8911 ± 318	12.735 ± 0.464
Torsion	1	772.8	853.9	18	9765 ± 120	14.038 ± 0.149
	2	778.5	833.8	13	10740 ± 116	15.095 ± 0.144
	3	778.2	826.0	10	8784 ± 98	12.569 ± 0.123
	4	750.6	807.4	12	10540 ± 219	14.743 ± 0.281

**Table 4.** Summary of BiF<sub>3</sub>(s) Vapour Pressures

T (K)	A      B		2nd law		3rd law
			$\Delta_{\text{sub}}H^{\circ}_{298.15}$ (kJ mol <sup>-1</sup> )	$\Delta_{\text{sub}}S^{\circ}_{298.15}$ (J mol <sup>-1</sup> K <sup>-1</sup> )	$\Delta_{\text{sub}}H^{\circ}_{298.15}$ (kJ mol <sup>-1</sup> )
756.4-853.1 <sup>(b)</sup>	9657 ± 155	13.731 ± 0.193	193.194 ± 2.968	194.452 ± 3.695	205.28 ± 0.411
669 -838 <sup>(b),(c)</sup>	9845 ± 104	13.979 ± 0.137	193.957 ± 0.858	195.133 ± 2.67	204.89 ± 0.649
639.7-782.8 <sup>(a)</sup>	10121 ± 75	14.244 ± 0.097	200.598 ± 1.436	202.178 ± 0.019	206.38 ± 0.014
750.6-837.6 <sup>(b)</sup>	9625 ± 80	13.816 ± 0.099	192.870 ± 1.532	196.476 ± 0.019	206.28 ± 0.035

<sup>a</sup>Gravimetric Knudsen-effusion method, <sup>b</sup>Torsion-effusion method, <sup>c</sup>Knudsen effusion-Microcalorimetric method.

**Table 5.** Standard Molar Thermodynamic Functions for BiF<sub>3</sub>(s) and BiF<sub>3</sub>(g) at Selected Temperatures. v/cm<sup>-1</sup>, 505, 203, 425, 175; Geometric Constants:<sup>1)</sup> r(Bi-F)=0.236 nm; r(Bi-Bi)=0.285 nm; ∠F-Bi-F=100° (R=8.31451 J mol<sup>-1</sup> K<sup>-1</sup>; p<sup>o</sup>=101325 Pa; T<sup>o</sup>=298.15 K)

T (K)	C <sub>p</sub> <sup>o</sup> (J mol <sup>-1</sup> K <sup>-1</sup> )	(H <sub>T</sub> <sup>o</sup> -H <sub>298.15</sub> <sup>o</sup> ) (kJ mol <sup>-1</sup> )	Δ(S <sub>T</sub> <sup>o</sup> -S <sub>298.15</sub> <sup>o</sup> ) (J mol <sup>-1</sup> K <sup>-1</sup> )	-Δ[(G <sub>T</sub> <sup>o</sup> -H <sub>298.15</sub> <sup>o</sup> )/T] (J mol <sup>-1</sup> K <sup>-1</sup> )
solid <sup>d</sup>				
298.15	85.817	0	0	122.591
300	85.865	0.772	0.531	120.548
400	93.829	9.112	26.234	126.045
500	104.131	18.999	48.253	132.846
600	115.354	29.968	68.221	140.865
700	127.011	42.084	86.874	149.345
gas				
298.15	73.644	0	0	322.548
300	73.740	0.136	0.456	322.550
400	77.440	7.714	22.232	325.494
500	79.316	15.560	39.730	331.159
600	80.427	23.552	54.298	337.594
700	81.120	31.631	66.752	344.112
800	81.580	39.768	77.616	350.454
900	81.901	47.943	87.244	356.522

<sup>d</sup>Derived using C<sub>p</sub><sup>o</sup> and Δ<sub>sub</sub>S<sub>298</sub><sup>o</sup> for BiF<sub>3</sub>(s) from reference 1 and S<sub>298</sub><sup>o</sup>(g) calculated in this work<sup>(2)</sup>.

deviation, is based only on the Knudsen-effusion data and is comparable with Δ<sub>sub</sub>H<sub>298.15</sub><sup>o</sup>=201.3 kJ mol<sup>-1</sup> derived later from an enthalpy-entropy correlation. Average third-law Δ<sub>sub</sub>H<sub>298.15</sub><sup>o</sup> values derived from literature vapour pressures are also included in Table 4.

Uncertainty of temperature to which the coefficients A and B summarized in Table 4 are valid may be avoided by use of the modified sigma function method<sup>(10)</sup>.

Δ<sub>sub</sub>H<sub>298.15</sub><sup>o</sup> and Δ<sub>sub</sub>S<sub>298.15</sub><sup>o</sup> values were derived from the least squares slopes and intercepts of modified sigma function plots of the literature BiF<sub>3</sub> vapour pressure data sets<sup>(12)</sup> as well as the present measurements. For these calculations, in addition to the free energy functions of gaseous and solid BiF<sub>3</sub> reported in Table 5, a value of C<sub>p</sub><sup>o</sup>=44.0 J mol<sup>-1</sup> K<sup>-1</sup>, and a molar enthalpy of fusion of (909.18±12.55) kJ mol<sup>-1</sup>, were used

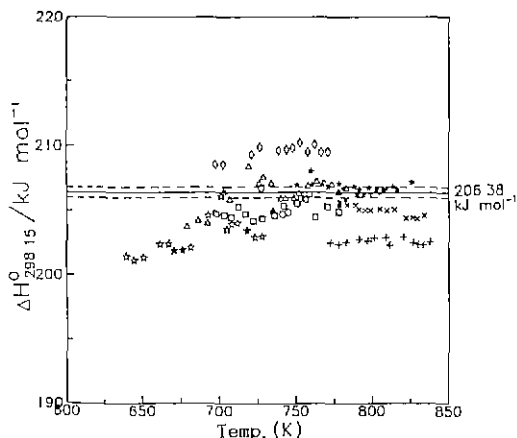


Fig. 4. Enthalpy of sublimation at 298.15 K of  $\text{BiF}_3(\text{s})$  determined in this research.

Knudsen effusion: ○, orifice 1; □, orifice 2; △, orifice 3; ◆, orifice 4; ★, orifice 5.  
Torsion effusion: \*, orifice 1; +, orifice 2; ×, orifice 3; ★, orifice 4.

to obtain thermal functions for liquid  $\text{BiF}_3$ . The resulting  $\Delta_{\text{sub}}H_{298.15}^{\circ}$  and  $\Delta_{\text{sub}}S_{298.15}^{\circ}$  are summarized in Table 6 and have been plotted as  $\Delta_{\text{sub}}H_{298.15}^{\circ}$  vs.  $\Delta_{\text{sub}}S_{298.15}^{\circ}$  in Fig. 5. The values are linearly correlated by the least-squares equation  $\Delta_{\text{sub}}H_{298.15}^{\circ} = (20.1648 \pm 6.3924) + (0.9282 \pm 0.0320)\Delta_{\text{sub}}S_{298.15}^{\circ}$ , (correlation coefficient = 0.999) where  $\Delta_{\text{sub}}H_{298.15}^{\circ}$  is in  $\text{kJ mol}^{-1}$  and  $\Delta_{\text{sub}}S_{298.15}^{\circ}$  is in  $\text{J mol}^{-1}\text{K}^{-1}$ .

Previous studies have indicated that values of  $\Delta_{\text{sub}}H_{298.15}^{\circ}$  and  $\Delta_{\text{sub}}S_{298.15}^{\circ}$  generated from sets of  $\log P(\text{Pa})$  versus  $T^{-1}$  are frequently linearly correlated. McCrery and Thorn<sup>11)</sup> suggest an explanation for this type of correlation in that the error or errors inadvertently encountered in vapour pressure determinations, are systematic in the plot of  $\Delta_{\text{sub}}H_{\text{T}}^{\circ}$  versus  $\Delta_{\text{sub}}S_{\text{T}}^{\circ}$  rather than random. Thus one can define a procedure whereby the apparent precision of the third-law procedure is retained but inconsistencies are removed by using information available in the analysis of  $\log P(\text{Pa})$  versus  $T^{-1}$ . For  $\text{BiF}_3$ , Pankratz<sup>12)</sup> reports an assessed  $\Delta_{\text{sub}}S_{298.15}^{\circ}$  of  $195.1 \text{ J mol}^{-1}\text{K}^{-1}$ . The corresponding  $\Delta_{\text{sub}}H_{298.15}^{\circ}$  from the linear correlation of  $\Delta_{\text{sub}}H_{298.15}^{\circ}$  and  $\Delta_{\text{sub}}S_{298.15}^{\circ}$  is  $201.3 \text{ kJ mol}^{-1}$  as shown in Fig. 5. The third-law  $\Delta_{\text{sub}}H_{298.15}^{\circ}$  obtained from the enthalpy-entropy correlation has been used to derive a sublimation pressure equation which is consistent with the thermal

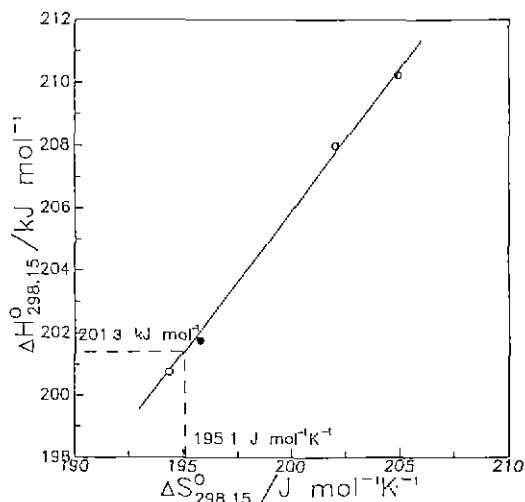


Fig. 5. Correlation of molar enthalpy and entropy of sublimation at 298.15 K for  $\text{BiF}_3(\text{s})$ .  
○, Cubicciotti<sup>1)</sup>; ●, Maria and co-workers<sup>2)</sup>; ◐, This study, Knudsen effusion; ◑, This study, torsion effusion.

Table 6.  $\Delta_{\text{sub}}H_{298.15}^{\circ}$  and  $\Delta_{\text{sub}}S_{298.15}^{\circ}$  for  $\text{BiF}_3(\text{s})$  Derived from The Modified Sigma Function Method<sup>11)</sup>

$\Delta_{\text{sub}}H_{298.15}^{\circ}$ ( $\text{kJ mol}^{-1}$ )	$\Delta_{\text{sub}}S_{298.15}^{\circ}$ ( $\text{J mol}^{-1}\text{K}^{-1}$ )
$200750 \pm 2994^a$	$194.398 \pm 3.730^a$
$201728 \pm 2087^b$	$195.867 \pm 2.762^b$
$208000 \pm 121^c$	$202.110 \pm 0.156^c$
$210218 \pm 219^d$	$204.903 \pm 0.272^d$

<sup>a</sup>from reference 1; <sup>b</sup>from reference 2; <sup>c</sup>This study, Knudsen effusion; <sup>d</sup>This study, torsion effusion.

data. The resulting  $P(T)$  equation recommended for the vapour pressure of  $\text{BiF}_3$  is:  $\log P = -C/T + 5.2375 \log T - 3.205 \times 10^{-3}T + 4.661 \times 10^4/T^2 + 1.348$  with,  $C = (\Delta_{\text{sub}}H_{298.15}^{\circ} - 13.5149)/1.9146 \times 10^{-2}$ . In this equation  $p$  is in Pa,  $T$  in Kelvin and  $\Delta_{\text{sub}}H_{298.15}^{\circ}$  in  $\text{kJ mol}^{-1}$ . This equation was used to compute the recommended line for  $\text{BiF}_3(\text{s})$  shown on Fig. 3.

Condensation coefficients  $\alpha_c$  were obtained from the slopes and intercepts of isothermal linear plots of inverse steady-state vapour pressure and effective orifice area. From the slopes and intercepts of semi-logarithmic plots of  $\log \alpha_c$  vs.  $T^{-1}$  (Fig. 6), an apparent activation sublimation enthalpy  $\Delta_{\text{cond}}H_{780}^* = -129.52 \text{ kJ mol}^{-1}$

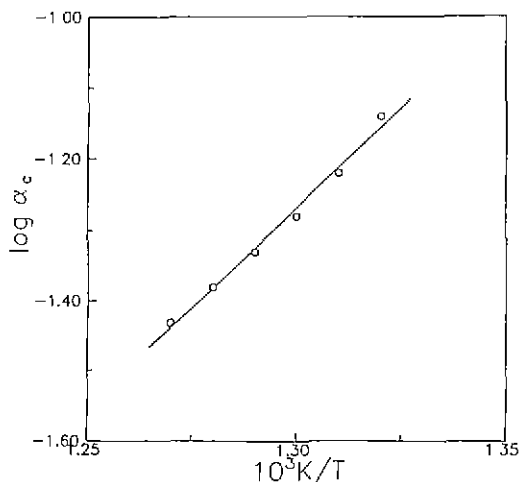


Fig. 6.  $\log \alpha_c$  versus  $1/T$  (Gravimetric Knudsen method).

and entropy  $\Delta_{\text{cond}}S^*_{780} = -192.50 \text{ J mol}^{-1} \text{ K}^{-1}$  for condensation were obtained from the gravimetric effusion measurements. Corresponding values for vaporisation (relative to the solid) were  $\Delta_{\text{vap}}H^*_{780} = 58.13 \text{ kJ mol}^{-1}$  and  $\Delta_{\text{vap}}S^*_{780} = -84.40 \text{ J mol}^{-1} \text{ K}^{-1}$  at 780 K. It is to be recognized that values of  $\alpha_c$  given in Table 7 were obtained by assignment of the cross-sectional area ( $71.57 \text{ mm}^2$ ) of the effusion cell body as the effective area of the vaporising and condensing surface. The actual effective area may well be larger and hence  $\alpha_c$  may actually be smaller. Apparent values of  $\alpha_c$  and their temperature dependence are characteristic only of effusion systems where steady-state vapour pressures are independent of sample size. Under these conditions, extrapolation of steady-state pressures to obtain equilibrium values appears quite satisfactory.

#### 4. Conclusion

Sublimation pressures above anhydrous bismuth trifluoride have measured using the gravimetric Knudsen and torsion effusion methods. Steady state effusion pressures were found to depend on the effective orifice area of the effusion cells. Equilibrium sublimation pressures obtained from the steady state data have been assessed in the context of literature values.

Condensation coefficients and their temperature dependence have been derived from the steady state su-

Table 7. Equilibrium Vapour Pressures and Condensation Coefficients for  $\text{BiF}_3(\text{s})$  at Selected Temperatures Derived From Plots of Inverse Steady-State Vapour Pressure and Effective Orifice Area.  $\log P(\text{Pa}) = -A/T + B$  and  $aW_B$  for This Purpose Are Obtained from Tables 3 and 4 Respectively

Knudsen-method			Torsion-method		
T (K)	$P_R$ (Pa)	$\alpha_c \times 10^2$	T (K)	$P_T$ (Pa)	$\alpha_c \times 10^2$
760	8.434	7.227	795	51.028	2.429
765	10.314	6.080	800	60.661	2.500
770	12.577	5.252	805	71.943	2.570
775	15.295	4.627	810	85.068	2.645
780	18.550	4.137	815	100.505	2.722
785	22.439	3.744	820	118.398	2.801

blimation pressures and hence activation enthalpy and entropy changes for the vaporisation and condensation of bismuth trifluoride have been obtained. Standard sublimation enthalpy changes,  $\Delta_{\text{sub}}H^{\circ}_{298.15}$ , have been derived by both Second and Third Law methods, i.e., modified Sigma function and averaged enthalpy methods respectively. Standard sublimation entropy changes,  $\Delta_{\text{sub}}S^{\circ}_{298.15}$ , have also been derived by the modified function method.

The role of the correlation between  $\Delta_{\text{sub}}H^{\circ}_{298.15}$  and  $\Delta_{\text{sub}}S^{\circ}_{298.15}$ , systematic errors between sets of  $\log P$  vs.  $T^{-1}$  in vapour and sublimation pressure determinations has also been examined. A linear correlation has been demonstrated whereby the separation of systematic errors is indicated. This procedure recognizes and removes systematic errors in standard sublimation enthalpy changes derived from the slopes of  $\log P$  vs.  $T^{-1}$  and defines a criterion whereby reliable standard sublimation enthalpy changes may be obtained. Using this approach, recommended  $P(T)$  equations for the sublimation pressures of anhydrous bismuth trifluoride have been derived.

#### NOMENCLATURE

$\Delta_{\text{sub}}H^{\circ}_{298.15}$ : standard sublimation enthalpy changes,  $\text{kJ mol}^{-1}$

$\Delta_{\text{sub}}S^{\circ}_{298.15}$ : standard sublimation entropy changes,  $\text{J mol}^{-1} \text{ K}^{-1}$



- $\Delta_{\text{cond}}H^*_T$  : apparent activation enthalpy changes for condensation,  $\text{kJ mol}^{-1}$
- $\Delta_{\text{cond}}S^*_T$  : apparent activation entropy changes for condensation,  $\text{J mol}^{-1} \text{K}^{-1}$
- $\Delta_{\text{vap}}H^*_T$  : apparent activation enthalpy changes for vaporisation,  $\text{kJ mol}^{-1}$
- $\Delta_{\text{vap}}S^*_T$  : apparent activation entropy changes for vaporisation,  $\text{J mol}^{-1} \text{K}^{-1}$
- $\Delta[(G^\circ_T - H^\circ_{298.15})/T]$  : free energy functions,  $\text{J mol}^{-1} \text{K}^{-1}$
- $W_D$  : Clausius factors
- $f$  : recoil force factors
- $k$  : torsion constant,  $\text{N m}^{-1} \text{rad}^{-1}$
- $C_p^\circ$  : heat capacity,  $\text{J mol}^{-1} \text{K}^{-1}$
- $\nu$  : fundamental frequency,  $\text{cm}^{-1}$
- $r$  : bond distance, nm
- $R$  : gas constant,  $\text{J mol}^{-1} \text{K}^{-1}$
- $\log$  : natural logarithm
- $\alpha_c$  : condensation coefficients

REFERENCES

1. D. Cubicciotti, "The Thermodynamic Properties of Bismuth Trifluoride," *J. Electrochem. Soc.*, **115**, 1138-1143 (1968).
2. G. De Maria, L. Malaspina, G. Bardi and R. Gigli, "Simultaneous Determination by Knudsen Effusion-Microcalorimetric Technique of the Vapour Pressure and Sublimation Enthalpy of Antimony Trifluoride. Vapour Pressure of Bismuth Trifluoride," *Revue Roumaine de* **18**(3), 367-375 (1973).

3. S. Blairs, A.J. Shelton and R. Unsworth, "Metal Cell for Use in Vapour Pressure Measurements by Effusion Method," *J. Sci. Instrum.*, **38**, 469-470 (1961).
4. W.C. DeMarcus, "The Problem of Knudsen Flow, Part 3. Solutions for One-Dimensional System," U.S. At. Energy Comm. K-1302, 1957.
5. R.D. Freeman and J.G. Edwards, "The Characterization of High Temperature Vapors, J.L. Margrave, Ed., Wiley, New York. Appendix C.1967.
6. J.H. Kim, "The Sublimation Pressure and Standard Enthalpy of Sublimation of Bismuth Triiodide," *J. Kor. Ceram. Soc.*, **27**(7), 943-951 (1990).
7. J.H. Kim, "Sublimation Pressure and Standard Enthalpy of Sublimation of Bismuth Triiodide by Torsion-Effusion Method," *J. Kor. Ceram. Soc.*, **28**(2), 109-118 (1991).
8. J.R. McCreary and R.J. Thorn, "Heat and Entropy of Sublimation of Nickel Dichloride, Dibromide and Diiodide; Dissociation Energies of Gaseous  $\text{NiCl}_2$ , and  $\text{NiBr}_2$ ," *J. Chem. Phys.*, **48**, 3290-3297 (1967).
9. R.P. Beyer, "A Computer Program for Calculating Thermodynamic Properties Spectroscopic Data," U.S. Bureau of Mines, Information Circular 871, 1982.
10. D. Cubicciotti, "A New-plot Treatment of Equilibrium Data and Its Application to the Vaporization of Bismuth Chloride," *J. Phys. Chem.*, **70**, 2410-2413 (1966).
11. J.R. McCreary and R.J. Thorn, "Enthalpy Sublimation of Zinc and Cadmium; Correlation of  $\Delta H^\circ$  vs  $\Delta S^\circ$ ; Comparison of Torsional and Knudsen Vapour Pressures," *J. Chem. Phys.*, **50**, 3725-3733 (1969).
12. L.B. Pankratz, "Thermodynamic Properties of Halides," U.S. Bureau of Mines Bulletin 674, 1984.