

Effective Algorithm in Steady-State Analysis for Variable-Speed and Constant-Speed Wind Turbine Coupled Three-Phase Self-Excited Induction Generator

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Abstract- In this paper, the steady-state operating performance analysis for the three-phase squirrel cage rotor self-excited induction generator (SEIG) driven by a variable-speed prime mover (VSPM) in addition to a constant-speed prime mover (CSPM) is presented on the basis of an effective algorithm based on its frequency-domain equivalent circuit. The operating characteristics of the three-phase SEIG coupled by a VSPM and/or a CSPM are evaluated on line processing under the condition of the electrical passive load parameters variations with simple and efficient computation processing procedure in unregulated voltage control loop scheme. A three-phase SEIG prototype setup with a VSPM as well as a CSPM is implemented for the small-scale clean renewable and alternative energy utilizations. The experimental operating characteristic results are illustrated and give good agreements with the simulation ones.

Keywords: Three-Phase Self-Excited Induction Generator, Variable-Speed and Constant-Speed Wind Turbine, Stand-Alone Power Conditioner, Renewable Energy Sources

1. Introduction

In the stand-alone operation for clean rural alternative energy utilization areas, the three-phase induction generator can operate in the self-excitation power generation mode when an appropriate capacitor bank assembly connected on its stator terminal ports and driven by the renewable energy prime mover as a wind turbine[1], [2]. The three-phase self-excited induction generator (SEIG) determines its own generated terminal voltage and its output frequency, which strongly depend on the capacitance of the fixed excitation capacitor bank, the circuit parameters of the three-phase induction generator, the electrical passive circuit components of the stand-alone load or the independent load and the angular speed of the prime mover as the wind turbine[3-6]. The approximate steady-state circuit analysis in a frequency domain of the three-phase SEIG has been done so far with the following generic assumptions for a few papers presented previously [2-9], that is,

- Iron losses are negligible
- Only fundamental M.M.F. waves are considered
- Resistances and reactances of the three-phase induction generator are constant, except for the magnetizing reactance described graphically by means of the magnetization curve.

-The rate of change in the parameters and variables of the electro-mechanical equivalent circuit is extremely small, so that the per-phase steady-state equivalent circuit in the frequency domain can be used so far.

This paper describes a simple algorithm to evaluate the steady-state operating performance analysis of the three-phase SEIG driven by a variable-speed prime mover (VSPM) as well as a constant-speed prime mover(CSPM) based on the electro-mechanical equivalent circuit representation in the frequency domain basis as promising stand-alone power supplies in rural district.

2. Variable-Speed Prime Mover Characteristics

The mechanical output power P_m of the VSPM is defined as [1-6],

$$P_m = T_m \omega_s \nu \quad (1)$$

where ν is the per unit speed of the VSPM ($\nu=N/N_s$), N and N_s are the rotor speed and the three-phase SEIG synchronous speed in (rpm), respectively. ω_s is the rated synchronous angular speed ($\omega_s = 2\pi N_s/60$). T_m is the mechanical output torque of the VSPM in N.m and represented by,

$$T_m = \tau_o - \nu_o \nu \quad (2)$$

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where τ_o and v_o respectively are the torque coefficient and the speed coefficient in N.m.

In experiment, a controllable separately-excited dc motor is used with constant armature voltage and a field current control. Fig.1 illustrates the effect of the field current control on the torque speed characteristics and the corresponding torque-speed coefficients τ_o and v_o which are given by,

$$\tau_o = \frac{K_t \phi_m V_a}{R_a} \quad \text{and} \quad v_o = \frac{2\pi K_t^2 \phi_m^2}{60R_a} N_s$$

where K_t is the torque constant, ϕ_m is the field flux in wb per pole of the dc motor, V_a is the armature voltage in volt and R_a is the armature resistance in ohm.

3. Steady-State Analysis of Three-Phase SEIG Driven By Variable-Speed Prime Mover

The nodal admittance approach-based circuit analysis is applied on the approximate frequency domain-based electro-mechanical equivalent circuit of the three-phase SEIG

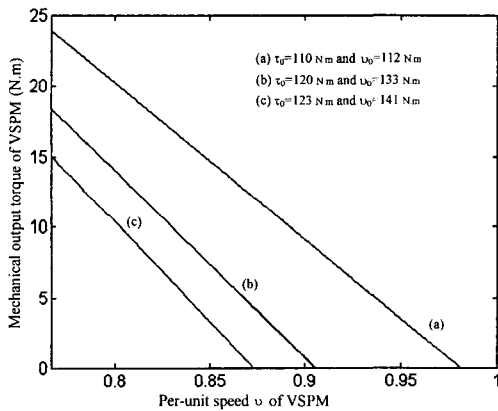


Fig. 1 Mechanical output torque characteristics of VSPM against its per-unit speed

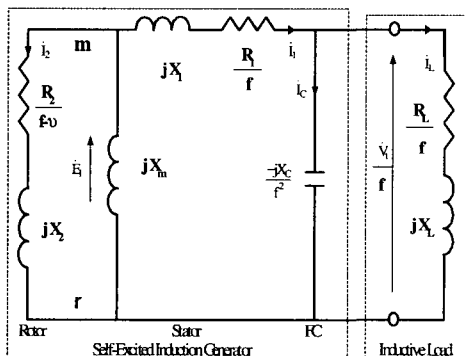


Fig. 2 Per-phase equivalent circuit of three-phase SEIG

in Fig.2 with the per-unit frequency, f ($f=F/F_b$, F and F_b are the generated output frequency and base frequency of the three-phase SEIG) and the relative rotor speed v ($v=N/N_s$, $N_s=1500$ rpm when $F_b=50$ Hz) as state variables.

In Fig.2, R_1 , X_1 , R_2 and X_2 are the three-phase SEIG parameters referred to its stator winding side, R_L and X_L are the inductive load components in ohm, X_C is the excitation capacitive reactance in ohm ($X_C=(1/2\pi F_b C; F_b=50\text{Hz}$ and C is the excitation capacitance in farad), X_m is the magnetizing reactance in ohm, \dot{E}_1 , \dot{V}_1 , \dot{I}_1 , \dot{I}_2 , \dot{I}_L and \dot{I}_C are the per-phase air gap voltage in volt, the per-phase generated terminal voltage in volt, the per-phase stator current in ampere, the per-phase rotor current in ampere referred to the stator side, the per-phase load current in ampere and the per-phase excitation current in ampere for the three-phase SEIG, respectively.

The squirrel cage rotor current I_2 referred to the stator winding side of the three-phase SEIG can be defined as,

$$I_2 = \frac{E_1}{R_2 \sqrt{\frac{1}{(f-v)^2} + \left(\frac{X_2}{R_2}\right)^2}} \quad (3)$$

In actual, the term $(f-v)$ is extremely small from a practical point of view, the term (X_2^2/R_2^2) in (3) could be substantially neglected with respect to $1/(f-v)^2$. Thus, the above equation of the rotor current I_2 referred to the stator winding circuit side can be expressed by the following simple equation,

$$I_2 = \frac{(f-v)E_1}{R_2} \quad (4)$$

The mechanical input power P_i (watt) of the three-phase SEIG is estimated by the reference [5]

$$P_i = -3I_2^2 \frac{R_2}{(f-v)} \left(\frac{v}{f}\right) \quad (5)$$

By substituting I_2 into (5) and making a mechanical power balance through equating (5) and (1). The per-unit speed v can be derived as a function of the per-unit frequency f ,

$$v = \frac{(\tau_o + \frac{3E_1^2}{R_2 \omega_s})f}{v_o f + \frac{3E_1^2}{R_2 \omega_s}} \quad (6)$$

By using the nodal admittance approach on the magnetizing reactance X_m , the following equation can be written as,

$$(\dot{Y}_{mr} + \dot{Y}_m + \dot{Y}_r)\dot{E}_1 = 0 \quad (7)$$

For the successful generated terminal voltage building up of the three-phase SEIG, E_1 does not equal to zero, the relationship of the following nodal admittance yields;

$$\dot{Y}_{mr} + \dot{Y}_m + \dot{Y}_r = 0 \quad (8)$$

where \dot{Y}_{mr} , \dot{Y}_m and \dot{Y}_r can be represented by using the equivalent circuit shown in Fig.2 as follow;

$$\dot{Y}_{mr} = \frac{1}{\left(\frac{R_L}{f} + jX_L\right)\left(\frac{-jX_C}{f^2}\right) + \frac{R_1}{f} + jX_1} \quad (9)$$

$$\text{or } \dot{Y}_{mr} = G_{mr} + jB_{mr},$$

$$\text{where } G_{mr} = \frac{D_1f + D_3f^3 + D_5f^5}{D_0 + D_2f^2 + D_4f^4 + D_6f^6}$$

$$\text{and } B_{mr} = \frac{(C_0 + C_2f^2 + C_4f^4)f^2}{D_0 + D_2f^2 + D_4f^4 + D_6f^6}$$

$$\dot{Y}_m = -\frac{j}{X_m} \quad (10)$$

$$\dot{Y}_r = \frac{1}{\left[\frac{R_2}{f - v} + jX_2\right]} \quad (11)$$

$$\dot{Y}_r = \frac{(-\tau_0 + v_0f)f}{\left(\frac{3E_1^2}{\omega_s} + v_0R_2f\right) + j(-\tau_0 + v_0f)X_2f}$$

$$\text{or } \dot{Y}_r = G_r + jB_r$$

$$\text{where } G_r = \frac{(A_0 + A_1f + A_2f^2)f}{T_0 + T_1f + T_2f^2 + T_3f^3 + T_4f^4}$$

$$\text{and } B_r = \frac{(Q_0 + Q_1f + Q_2f^2)f^2}{T_0 + T_1f + T_2f^2 + T_3f^3 + T_4f^4}$$

The constants A_i ($i=0\sim 2$), D_j ($j=0\sim 6$), C_k ($k=0,2,4$), T_l ($l=0\sim 4$), and Q_h ($h=0\sim 2$) are estimated in Appendix.

Equating the sum of the imaginary terms in (8) to zero, the magnetizing reactance can be obtained by,

$$X_m = \frac{1}{B_r + B_{mr}} \quad (12)$$

where B_{mr} and B_r are given by (9) and (11), respectively. Equating the sum of the real terms of (8) to zero, the 8th order polynomial equation a function of the per unit frequency f can be written by,

$$Y_8f^8 + Y_7f^7 + Y_6f^6 + Y_5f^5 + Y_4f^4 + Y_3f^3 + Y_2f^2 + Y_1f + Y_0 = 0 \quad (13)$$

where the real coefficients from Y_0 to Y_8 can be expressed in Appendix .

To compute the steady-state performance of the three-phase SEIG, the steady-state value of the air-gap voltage E_1 is required. The magnetization curve obtained from the no-load test, which is used to obtain the air-gap voltage E_1 against the magnetizing reactance X_m curve shown in Fig.3, is then represented by the following equation,

$$E_1 = \begin{cases} 207.2 - 3.77X_m & X_m \leq 24.2 \\ 541.7 - 17.79X_m & 24.2 \leq X_m \leq 26.5 \\ 0 & X_m \geq 26.5 \end{cases} \quad (14)$$

By using Newton Raphson method with the initial value of the per-unit frequency $f = \tau_0/v_0$, the per-unit frequency f can be determined from (13) and can be then substituted into (12) to calculate the magnetizing reactance X_m . The air gap voltage E_1 is estimated from (14).

The following equations are used for describing the three-phase SEIG performances,

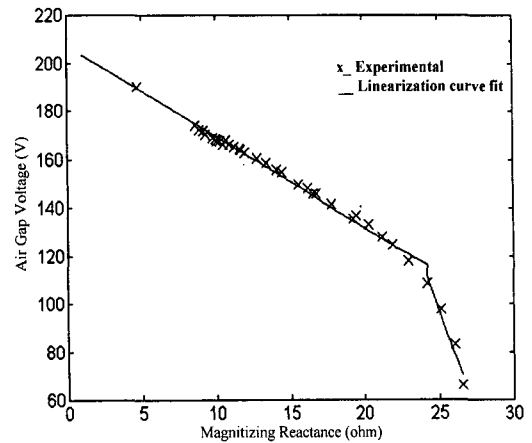


Fig. 3 Air-gap voltage E_1 vs. magnetizing reactance X_m of SEIG

$$V_t = fE_1 \sqrt{R_{eq}^2 + X_{eq}^2} \quad (15)$$

$$\text{where } R_{eq} = X_1 B_{mr} - \frac{R_1}{f} G_{mr} + 1$$

$$\text{and } X_{eq} = X_1 G_{mr} + \frac{R_1}{f} B_{mr}$$

$$I_L = \frac{V_t}{\sqrt{R_L^2 + f^2 X_L^2}} \quad (16)$$

$$P_L = 3I_L^2 R_L \quad (17)$$

$$Q_L = 3fI_L^2 X_L \quad (18)$$

where V_t , I_L , P_L and Q_L are the per-phase generated terminal voltage of the three-phase SEIG, the per-phase load current, and the total active power and reactive power of the balanced passive load, respectively.

4. Performance Analysis of SEIG with Constant-Speed Prime Mover

The steady-state theoretical algorithm of the three-phase SEIG driven by a VSPM is used to calculate the operating performance evaluations of the CSPM coupled three-phase SEIG. With a constant speed or relative rotor speed v , the admittances; \dot{Y}_{mr} and \dot{Y}_m have been expressed, respectively by (9) and (10). While \dot{Y}_r , a function of the relative rotor speed v , can be represented from (11) under the conditions of neglecting the coefficient $(3E_1^2/\omega_s)$ and setting to $v_0=1$ and $\tau_0=v$ and given by,

$$\dot{Y}_r = \frac{1}{\left[\frac{R_2}{f-v} + jX_2 \right]} \quad (19)$$

$$\text{or } \dot{Y}_r = \frac{(f-v)}{R_2 + j(f-v)X_2}$$

The 8th degree polynomial equation represented in the per unit frequency f and defined as (13) is expressed by

$$Y_{8c}f^7 + Y_{7c}f^6 + Y_{6c}f^5 + Y_{5c}f^4 + Y_{4c}f^3 + Y_{3c}f^2 + Y_{2c}f + Y_{1c} = 0 \quad (20)$$

where the real coefficients from Y_{1c} to Y_{8c} are obtained and derived from the real coefficients from Y_0 to Y_8 under the conditions of neglecting the coefficient $(3E_1^2/\omega_s)$ and setting to $v_0=1$ and $\tau_0=v$ in the Appendix. The three-phase SEIG performances such as its generated terminal voltage, the load current, and the total active power and reactive power of the balanced inductive load can be calculated un-

der the above conditions by using (15), (16), (17) and (18), respectively.

5. Experimental and Simulation Results

5.1 Performance Evaluations of SEIG with Variable-Speed Prime Mover

The steady-state analytical algorithm of the three-phase SEIG driven by a VSPM is based on the per-phase electro-mechanical equivalent circuit of the three-phase SEIG shown in Fig.2. The nodal admittance approach is applied to determine the characteristics of the three-phase SEIG driven by a variable-speed prime mover VSPM as wind turbine. A feasible prototype of the three-phase SEIG driven by a VSPM represented by a controllable separately-excited dc motor is built and tested actually. The no-load generated terminal voltage vs. the excitation capacitance characteristics, which are selected to be chosen above the minimum value required to build up the terminal voltage of the three-phase SEIG driven by a VSPM is shown in Fig.4. The terminal voltage of the three-phase SEIG driven by a VSPM with a certain torque-speed characteristic ($\tau_0=120$, $v_0=133$) increases with the excitation capacitance and also with changing the torque-speed characteristic from ($\tau_0=120$, $v_0=133$) to another one ($\tau_0=110$, $v_0=112$) as illustrated in Fig.1. Fig.5 indicates the variations of the output frequency of the three-phase SEIG driven by a VSPM against its excitation capacitance at no load with different torque-speed characteristics. The output frequency of the three-phase SEIG decreased with increasing the excitation capacitance from 150 μ F to 350 μ F at a certain torque-speed coefficients ($\tau_0=120$, $v_0=133$ where the VSPM speed decreases in accordance with the torque-speed characteristic of the VSPM shown in Fig.1) and increases linearly with increasing the speed as with another torque-speed coefficients ($\tau_0=110$, $v_0=112$). Fig.6 represents the steady-state generated terminal voltage variations of the three-phase SEIG coupled by a VSPM with a certain torque-speed characteristic ($\tau_0=120$, $v_0=133$) and its output power when it is excited by three different capacitances of the excitation capacitor bank ($C=194\mu$ F, 244μ F, and 294μ F per-phase) and supplying to a balanced three-phase resistive load. Fig.7 depicts the generated terminal voltage variations against the VSPM speed according its specified torque-speed characteristic when the three-phase SEIG loaded by a balanced resistive load. Fig.6 and Fig.7 indicate that the generated terminal voltage of the three-phase SEIG driven by a VSPM decreases as increasing its output power, which also decreases the VSPM speed. The VSPM speed decreases in accordance with the torque-speed char-

acteristic of the VSPM from the no load $N=1360$ rpm to the full load $N=1220$ rpm. For an inductive load condition with 0.8 lagging power factor, a certain torque-speed coefficients ($\tau_0=120$, $\nu_0=133$) and various capacitances ($C=194 \mu\text{F}$, $244 \mu\text{F}$, and $294 \mu\text{F}$ per phase) of the excitation capacitor bank, Fig.8 illustrates the three-phase SEIG terminal voltage variations with the output power calculated from the digital simulation and experimental results. In Fig.9, the terminal voltage vs. the VSPM speed with a certain torque-speed characteristic ($\tau_0=120$, $\nu_0=133$) is represented due to the inductive load variations. Fig.8 and Fig.9 indicate that the generated terminal voltage tends to fall steeply with the balanced three-phase inductive load as compared with the resistive load. The maximum output power can be found to be less than that to be supplied to a resistive load and the prime mover speed decreases in accordance with the torque-speed characteristic of the VSPM from the no load rotor speed $N=1360$ rpm to the full load rotor speed $N=1260$ rpm. With inductive loads, the terminal excitation

capacitors must provide the reactive load power to the inductive load in addition to reactive load power to the three-phase SEIG. Therefore, an additional shunt capacitance would be required for improved voltage regulation.

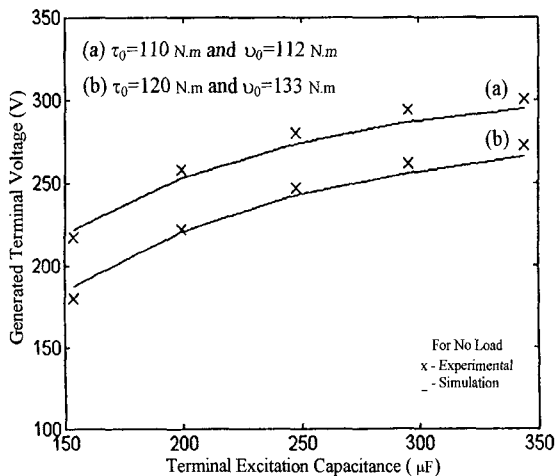


Fig. 4 No load terminal voltage variations of SEIG driven by VSPM vs. excitation capacitance

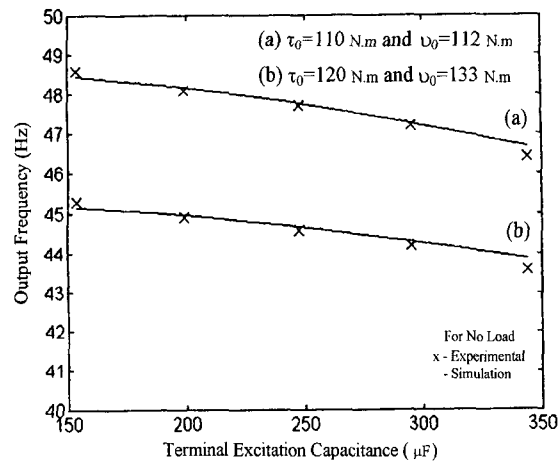


Fig. 5 Output frequency variations of SEIG driven by VSPM vs. excitation capacitance

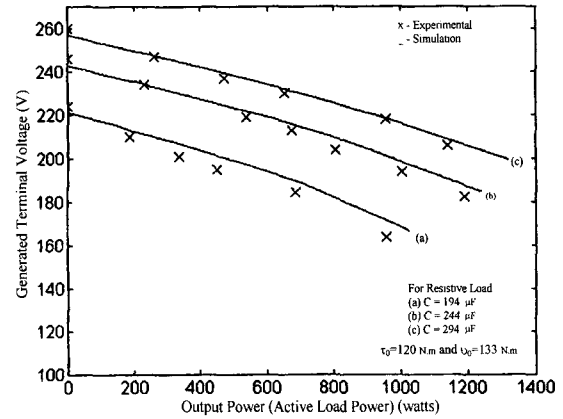


Fig. 6 Terminal voltage variations of SEIG driven by VSPM vs. the resistive load power

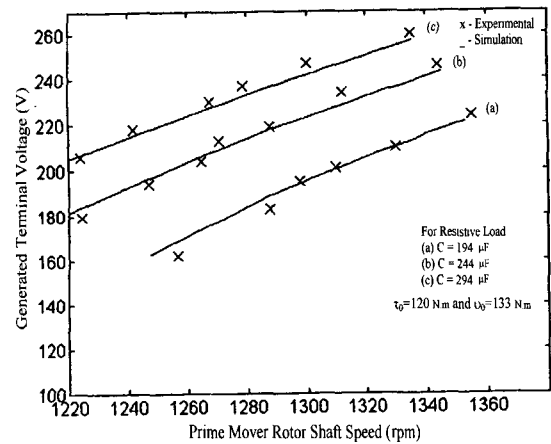


Fig. 7 Terminal voltage of SEIG driven by VSPM against its rotor speed due to the resistive load variations

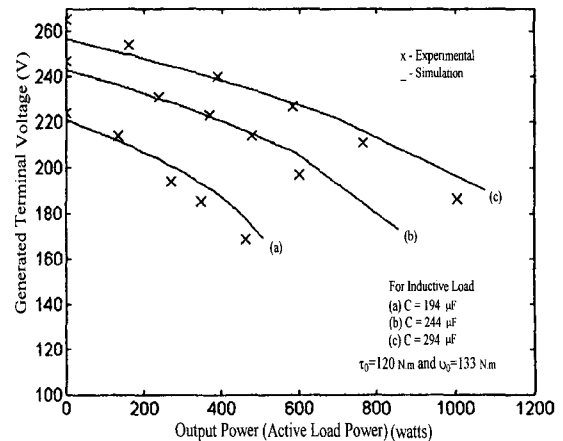


Fig. 8 Terminal voltage variations of SEIG driven by VSPM against the inductive load power

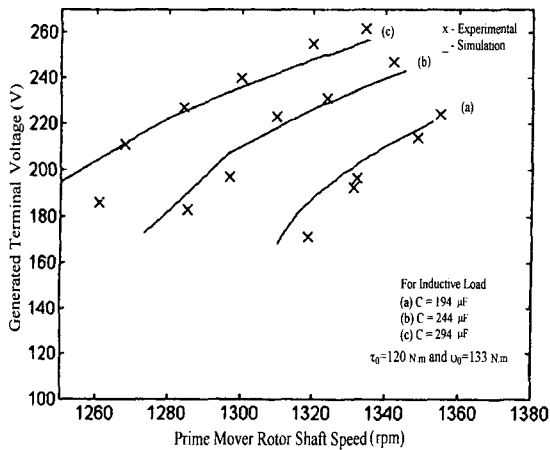


Fig. 9 Terminal voltage variations of SEIG driven by VSPM against its rotor speed due to the inductive load variations

5.2 Performance Evaluations of SEIG with Constant-Speed Prime Mover

For the three-phase SEIG driven by a CSPM with different constant speeds; $N=1400$ rpm, $N=1300$ rpm and $N=1250$ rpm, the no-load generated terminal voltage vs. the excitation capacitance characteristics which are selected to be chosen above the minimum value required to build up the three-phase SEIG terminal voltage is shown in Fig.10. The terminal voltage of the three-phase SEIG increases with the capacitances of the excitation capacitor bank at a constant speed and with increasing the CSPM speed. Fig.11 indicates the variations of the output frequency of the three-phase SEIG against its excitation capacitance with different constant speeds; $N=1400$ rpm, $N=1300$ rpm and $N=1250$ rpm. The output frequency of the three-phase SEIG driven by a CSPM slightly changes with increasing the excitation capacitance from $150 \mu\text{F}$ to $350 \mu\text{F}$ and increases linearly with increasing the CSPM speed. Fig.12 gives the load characteristics of the three-phase SEIG terminal voltage with the output power for a fixed capacitance of the excitation capacitor bank at a constant speed $N=1300$ rpm when supplying a resistive load. The terminal voltage variation is shown in the same figure for three values of excitation capacitances ($C=244\mu\text{F}$, $294\mu\text{F}$ and $344\mu\text{F}$ per-phase). The terminal voltage drops with increasing the load power and increases with increasing the capacitance of the excitation capacitor bank. Also, at the lower capacitance, the maximum output power extracted from the three-phase SEIG is lower than for the higher capacitance. Fig.13 depicts the variation of the terminal voltage of the three-phase SEIG with its output power for an inductive load with 0.8 lagging power factor under the conditions of various capacitances of the excitation capacitor bank and a constant speed $N=1300$ rpm. The

terminal voltage of the three-phase SEIG drops with increasing the inductive load and the maximum output power

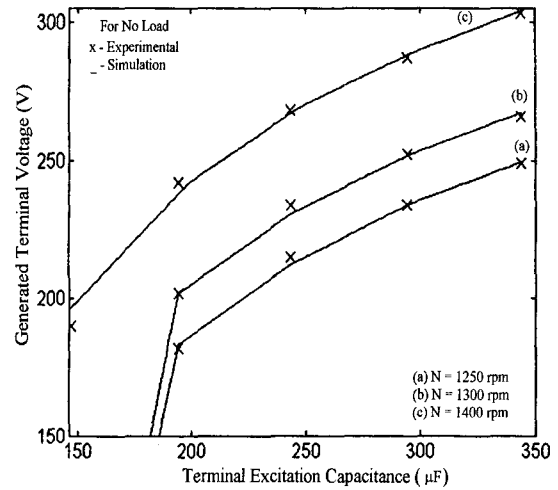


Fig. 10 No load terminal voltage of SEIG driven by CSPM vs. excitation capacitance

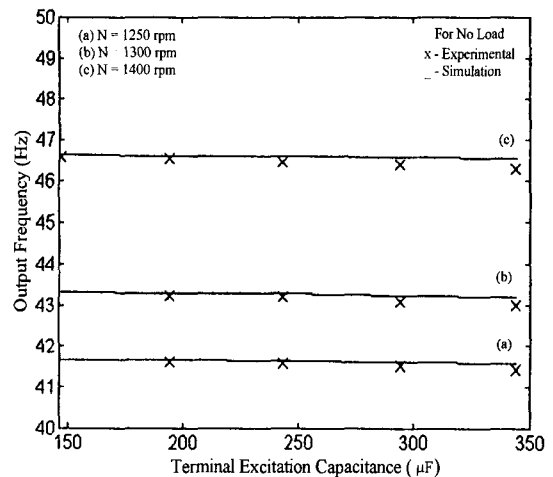


Fig. 11 Output frequency of SEIG driven by CSPM vs. excitation capacitance

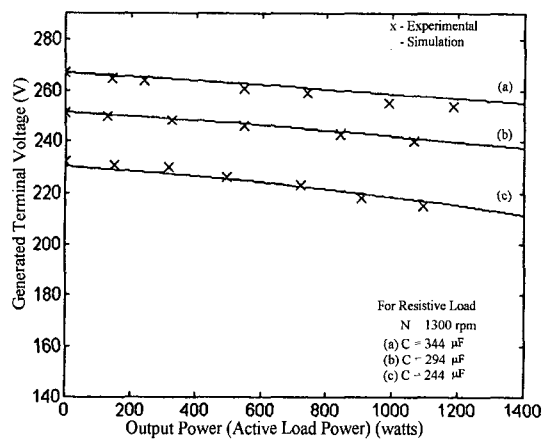


Fig. 12 Terminal voltage of SEIG driven by CSPM vs. the resistive load power

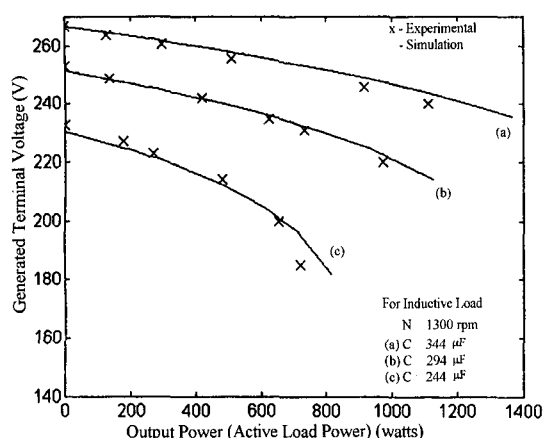


Fig. 13 Terminal voltage of SEIG driven by CSPM against the inductive load power

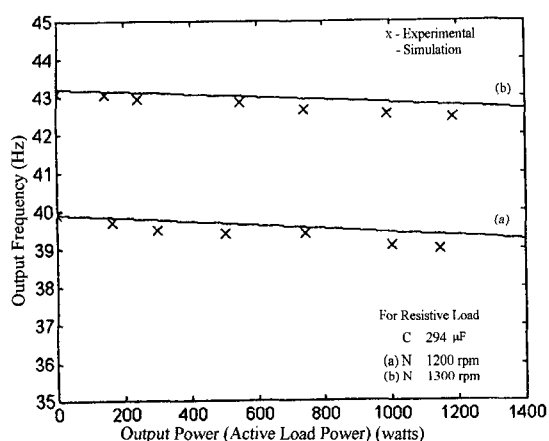


Fig. 14 Output frequency of SEIG driven by CSPM against the resistive load power

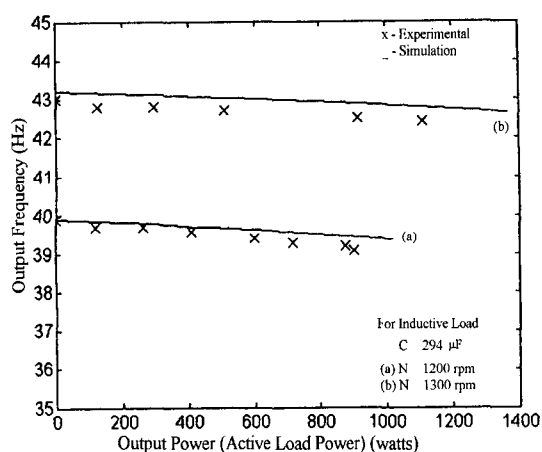


Fig. 15 Output frequency of SEIG driven by CSPM against the inductive load power

extracted from the three-phase SEIG increases with the CSPM than that with the VSPM. Fig.14 and Fig.15 show the output frequency variations of the three-phase SEIG against its output power for both a resistive and an

inductive loads, respectively with a fixed excitation capacitance $C=294\mu\text{F}$ and different values of constant speeds. The output frequency of the three-phase SEIG drops from the no load to the full load which means that the output frequency of the three-phase SEIG changes with the load power variations but with small variation ranges. The frequency variations increase with the inductive load.

6. Conclusions

This paper has introduced an effective theoretical algorithm for the steady-state frequency domain circuit analysis and operating performance evaluations based on the electro-mechanical equivalent circuit of the three-phase SEIG driven by a VSPM in addition to a CSPM. A squirrel cage three-phase SEIG prototype setup was established for the low cost wind turbine type rotating power conditioner in the rural alternative energy effective utilization areas from an earth environmental protection point of view. The feasible experimental results in the steady-state operating performances of the three-phase SEIG had pretty good agreements with those obtained from the digital simulation ones.

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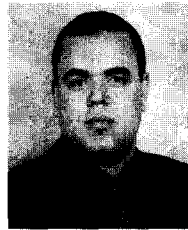
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Appendix

$$\begin{aligned}
 A_0 &= G_0 G_2, \\
 A_1 &= G_1 G_2 + G_0 G_3, \\
 A_2 &= G_1 G_3, \\
 D_0 &= Z_0^2, \\
 D_2 &= Z_1^2 + 2Z_0 Z_2, \\
 D_4 &= Z_2^2 + 2Z_3 Z_1, \\
 D_6 &= Z_3^2, \\
 D_1 &= -X_C Z_0, \\
 D_3 &= R_1 Z_1 + X_L Z_0 - Z_2 X_C, \\
 D_5 &= R_1 Z_3 + X_L Z_2, \\
 C_0 &= -Z_1 X_C - R_1 Z_0, \\
 C_2 &= Z_1 X_L - Z_3 X_C - Z_2 R_L, \\
 C_4 &= Z_3 X_L, \\
 T_0 &= G_0^2, \\
 T_1 &= 2G_0 G_1, \\
 T_2 &= G_1^2 + G_2^2 X_2^2, \\
 T_3 &= 2G_2 G_3 X_2^2, \\
 T_4 &= G_3^2 X_2^2, \\
 Q_0 &= -G_2^2 X_2, \\
 Q_1 &= -2G_2 G_3 X_2, \\
 Q_2 &= -G_3^2 X_2, \\
 Z_0 &= -R_1 X_C - X_C R_L, \\
 Z_1 &= X_C X_L + X_1 X_C + R_1 R_L, \\
 Z_2 &= R_1 X_L + X_1 R_L, \quad Z_3 = -X_1 X_L,
 \end{aligned}$$

$$\begin{aligned}
 Y_0 &= T_0 D_1 + A_0 D_0, \\
 Y_1 &= T_1 D_1 + A_1 D_0, \\
 Y_2 &= T_2 D_1 + T_0 D_3 + A_0 D_2 + A_2 D_0, \quad Y_3 = T_3 D_1 + T_1 D_3 + A_1 D_2, \\
 Y_4 &= T_4 D_1 + T_2 D_3 + T_0 D_5 + A_0 D_4 + A_2 D_2 \quad Y_5 = T_3 D_3 + T_1 D_5 + A_1 D_4, \\
 Y_6 &= T_4 D_3 + T_2 D_5 + A_0 D_6 + A_2 D_4, \\
 Y_7 &= T_3 D_5 + A_1 D_6, \\
 Y_8 &= T_4 D_5 + A_2 D_6
 \end{aligned}$$

Where $G_0 = 3E_1^2 / \omega_s$, $G_1 = v_0 R_2$, $G_2 = -\tau_0$ and $G_3 = v_0$,
 $R_1 = 0.52 \text{ ohm}$, $X_1 = 1.01 \text{ ohm}$, $R_2 = 0.52 \text{ ohm}$,
 $X_2 = 1.01 \text{ ohm}$,
 $\tau_0 = 120$, $v_0 = 133$, $N_s = 1500 \text{ rpm}$, $\omega_s = 2\pi N_s / 60.0$,



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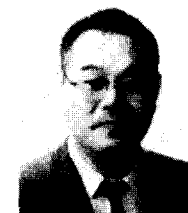
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