Hybrid Fuzzy Adaptive Control of LEGO Robots

Ján Vašěák, and Marián Mikloš**

*Department of Computational Intelligence and Systems Science,
Tokyo Institute of Technology,
4259 Nagatsuta, Midori-ku, Yokohama 226-8502, Japan,
**Department of Cybernetics and Artificial Intelligence,
University of Technology in Ko ice,
Letná 9, 042 00 Kosice, Slovakia

Abstract

The main drawback of "classical" fuzzy systems is the inability to design and maintain their database. To overcome this disadvantage many types of extensions adding the adaptivity property to those systems were designed. This paper deals with one of them a new hybrid adaptation structure, called gradient-incremental adaptive fuzzy controller connecting gradient-descent methods with the so-called self-organizing fuzzy logic controller designed by Procyk and Mamdani. The aim is to incorporate the advantages of both principles. This controller was implemented and tested on the system of LEGO robots. The results and comparison to a 'classical' (non-adaptive) fuzzy controller designed by a human operator are also shown here.

Key words: Fuzzy adaptive controller, Gradient-descent methods, Jacobian, Gradient-incremental adaptation

1. Introduction

Fuzzy logic has found many successful applications, especially in the area of control, but there are some limits of its use that are connected with the inability of the knowledge acquisition and adaptation to changed external conditions or parameters of the controlled system. To overcome this problem there were published lots of papers, e.g. [4, 8, 9], which deal with structures of Adaptive Fuzzy Controllers(AFC) using mostly approaches based on many variations of gradient-descent methods, the least square method [7], linear and non-linear regression or the linguistically based rule extraction.

Further, we will focus our attention only on 'pure' AFC. The main reason why to deal with this type of AFC is that they are with their nature and calculus the most similar systems to the non-adaptive (classical) FC. The properties of FC are well known, more than in the case of neural networks or genetic algorithms, in general. Fuzzy logic is able to simulate the human vague thinking very efficiently and therefore it seems to be very advantageous only to add the ability of the knowledge acquisition to 'classical' fuzzy systems and nearby to preserve their properties.

In this paper we will show the design of a hybrid control structure compound from two essential adaptation ways the well known Gradient-Descent Adaptation (GDA) and the so-called Self-Organizing Fuzzy Logic Controller(SOFLC)

proposed by Procyk and Mamdani [9] with the aim to connect their advantages. In the section 6 we will

show the implementation of this controller into the LEGO robots as well as some experiments with the evaluation of its efficiency.

II. Adaptation principles of fuzzy controllers

The adaptation task of FC consists in the adjusting parameters of its knowledge base to fulfill the general goal of control, i.e. to eliminate the difference between the desired w(k) and real output y(k) of the system to be controlled. In other words to eliminate the control error e(k) = w(k) - y(k) (k as sampling step related to the time t, t = T.k where T is the sampling period). Other criteria concerning, e.g. transition time, energy consumption, overshoots, etc. can be taken into consideration, too. In principle, the values of knowledge base parameters can be obtained in two ways: either by identifying the parameters of the controlled system or by measuring the control quality. The first way defines the so-called parameter-adaptive systems and the second the first case, performance-adaptive systems. In information about the controlled system obtained in such a way is then to be transformed into the form of fuzzy rules of the controller. Therefore the methods of this kind are known as indirect methods, too (see [1, 6]). The performance adaptive systems transform the measured control quality directly to the controller parameters excluding the need of the system identification. They enable also to include another criteria where the minimal control error (control task) seems to be only a

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special criterion.

The methods mentioned in the above are able to adjust either the parameters of membership functions (MF) or structure of rules or both. Mostly, they differ from the calculus used or other restriction conditions (type of MF, rule structure, etc.). However, most of them are based on minimizing the control error. As a gradient determines the shortest "descent" of this error in accordance on the knowledge base parameters it seems to be the most powerful adaptation method if there are no such application-dependent circumstances avoiding its use. SOFLC is also a special form embedding this calculus since it utilizes Jacobian what can be seen very clearly in (4). In the following we will describe both GDA and SOFLC used in our hybrid structure that can be included to direct methods.

Ill. Gradient-descent based adaptation of the knowledge base

Each GDA is based on searching for a minimum (in the best case for the global one) of the *error function* E(k). We will define it as $E(k) = e(k)^2/2$ and for the sake of simplicity we will omit the sampling step k in several formulae. Individual methods differ from one another by searching the minimum, defining the learning factor or other restriction conditions concerning, e.g. the shape of MF, etc. We will describe two ways of GDA here.

$$\Delta a_{i,j} = 2 \cdot (w - y) \cdot \operatorname{sgn}(x_i - a_{i,j}) \cdot \left(\frac{\sum_{p=1}^{N_{A_{i,j}}} \alpha_p \cdot b_p - y \cdot \sum_{p=1}^{N_{A_{i,j}}} \alpha_p}{\sum_{p=1}^{N_r} \alpha_p \cdot s_{i,j} \cdot \mu_{A_{i,j}}(x_i)} \right) \cdot \left(\frac{\sum_{p=1}^{N_{A_{i,j}}} \alpha_p \cdot (1 - \mu_{A_{i,p}}(x_i))}{\sum_{p=1}^{N_r} \alpha_p \cdot b_p - y \cdot \sum_{p=1}^{N_{A_{i,j}}} \alpha_p} \right) \cdot \left(\frac{\sum_{p=1}^{N_{A_{i,j}}} \alpha_p \cdot b_p - y \cdot \sum_{p=1}^{N_{A_{i,j}}} \alpha_p}{\sum_{p=1}^{N_{A_{i,j}}} \alpha_p \cdot (w - y)} \right)$$

$$\Delta b_j = \frac{\sum_{p=1}^{N_{A_{i,j}}} \alpha_p \cdot (w - y)}{\sum_{p=1}^{N_{A_{i,j}}} \alpha_p}$$

$$(1)$$

$$a_{i,j}(k+1) = a_{i,j}(k) + K_a \cdot \Delta a_{i,j}(k)$$

$$s_{i,j}(k+1) = s_{i,j}(k) + K_s \cdot \Delta s_{i,j}(k)$$

$$b_{i,j}(k+1) = b_{i,j}(k) + K_b \cdot \Delta b_{i,j}(k)$$
(2)

Let us consider a TSK controller (Takagi-Sugeno- Kang) with n inputs x_i and one output u of the j-th constant value b_j ($u = b_j$) with the product operator as the aggregation operator as well as MF in the symmetrical triangular form characterized by its center $a_{i,j}$ and support $s_{i,j}$ (limit points of the support are $a_{i,j} - s_{i,j}/2$ and $a_{i,j} + s_{i,j}/2$) where i and j denote the i-th input and the j-th linguistic value for this input,

respectively [2].

If there each input variable x_i has l_i linguistic values and the output variable m values then we will get in total m + 2.TN parameters where $TN = l_1 + ... + l_n$ is the total number of input MF. It can be proved their partial derivatives are in the form of (1) [5] where p = l, ..., N_{bj} refer to all rules with the consequent b_j and p = l,..., N_{Aij} to all rules with MF $A_{i,j}$ in their premises. N_r is the total number of rules and a_p the strength of the p-th rule.

It is evident the knowledge base parameters to be adjusted are $a_{i,j}$, $s_{i,j}$ and b_j . If we compute partial derivatives of E(k) by these parameters in each sampling step k then considering the well known properties of the gradient we will get for next step k+1 the following values of $a_{i,j}$, $s_{i,j}$ and bj as shown in (2).

where K_a , K_s and K_b are the learning factors.

If we introduce an additional condition of maintaining fuzzy partitions and $a_{i,j} < a_{i,2} < ... < a_{i,li}$ [3] then the support $s_{i,j}$ will be given by $a_{i,j+1}$ $a_{i,j-1}$ and the system of equations (1) will be modified as described in (3) where $r = 1, \cdot, N_r$.

$$\Delta \alpha_{i,j} = \begin{cases}
\frac{y - w}{a_{i,j} - a_{i,j-1}} \cdot \left[\frac{\mu_{A_{i,j}}(x_i)}{\mu_{A_{i,j-1}}(x_i)} \cdot \frac{1}{\mu_{A_{i,j-1}}(x_i)} \cdot \frac{1}{\mu_{A_{i,j-1}}(x_i)} \cdot \frac{1}{\mu_{A_{i,j-1}}(x_i)} \cdot \frac{1}{\mu_{A_{i,j-1}}(x_i)} \cdot \frac{1}{\mu_{A_{i,j}}(x_i)} \cdot \frac{1}{\mu_{A_{i,j+1}}(x_i)} \cdot \frac{1}{\mu_{A_$$

This method in contrast to (1) avoids generating uncovered parts of the universe of discourse by MF and shows mostly a better convergence. Further, the total number of parameters is $N_r + TN$ and in most cases less than in (1) (if $m + TN > N_r$).

IV. Structure of SOFLC

The control circuit with a performance-adaptive AFC known as SOFLC is shown in fig. 1. As already mentioned this structure enables incorporating also another criteria than only the minimal control error.

Control criteria are contented in the block of *performance measure* where the quality is evaluated by the *performance index* p(k) which expresses the magnitude and direction of changes to be performed in the knowledge base of the controller. The basic design problem of AFC consists in the design of M, where for each time sample t = K.T(K=0, I,...) a simplified incremental model of the controlled system M = J.T (J --- Jacobian) is computed. It represents a supplement to the

original model to reach a zero control error and is analogous to the linear approximation of the first order differential equation or in other words to gradients, too. As Jacobian (4) is a determinant of all first derivatives of the system with n equations $f_1,..., f_n$ of n input variables $x_1, ..., x_n$ it means J is equal to the determinant of the dynamics matrix, i.e. it is a numerical value describing all n gradients in the sense of a characteristic value.

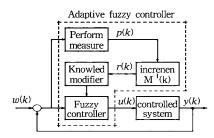


Fig. 1. Self-organizing fuzzy logic controller

Now we need to transform this incremental description of a controlled system to the description of a controlling system, i.e. a controller. Considering the properties of the feed back connection we can see that $y(k) \approx e(k)$ (w(k) is known). As inputs and outputs of a controlled system change to outputs and inputs of a controller, respectively we can get the controller description like the inverse function of $y(k) = f_M(u(k))$, i.e. the model of the controller is $u(k) = f_M^1(y(k))$. Because J is a number, then M^1 is the reverse value of J.T. The reinforcement value r(k) is computed as $r(k) = M^1.p(k)$.

$$J = \begin{vmatrix} \frac{\partial f_1}{\partial x_1} & \frac{\partial f_1}{\partial x_2} & \cdots & \frac{\partial f_1}{\partial x_n} \\ \vdots & \vdots & & & \vdots \\ \frac{\partial f_n}{\partial x_1} & \frac{\partial f_n}{\partial x_2} & \cdots & \frac{\partial f_n}{\partial x_n} \end{vmatrix} = \begin{vmatrix} grad & f_1 \\ \cdots \\ grad & f_n \end{vmatrix}$$
(4)

The knowledge base adaptation can be either relation-based or rule-based. For our purposes we will use the second way of adaptation. In general (for both methods), it is based on removing such rules $R_{new}(k)$ that caused a 'bad' control in the previous time step $R_{bad}(k)$ and including new 'reinforced' rules, i.e. for next time step k+1 we will get:

$$R(k+1) = (R(k) \cap \overline{R_{bad}}(k)) \cup R_{new}(k)$$
(5)

Each fuzzy rule r_p $(p = 1,...,N_r)$ of n inputs and one output represents their Cartesian product and is also a fuzzy relation $R_p = A_{1,p}$ x ...x $A_{n,p}$ x B_p . The knowledge base R is then a union of such rules (fuzzy relations) and after substituting into (5) it will be changed to (6). $R_{bad}(k)$ can be a union of all previously fired rules, too. However, for the sake of simplicity we will consider only one rule with the greatest strength and therefore A^{bad}_1 x ...x A^{bad}_n is its premise. Reinforcement value r(k) corrects only the consequent of such a rule and B_{new} is the fuzzified result of y(k) + r(k), i.e. fuzz(y(k) + r(k)). The simplest fuzzification is in the form of singletons but in general, other forms are possible, too.

$$R(k+1) = \begin{bmatrix} \bigcup_{p=1}^{N_r} (A_{1,p} \cap \overline{A_1^{bad}}) x \dots x A_{n,p} x B_p \end{bmatrix} \cup \dots \cup \begin{bmatrix} \bigcup_{p=1}^{N_r} A_{1,p} x \dots x (A_{n,p} \cap \overline{A_n^{bad}}) x B_p \end{bmatrix} \cup \bigcup_{p=1}^{N_r} A_{1,p} x \dots x A_{n,p} x (B_p \cap \overline{B^{bad}}) \end{bmatrix} \cup \bigcup_{R_{nw}} \underbrace{(A_1^{bad} x \dots x A_n^{bad} x B^{new})}_{R_{nw}}$$

$$(6)$$

V. Hybrid gradient-incremental adaptive fuzzy controller

In the above-described methods have their advantages and also drawbacks. GDA should be the fastest adaptation and it should converge after the minimal number of steps. However, there are two basic problems. First, an error function E(k)may be of a complex shape and hereby characterized by a number of local minima. It is very difficult in advance to estimate their number and possible place of the global minimum, i.e. optimal solution. Further, the absence of such estimation disables the determination of the learning factor value, too. If it is too small the convergence will be too slow and if it is too big there will be a risk the global minimum will be 'jumped over'. Secondly, there is possibility to minimize only one criterion error function but in the practice there are also other control criteria. SOFLC is more practice-oriented but it is sensitive to external signals such as disturbances, noises and set-point changes because of their inability to distinguish whether the parameters of the controlled system are changed or an external signal entered the system. A negative effect can occur if the adaptation proceeds although it is not more necessary. So some wrong changes in the knowledge base may be performed. This state is caused by the wrong understanding if e.g. an external error occurs and AFC will evaluate it as a parameter change. Therefore, we tried to connect these two methods to one hybrid MISO structure to avoid their drawbacks as seen in the fig. 2 and named it as Gradient-Incremental adaptive Fuzzy Controller(GIFC).

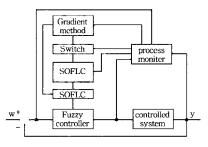


Fig. 2. Structure of a gradient-incremental adaptive fuzzy controller.

The adaptation process can be described in following steps:

- 1. Definition of input and output variables
- 2. Defining of term sets for variables in the step 1
- 3. Design of initial membership functions (not necessary)
- Processing GDA by (3) until the threshold of e(k) is reached
- 5. Processing SOFLC until the control error is greater than the threshold of e(k)
- 6. Processing GDA by (1) until the threshold is reached and repeated switching to the step 5

The main idea is that GDA is the fastest method if the threshold of the control error as the most important criterion is not too strict. In such a case we can choose a greater learning factor and speed up the adaptation. After this 'rough' adaptation we can switch the control to SOFLC to minimize the control error to be as small as possible and at this same time to include other criteria, too. GDA by (3) maintains fuzzy partitions. This condition owns several suitable properties but on the other hand side it is certain restriction in the adaptation process. Therefore, SOFLC does not hold this condition. However, if the control error increases again it will not more possible to switch adaptation to GDA by (3). From this reason it will be switched to GDA by (1).

From (6) it is evident the so-called problem of rule expansion can occur as each 'bad' rule can be replaced by up to n+1 new rules, i.e. if in each step just one rule is replaced the knowledge base will be expanded by n further rules. To prevent this effect a garbage collection mechanism was designed. Its task is to remove replaced and identical rules. If there are rules with identical premises but different consequents occur the older rule will be removed.

VI. Experiments

The proposed hybrid control algorithm GIFC was implemented and tested on LEGO robots. Its results were compared also with a non-adaptive FC designed by a human operator. The control task was the so-called *parking problem*, i.e. to park a mobile robot at a given place and direction. This task was solved with and without obstacles. The process monitor (see fig. 2) evaluates the parking process by two criteria: **parking error** E_P - more important corresponding with the control error and **trajectory error** E_T - considered only in SOFLC which is computed as division of the *real* trajectory length and *optimal* trajectory length. The optimal trajectory is the shortest distance between the robot and the goal. The first criterion is in the form:

$$E_P = \sqrt{(\phi_f - \phi)^2 + (x_f - x)^2 + (y_f - y)^2}$$
 (7)

where (x,y) are coordinates of the robot ϕ is the turning angle of wheels and (x_f, y_f, f) are position and direction of the goal (parking place). Similar description is used for starting (initial) points, too.

In the case of obstacles the strategy of their avoiding

depends on two light sensors. The existence of an obstacle is determined (supposed) if the light intensity of at least one sensor decreases under given threshold. There are two possibilities either the left or right direction and such a direction is chosen where the light intensity is higher. It supposes this way is shorter than another one to go round the obstacle. If the light intensity of both sensors is equal then the direction may be chosen randomly. In this case it is possible to define still one criterion -- number of impacts on the obstacle.

In figures 3, 4 and 5 results of several experiments for different starting points are depicted.

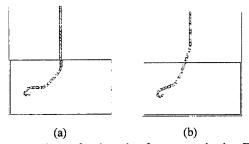


Fig. 3. Comparison of trajectories for a non-adaptive FC (20, 80, 260) (a) and GIFC (20, 80, 260) (b).

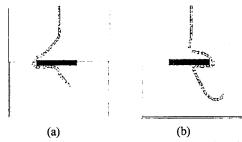


Fig. 4. Comparison of trajectories with an obstacle for a non-adaptive FC (60, 70, 150) (a) and GIFC (80, 80, 260) (b).

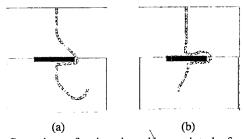


Fig. 5. Comparison of trajectories with an obstacle for a non-adaptive FC (80, 80, 260) (a) and GIFC (40, 80, 110) (b).

In the table 1 we can see that first two criteria E_P and E_T are better fulfilled at a non-adaptive FC. There are two reasons. First, E_P and E_T are not totally independent. Both are quantitative and E_P influences E_T directly proportionally. If E_P increases then also the trajectory will be more different from the optimal length but the shape may be in spite of that of 'better' what is also this case. It can be seen especially at the obstacle avoidance fig. 4 and 5. This assertion is supported by

a smaller number of impacts at GIFC than at non-adaptive FC. Secondly, reinforced rules are fired till in next steps after the error already occurred and in such a way delay influences the efficiency of GIFC negatively. Shortening the sampling period T can eliminate this problem. There are only hardware limitations.

Table 1. Comparison of the control quality for non-adaptive FC (NAFC) and GIFC.

Type	EP	ET	Number of impacts
NAFC	0.407	1.131	-
GIFC	6.545	1.132	-
NAFC	0.568	1.450	3.15
GIFC	4.706	1.521	1.33

VII. Conclusions

The principal advantage of this approach is the substitution of a human expert in the design of a fuzzy controller, which is the most serious disadvantage of standard fuzzy systems. The design presented enables fuzzy systems to move in an unknown outer area that can be changed, e.g. autonomous vehicles among obstacles. Experiments showed that the most important criterion of number of impacts is better than at non-adaptive FC designed by a human operator. The quality of other two criteria may be improved by reinforcing the garbage collection mechanism. Many rules are not yet removed from the knowledge base and they are more information noise than contribution. It is possible to improve it by removing rules with MF their average grade of membership is small further by merging rules with similar premises or by considering partial contradiction of rules with identical premises.

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