# Rotational State Distributions of $\mathbf{I}_{2}(B)$ from Vibrational Predissociation of $\mathbf{I}_{2}(B)$-Ne 

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#### Abstract

The vibrational predissociation of triatomic. i.e.. atom-diatom. van der Waals complexes in transient electronic excited state has been widely investigated. The predissociation rates or lifetimes are major concems of the previous studies. Experimentally rotational state distributions of diatonic product are hardly investigated and few theoretical stuides on rotational state distributions have appeared in literature. In this work. choosing the frequently studied $\mathrm{I}_{2}(B)$-Ne complex as an example, we investigate the change of rotational state distributions of $\mathrm{I}_{2}(B)$ produced from predissociation of the various initial states of $\mathrm{I}_{2}(B)-\mathrm{Ne}$. The present study on the rotational distributions indicates that rotational state distributions depend significantly on the predissociation energy and the van der Waals vibrational modes of $\mathrm{I}_{2}(B)-\mathrm{Ne}$. That is, the initial state dependency of rotational state distributions is extensively discussed.


Key Words : Vibrational predissociation I_-Ne

## Introduction

The vibrational predissociation is one of important intramolecular energy transfer (from vibrational to translational energy transfer) phenomena that occur within a molecule having a weak bond. The systems of which vibrational predissociation dynamics is frequently and extensively studied are triatomic (atom-diatom) van der Waals complexes having a typical weak van der Waals bond and one very strong diatomic bond. Particularly (Hal) -Rg (= diatomic halogen + rare gas atom) complexes in their excited electronic state are widely studied experimentally and theoretically. ${ }^{1,2} \mathrm{~A}$ triatomic (Hal)-Rg complex can be represented as $A B-C$ $\left(v_{1}, v . v_{2}, v_{3}\right)$ that has three vibrational degrees of freedom. The vibrational quantum number $v_{1}$ represents the fast stretching motion of A-B. $v_{2}$ is for the van der Waals stretching motion of $C$ with respect to AB . and $v_{3}$ is for the van der Waals bending motion of $C$ with respect to $A B$. The vibrational predissociation process can be viewed as $\mathrm{AB}-\mathrm{C}\left(v_{1}, v_{2}, v_{3}\right) \rightarrow$ $\mathrm{AB}\left(v^{\prime}, j^{\prime}\right)+\mathrm{C}$ where $v^{\prime}$ is the vibrational quantum number and $j^{\prime}$ is the rotational quantum number of free diatomic molecule AB . When $v^{\prime}$ is smaller than $v_{1}\left(\right.$ i.e.. $\Delta v\left(=v^{\prime}-v_{1}\right)$ is negative), vibrational predissociation of $\mathrm{AB}-\mathrm{C}$ occurs.
Since the early stage of predissociation research ${ }^{3-6}$ the vibrational predissociation of $\mathrm{I}_{-}(B)-\mathrm{Ne}$ (in the excited ${ }^{3} \Pi$ $\left(0_{n}^{-}\right)$electronic state ${ }^{7}$ ) has been most frequently investigated. ${ }^{\frac{8}{\bullet} \cdot 4}$ The first investigation by Levy's group measured predissociation rates and some excited vibrational energy levels of $\mathrm{I}_{2}(B)$ Ne. ${ }^{3.6}$ The accurate vibrational predissociation rates (or lifetimes) of $\mathrm{I}_{2}(B)-\mathrm{Ne}\left(v_{1}, 0.0\right)$ were first reported by Zewail and coworkers. ${ }^{[161]}$ It is found that the vibrational predissociation rates of $\mathrm{I}_{2}(B)-\mathrm{Ne}\left(v_{1}, 0,0\right)$ increase as $v_{1}$ increases. Recently Heaven and coworkers reported their double resonance studies on $\mathrm{I}(B)$-Ne predissociation. ${ }^{3033}$ So far, experimentally the dissociation energy of $\mathrm{I}_{2}(B)-\mathrm{Ne}(34.0,0)$ are measured as

[^0]$53.7 \mathrm{~cm}^{-1}$. For few excited states, e.g. $\mathrm{I}_{2}(B)-\mathrm{Ne}(34,1.0)$, $\mathrm{I}_{2}(B)-\mathrm{Ne}(34,0.2), \mathrm{I}_{2}(B)-\mathrm{Ne}(34.0,4)$ and $\mathrm{I}_{2}(B)-\mathrm{Ne}(33,1.0)$, etc., the vibrational levels are detemmed. ${ }^{23}$ The predissociation rates for excited (in van der Waals modes) $\mathrm{I}_{2}(B)-\mathrm{Ne}\left(v_{1}, v_{2}>\right.$ $\left.0 . v_{3}>0\right)$ are hardly studied while the predissociation of $\mathrm{I}_{2}(B)-\mathrm{Ne}\left(v_{1}, 0,0\right)$ are investigated for various $w_{1}$. It is also found that the vibrational predissociation process of $\Delta v=-1$ channel. i.e.. $\mathrm{I}_{2}(B)-\mathrm{Ne}\left(v_{1}, 0.0\right) \rightarrow \mathrm{I}_{2}\left(B . v_{1}-1\right)+\mathrm{Ne}$. is closed when $v_{1}>36$. The vibrational predissociation through the $\Delta v=-1$ chamel is not efficient when $v_{1}>322^{20}$

Theoretical investigations on vibrational predissociation of $\mathrm{I}_{2}(B)$-Ne have also been carried out extensively. ${ }^{13-19,21.24}$ The most widely used potential energy function is a pairvise sum of the potentials of diatomic I-I and of Ne-I. The I-I potential energy function is empirically determined from the Zewail's experiment. ${ }^{12,17}$ And the Ne-I potential function is usually taken as a Morse type function whose parameters are fitted to reproduce the experimental predissociation lifetimes of $\mathrm{I}_{2}(B)-\mathrm{Ne}$. Once the potential function is determined. theoretical calculations reveal detailed infomations on predissociation. i.e.. the predissociation rates, rotational state distributions of product. energy levels including high excited states, etc. The recent theoretical work on $\mathrm{I}_{2}(B)-\mathrm{Ne}\left(v_{1}, 0.0\right)$ is Garcia-Vela's wave packet calculations. ${ }^{14}$ García-Vela suggested a modified potential energy function that is fitted to the above experimental information. And with his modified potential function he calculated the vibrational state distributions. rotational state distributions of product $\mathrm{I}_{2}$, and lifetimes of $\mathrm{I}_{2}(B)-\mathrm{Ne}$. etc.

The vibrational predissociations from the van der Waals excited ( $v_{1}, v_{2}>0, v_{3}>0$ ) levels are also theoretically investigated. ${ }^{-4}$ The calculations reveal that the excitation energies from the ground state to the states with van der Waals bending mode excited ( Ne bending around $\mathrm{I}_{2}$. i.e., $v_{3}>0$ ) are smaller than those to the states with stretching mode excited ( Ne stretching against $\mathrm{I}_{2}$. i.e., $v_{2}>0$.) That is, the bending vibrational energy is smaller than that of
stretching motion. regardless of the vibrational motion of I-I stretching ( $v_{1}$ ) vibration. The predissociation rates through $\Delta v=-1$ channel are found to be much larger than those through $\Delta v=-2$ channel and, consequently, $\Delta v=-1$ channel decides the total vibrational predissociation rate. The predissociation rates of the states with van der Waals stretching mode excited are found to be larger than those of the states with bending mode excited, in general. The predissociation rates increase as the stretching motion ( $v_{1}$ ) of $I_{2}$ increases because the predissociation energy becomes smaller. regardless of $v_{2}$ or $v_{3}$. When van der Waals bending mode is excited, the predissociation rates decrease as $\nu_{3}$ increases. But the predissociation rates increase as the stretching motion ( $v_{2}$ ) between Ne and $\mathrm{I}_{2}$ increases.

Though a lot of infomation on the vibrational predissociation of $\mathrm{I}_{3}(B)-\mathrm{Ne}$ has been gathered, still a limited knowledge on rotational state distributions of product $\mathrm{I}_{2}$ has been obtained. Experimentally the rotational state distributions of $\mathrm{I}_{2}$ produced from the $\mathrm{I}_{2}(B)-\mathrm{Ne}(32,0.0),(33.0,0)$. or (35.0.0) predissociation are reported ${ }^{31}$ For instance, the predissociation through $\Delta v=-1$ chamel yields rotational state ( $j^{\prime}$ ) distribution of product $\mathrm{I}_{2}$ up to $j^{\prime}=17$. while the predissociation through $v=-2$ channel yields the distribution up to $j^{\prime}=43$. Theoretically a simple fact is known. i.e. the rotational distributions depend strongly on the van der Waals bending mode, while the stretching mode hardly changes the distributions. ${ }^{2+4}$
In this work we extensively investigate vibrational predissociation of $\mathrm{I}_{2}(B)-\mathrm{Ne}\left(v_{1}, v_{2}>0, v_{3}>0\right)$ in excited van der Waals modes using VSCF-DWB-IOS approximation. concentrating on the rotational state distributions of product $\mathrm{I}_{3}$. The details of the theoretical method have been reported already. ${ }^{18.19}$ In this method the predissociation is viewed as a half-collision process. Therefore we start our calculation to determine the vibrational wave functions of the bound $\mathrm{I}_{2}(B)$ Ne in electronically excited $B$ state. To have the bound state wave functions we employ the vibrational self-consistent field approximation (VSCF) of which validity is verified. The continuum state wave function of the dissociating $\mathrm{I}_{2}+$ Ne should also be evaluated and the infinite-order sudden (IOS) approximation is adopted for this purpose. Then the dissociation rate is evaluated using distorted-wave Born (DWB) approximation that is essentially identical with the well known Fermi's golden rule. This VSCF-DWB-IOS approximation has been found to produce total rates with reasonable accuracy. The quantities we calculated are the predissociation rates of the transient excited vibrational states of $\mathrm{I}_{2}(B)-\mathrm{Ne}\left(v_{1}, v_{2}>0 . v_{3}>0\right)$ and the rotational state distributions of the dissociation product $\mathrm{I}_{2}$.

## Summary of Theory

The vibrational predissociation of $\mathrm{AB}-\mathrm{C}$ can be viewed as the dissociation of triatomic complex $\mathrm{AB}-\mathrm{C}\left(v_{1}, v_{3}, v_{3}\right) \rightarrow$ diatomic molecule $\mathrm{AB}\left(v^{\prime}<v_{1}\right)$ and atom C. i.e., $\mathrm{AB}-\mathrm{C}\left(v_{1}\right.$. $\left.v_{2}, v_{3}\right) \mathrm{AB}\left(v^{\prime} \cdot j^{\prime}\right)+\mathrm{C} \cdot v_{1}$ is a quantum number for stretching vibration of $A B, v_{2}$ is for stretching van der Waals vibration of $C$ with respect to $A B, v$ is for bending vibration of $C$ with
respect to $\mathrm{AB}, v^{\prime}$ is a stretching vibrational quantum number of free AB , and $j^{\prime}$ is a rotational quantum number of free AB . In this work $A B$ corresponds to $I_{2}$ and $C$ to Ne . The VSCF-DWB-IOS approximate method for vibrational predissociation is summarized below. For details. please consult References 18 and 19.
The vector from the center of mass of the diatomic molecule AB to the atom C is denoted $\mathbf{R}$. The distance vector between the atoms $A$ and $B$ is $\mathbf{r}$, and the angle between $\mathbf{R}$ and $\mathbf{r}$ is $\theta$. The Schrödinger equation for the vibrational motion of AB-C complex can be written as

$$
\begin{equation*}
H(r, R . \theta) \Psi(r, R, \theta)=E \Psi(r, R . \theta) \tag{1}
\end{equation*}
$$

The reduced Hamiltonian is

$$
\begin{align*}
H(r, R . \theta)= & -\frac{1}{2 \mu_{1}} \frac{\partial^{2}}{\partial r^{2}}-\frac{1}{2 \mu_{2}} \frac{\partial^{2}}{\partial R^{2}}+\frac{\mathrm{j}^{2}}{2 \mu_{1} r^{2}}+\frac{\mathrm{l}^{2}}{2 \mu_{2} R^{2}} \\
& +V_{1}(r)+V_{2}(r, R, \theta) \tag{2}
\end{align*}
$$

where $\mu_{1}$ is the reduced mass of A and B , and $\mu_{2}$ is the reduced mass of diatomic molecule AB and atom $\mathrm{C} . V_{1}(r)$ is the potential energy function between A and B and $V_{2}(r . R$, $\theta$ ) is the rest of the total potential function. i.e.. van der Waals interaction $\mathbf{j}$ and $\mathbf{I}$ are the two angular momenta associated with $r$ and $R$. respectively. When $\mathbf{J}=\mathbf{j}+\mathbf{l}=0$.

$$
\begin{equation*}
\dot{j}^{-}={\mathbf{l}^{-}}^{-}=\frac{-1}{\sin \theta} \frac{\partial}{\partial \theta}\left(\sin \theta \frac{\partial}{\partial \theta}\right) \tag{3}
\end{equation*}
$$

The Schrödinger equation (1) is solved for a bound vibrational state $\mathrm{AB}-\mathrm{C}\left(v_{1}, v_{2} . v_{3}\right)$ by using vibrational selfconsistent field (VSCF) approximation. The initial (before dissociation) bound state wave function is approximated as,

$$
\begin{align*}
& \Psi_{r_{1}, v_{2}, r_{3}}^{j}(r, R, \theta) \neq \Psi_{r_{1}-v_{2}+r_{3}}^{S C^{\prime} F}(r, R, \theta) \\
& \approx \phi_{v_{1}}^{l_{1}}(r) \phi_{r_{2}}^{2}(R) \phi_{r_{3}}^{3_{3}}(\theta) \tag{4}
\end{align*}
$$

where

$$
\begin{align*}
& H^{S C F}(r, R . \theta) \Psi_{r_{r_{1}}, r_{2} \cdot v_{3}}^{S C F}(r, R . \theta) \\
& \quad=E_{r_{1}, v_{2}, v_{3}}^{S C F} \Psi_{r_{1}, v_{2}, v_{3}}^{S C F}(r, R, \theta)  \tag{5}\\
& H^{S C F}(r, R, \theta)=h_{1}(r)+h_{2}(R)+h_{3}(\theta)  \tag{6}\\
& h_{1}(r) \phi_{r_{1}}^{1}(r)=\varepsilon_{r_{1}}^{1} \phi_{r_{1}}^{1}(r)  \tag{7}\\
& h_{2}(R) \phi_{r_{2}}^{-}(R)=\varepsilon^{2}{ }_{r_{2}} \phi_{r_{2}}^{2}(R)  \tag{8}\\
& h_{3}(\theta) \phi_{r_{2}}^{3}(\theta)=\varepsilon_{r_{3}}^{3}{ }_{r_{3}} \phi_{r_{3}}^{3}(\theta) \tag{9}
\end{align*}
$$

$\varepsilon^{1}{ }_{r_{1},} \varepsilon_{r_{r_{2}}}^{2}$ and $\varepsilon^{3}{ }_{r_{3}}$ are modal eigenvalues for $A-B$ stretching. $\mathrm{AB}-\mathrm{C}$ van der Waals stretching. and $\mathrm{AB}-\mathrm{C}$ van der Waals bending motions, respectively. The detailed expressions for $H^{S C F}$ and $H_{r_{1}, v_{2}}^{S C F} v_{3}$ are not presented here for 18.19
brevity
18.19 brevity ${ }^{18.19}$

Now we determine a final continuum (or dissociating) state wave function. $\Psi_{r_{j}^{\prime}}^{f}(r, R . \theta)$. Here we use a vibrationally adiabatic approximation. which is

$$
\begin{equation*}
\Psi_{v^{\prime}, j^{\prime}}^{f}(r, R, \theta) \approx \phi_{\nu^{\prime}}^{d}(r) \phi_{j^{\prime}}^{E}(r, \theta) \tag{10}
\end{equation*}
$$

where $\phi_{v}^{d}(r)$ is the stretching vibrational wave function of the state $v^{\prime}$ of free AB . The continuum wave function $\phi_{j}^{E}(R$. $\theta$ ) consists of two parts: one is the rotational ( $j$ ) motion of AB and the other is a relative translational $(E)$ motion of AB with respect to C . The Schrödinger equation for $\phi_{j}^{E}(R, \theta)$ is

$$
\begin{gather*}
{\left[-\frac{1}{2 \mu_{2}} \frac{\partial^{2}}{\partial R^{2}}+\frac{1}{2 \mu_{2} R^{2}} 1^{2}+\left\langle\phi_{v^{\prime}}^{d}(r)\right| \frac{1}{2 \mu_{1} r^{2}}\left|\phi_{v^{\prime}}^{i}(r)\right\rangle \mathbf{j}^{2}\right.} \\
+\left\langle\phi_{\left.v^{\prime}(r)\left|V_{2}(r, R, \theta)\right| \phi_{1}^{d}(r)\right\rangle-}\right. \\
\left.\left(E_{v_{1}, v_{2}, v_{j}}^{i}-E_{v^{\prime}}^{d}\right)\right] \phi_{j}^{E}(R, \theta)=0 \tag{11}
\end{gather*}
$$

where $E_{r^{d}}^{d}$ is the $v^{\prime}$ vibrational energy of free AB .
Under IOS. we set $\mathrm{j}^{-}=\mathrm{I}^{2}=j^{\prime}\left(j^{\prime}+1\right)$ because the total angular momentum is fixed as zero. then the scattering equation we have to solve is one-dimensional, i.e..

$$
\begin{gather*}
{\left[-\frac{1}{2 \mu_{2}} \frac{\partial^{2}}{\partial R^{2}}+\frac{1}{2 \mu_{2} R^{2}} j^{\prime}\left(j^{\prime}+1\right)+B j^{\prime}\left(j^{\prime}+1\right)\right.} \\
\left.+\bar{V}_{2}(R ; \theta)-E\right] \phi_{j^{E}}^{E}(R: \theta)=0 \tag{12}
\end{gather*}
$$

where $B$ is a rotational constant of AB at the state $v^{\prime}$ [the third term in Eq. (11)]. $\bar{V}(R: \theta)$ is the averaged $V$ integral over $\phi_{1,}^{d}(r)$ [the fourth term in Eq. (11)] $E$ is the translational energy which is $E_{r_{1}, v_{2}, r_{3}}^{d}-E_{l^{2}}^{a}$. and $E_{j}^{E}(R: \theta)$ parametrically depends on angle $\theta$.

The dissociation process is assumed to be due to mode-mode coupling which causes energy transfer (and predissociation) from vibrational motion of $\mathrm{AB}-\mathrm{C}$ to kinetic motion of C (V $\rightarrow \mathrm{T}$ ). The coupling, $V_{c}\left(=H-H^{\text {CFF }}\right)$ is generally so weak that a perturbative approach could be suitable (DWB approximation). The vibrational predissociation rate R is. when the energy nomalized continum wave function $\Psi_{r^{\prime} j^{\prime}}^{\prime}(r . R . \theta)$ is used.

$$
\begin{align*}
& \mathrm{R}\left(v_{1} v_{2} v_{3} \rightarrow v_{j}^{\prime \prime}\right)= \\
& \quad 2 \pi\langle | \Psi_{v_{j}^{\prime}}^{\prime}(r, R, \theta)\left|V_{c}\right| \Psi_{v_{1}, v_{2}, v_{s}}^{\prime}(r, R, \theta)| \rangle^{2} \tag{13}
\end{align*}
$$

The rotational state population $\left.P\left(v_{1}\right)_{2} v_{3} \rightarrow v_{j}^{\prime}\right)$, in units of $\%$, of $\mathrm{AB}\left(v^{\prime}, j\right)$ from $\mathrm{AB}-\mathrm{C}\left(v_{1}, v_{2} v_{3}\right)$ is.

$$
\begin{align*}
& P\left(v_{1} v_{2} v_{3} \rightarrow v^{\prime} j^{\prime}\right)= \\
& \quad \mathrm{R}\left(v_{1} v_{2} v_{3} \rightarrow v^{\prime} j^{\prime}\right) / \sum_{j} \mathrm{R}\left(v_{1} v_{2} v_{3} \rightarrow v^{\prime} j^{\prime}\right) \times 100 \tag{14}
\end{align*}
$$

The total predissociation rate $\mathrm{R}\left(v_{1} v_{-} v_{3}\right)$ from $\mathrm{AB}-\mathrm{C}\left(v_{1}, v_{2}\right.$ $\left.v_{3}\right)$ to $\mathrm{AB}\left(v^{\prime}, j^{\prime}\right)+\mathrm{C}$ is

$$
\begin{equation*}
\mathrm{R}\left(v_{1} v_{2} v_{3}\right)=\sum_{v} \sum_{j} \mathrm{R}\left(v_{1} v_{2} v_{3} \rightarrow v_{j}^{\prime}\right) \tag{15}
\end{equation*}
$$

## Computations and Results

The best known potential energy function for $\mathrm{I}_{-}(B)$-Ne is

$$
\begin{equation*}
V(r, R, \theta)=V_{\mathrm{I}-\mathrm{I}}(r)+2 V_{\mathrm{I}-\mathrm{Ki}}(r, R, \theta)+C\left(v_{1}\right) \tag{16}
\end{equation*}
$$

The analytical form of I-I potential function for $\mathrm{I}_{-}(B)$. $V_{\mathrm{I}-\mathrm{I}}(\rho)$
is obtained from the Gruebele and Zwail's experiment. ${ }^{13.17}$ García-Vela ${ }^{14}$ suggested a new Morse type potential function for $\mathrm{I}-\mathrm{Ne}, V_{\mathrm{I} . \mathrm{Ne}}(r, R, \theta)$ in which parameters are fitted to the experimental dissociation energy of $\mathrm{I}_{2}(B)-\mathrm{Ne}(34,0,0)$. The extra term $C\left(w_{1}\right)$, which depends on the I-I stretching vibrational motion, is introduced to exactly reproduce both experimental dissociation energies of $\mathrm{I}_{2}(B)-\mathrm{Ne}(0.0,0)$ and $\mathrm{I}_{2}(B)-\mathrm{Ne}(34,0.0)$ simultaneously ${ }^{2+}$ The potential energy function produces the equilibrium geometry of $\mathrm{I}_{2}(B)-\mathrm{Ne}$ as T-shaped which is experimentally found in Burroughs et $a l$ 's experiment. ${ }^{2(1)}$ From now on $\mathrm{I}_{2}(B)-\mathrm{Ne}\left(v_{1}, v_{2}, v_{3}\right)$ is briefly written as $\mathrm{I}_{2}-\mathrm{Ne}\left(v_{1}, v_{2}, v_{3}\right)$ or $\left(v_{1}, v_{2}, v_{3}\right)$.

The vibrational state energies of $\mathrm{I}_{2}-\mathrm{Ne}\left(v_{1}, v_{2}, v_{3}\right)$ are calculated using the suggested VSCF method where relevant equations (Eqs. 7. 8, and 9) are numerically and iteratively solved. For the $\mathbf{r}$ coordinate. the numerical integration was perfonmed with the grid size of 0.001 au from $r=4.5$ to 15 au. For the $\mathbf{R}$, the grid size is 0.05 au from $R=5$ to 40 au . It guarantees that the starting point of integration is well inside the classically forbidden region and at a large distance. the bound state wave function converges to zero and the continum wave function becomes a plane wave, i.e., free from the interaction. For the angle $(\theta)$ variable. the discrete variable representation is adopted and the 100 Legendre functions, that is. 100 grid points are used. The 127 amu isotope of I and the 20 amu Ne are assumed. With the same numerical quadrature the dissociating state wave functions are calculated. The vibrational wave functions of free $\mathrm{I}_{2}$ are numerically solved and the continum wave function of outgoing product $\mathrm{I}_{2}$ has been determined using the IOS approximation (Eq. 12). The Eq. 12 is solved repeatedly at 100 angles. Under the DWB approximation. the predissociation rates of $I_{2}-\mathrm{Ne}\left(v_{1}, v_{3} . v_{3}\right)$ and the rotational state distributions of $I_{2}\left(v^{\prime} . j\right)$ are evaluated using Eqs. 13 and 14 .

The vibrational energy levels of $\mathrm{I}_{2}-\mathrm{Ne}\left(v_{1}, v_{2}, v_{3}\right)$ are well studied previously ${ }^{2+}$ The level structures are, in general. ( $v_{1}$, $0.0)<\left(v_{1} .0 .1\right)<\left(v_{1}, 0,2\right)<\left(v_{1}, 1,0\right)<\left(v_{1}, 0,3\right)<\left(v_{1}, 1.1\right)$ $<\left(v_{1} .1 .2\right)<\left(v_{1} .2 .0\right)<\left(v_{1} .1,3\right)<\left(v_{1}, 2,1\right)<\left(v_{1}, 2.2\right)$ in the order of increasing energies. Of course the vibrational energy levels of $\mathrm{I}_{2}\left(v^{\prime}, j^{\prime}=0\right)$ are almost exactly known. ${ }^{12}$ The predissociation can be viewed as the reaction of $\mathrm{I}_{2}-\mathrm{Ne}\left(v_{1}, v_{2}\right.$ $\left.v_{3}\right) \rightarrow \mathrm{I}_{2}\left(v^{\prime}, j^{\prime}\right)+\mathrm{Ne}$. When $\Delta v\left(=v^{\prime}-v_{1}\right)=-1$, it is called the $\Delta v=-1$ process (or chamel). And the $\Delta v=-2$ channel when $\Delta v=-2$. etc. The reaction energy for the dissociation can be called the predissociation energy PE that is equal to Energy $\left[\mathrm{I}_{2}-\mathrm{Ne}\left(v_{1}, v_{3}, v_{3}\right)\right]$ - Energy $\left[\mathrm{I}_{2}\left(v^{\prime}, j^{\prime}=0\right)\right]$. When PE are positive, the dissociation occurs spontaneously.

As mentioned in the Introduction section, the studies on predissociation dissociation of $\mathrm{I}_{2}-\mathrm{Ne}\left(v_{1}, 0,0\right)$ have been reported by many authors. In Table 1. the predissociation rates (Rates) and predissociation energies (PE) of $\mathrm{I}_{2}-\mathrm{Ne}\left(v_{1}\right.$. 0.0 ) through $\Delta v=-1$ channel are listed. From the Table 1 , we see that the vibrational predissociation rates of ( $v_{1}, 0.0$ ) increase as $v_{1}$ increases (energy gap law), which is consistent with previous studies. The energy gap law is due to the fact that the PE decreases as $v_{1}$ increases. As $v_{1}$ becomes larger. the level gap between adjacent two $v_{1}$ levels of $I_{2}$ in $I_{2}-\mathrm{Ne}$

Table 1. Vibrational predissociation rates (Rates in $10^{2 \prime} \mathrm{~s}^{-1}$ ). predissociation energies ( PL in $\mathrm{cm}^{1}$ ). and rotational constants of $]_{2}\left(v_{1}-1\right)\left(B\left(v_{1}-1\right)\right.$ in $\left.\mathrm{cm}^{-1}\right)$ from $\mathrm{I}_{2}-\mathrm{Ve}\left(v_{1} .0 .0\right) \quad>\mathrm{I}_{2}\left(v_{1}-1 . j^{\prime}\right)+\mathrm{Ne}$. In rotational state distributions of product $\mathrm{I}_{2}\left(v_{l}-1 . j^{*}\right)$ three characteristic


| $v_{1}$ | Rates | PE | $B\left(w_{1}-1\right)$ | j'krema | $i^{\prime \prime}$ mas | $j_{\text {frech }}^{\prime \prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.28 | 59.54 | 0.0289 | 44 | 38 | 20 |
| 5 | 1.01 | 54.18 | 0.0283 | 42 | 38 | 20 |
| 10 | 2.73 | 46.88 | 0.0275 | 40 | 36 | 20 |
| 15 | 5.74 | 39.00 | 0.0265 | 36 | 34 | 18 |
| 20 | 12.95 | 30.61 | 0.0255 | 34 | 30 | 18 |
| 23 | 18.52 | 25.36 | 0.0248 | 32 | 28 | 2 |
| 26 | 37.56 | 20.00 | 0.0241 | 26 | 26 | 2 |
| 29 | 51.83 | 14.54 | 0.02 .33 | 24 | 22 | 2 |
| 33 | 109.77 | 7.20 | 0.0225 | 18 | 18 | 2 |
| 34 | 122.33 | 5.35 | 0.0220 | 14 | 14 | 2 |
| 36 | 178.25 | 1.69 | 0.0214 | 8 | 8 | 2 |
| 37 | closed | -0.14 | - | - | - | - |

becomes smaller. And it makes the energy difference between $\mathrm{I}_{2}-\mathrm{Ne}\left(v_{1}, 0,0\right)$ and free $\mathrm{I}_{2}\left(v_{1}-1\right)$ smaller so that the dissociation from $\mathrm{l}_{2}-\mathrm{Ne}$ to $\mathrm{I}_{2}-\mathrm{Ne}$ becomes faster. The Pए, for $l_{2}-\mathrm{Ne}(37,0,0)$ in Table 1 is negative so that the predissociation through $\Delta v=-1$ channel should not occur for $\mathrm{I}_{2}-\mathrm{Ne}(37,0,0)$, which is consistent with experimental finding. ${ }^{2.20}$ Our calculated rotational constants of $l_{2}$ at various vibrational levels, i.e., $B\left(v_{1}-1\right)$, are also listed in Table 1. The rotational constant becomes smaller as $v_{1}$ increases. It reflects that the bond length becomes longer as $1_{2}$ has larger vibrational energy.
The largest rotational energy that product $I_{2}$ can have, of course, is equal to the predissociation energy PD. This rotational state is denoted as a quantum number $j^{\prime}$ 'cerstw in Table 1. The $j^{\prime}$ hateses is the largest integer that satisfies the relation, i.e., $B\left(v_{1}-1\right)^{*} j^{\prime}$ 'urverer ${ }^{*}\left(j^{\prime}\right.$ 'arovess +1$) \leq \mathrm{PD}$. Since theoretical calculations enable one to calculate the $B\left(v_{1}-1\right)$ and PE, we could determine $j^{\prime}$ arpert. As shown in Figure I, the rotational state distributions of $I_{2}$ end at a certain rotational quantum number ( $j^{\prime}$ ниr $)$. (The criterion to choose $j^{\prime}$, mse is that the total population (\%) of all rotational states whose rotational quauntum number is larger than $j^{\prime}$ metr should be smaller than $0.01 \%$.) The $j^{\prime \prime}$ man are listed in Table I. Of course the $j_{\text {mptr }}^{\prime}$ are the highest rotational state that $l_{2}$ can
 is found that $j^{\prime}$ mese are, in most cases, smaller than $j^{\prime}$ lumswer It is due to a dynamical effect, e.g., the overlap between the bound state wave function and the dissociating state wave
 That is, $I_{2}$ produced from the predissociation of higher $v_{1}$ states of $I_{2}-\mathrm{Ne}\left(v_{1}, 0,0\right)$ has less rotational energy, i.e., rotates slowly.
Heaven and coworkers ${ }^{20}$ experimentally determined that the $j^{\prime} w_{k}, v$ of $\mathrm{I}_{2}\left(v^{\prime}=31, j^{\prime}\right)$ produced from the predissociation of $\mathrm{I}_{2}-\mathrm{Ne}(32,0.0)$ is 17 and its recoil energy is $2.6 \mathrm{~cm}^{-1}$. In Table 1 we see that our calculated $j^{\prime}$ man is 18 . Odd or even number of rotational quantum number is not a matter of


Figure 1. Rotational state distributions of $I_{2}\left(v_{1}-1\right.$. $j^{\prime}$ ) from $I_{2}-$ $\mathrm{Ne}\left(v_{1}, 0.0\right) \rightarrow I_{2}\left(v_{1}-I . j\right)+\mathrm{Ne}$ where $v_{1}=5.10 .20$. or 30 .
concern but rather it is a matter of choice because $I_{2}$ is homonuclear. Our value of 18 corresponds to 17 if odd number was chosen. Then our calculated recoil energy is PE $B^{*} j_{\text {mas }}^{\prime} *\left(j_{\operatorname{man}}^{\prime}-1\right)$, i.e., $9.04-0.0225^{*} 17^{*}(17+1)=2.16 \mathrm{~cm}^{-1}$ that is comparable to experimental value of $2.6 \mathrm{~cm}^{-1}$. GarcíaVela's wave packet calculations ${ }^{1+}$ also showed $j^{\prime}$ men is 18 . Here theory and experiment agree to each other very well.

In Figure 1, the rotational state distributions of $\mathrm{I}_{2}\left(v_{1}-1, j\right)$ produced from the vibrational predissociation reaction of $I_{2}-$ $\mathrm{Ne}\left(v_{1}, 0,0\right) \rightarrow \mathrm{I}_{2}\left(v_{1}-1, j^{\prime}\right)+\mathrm{Ne}\left(v_{1}=5,10,20\right.$, and 30$)$ are presented. As we see in all cases, the distributions exhibit two distinct maximum peaks, i.e. bimodal. This bimodal structure appearing in vibrational predissociation of triatomic complexes was well analyzed by Lee using the concept of angle functions. ${ }^{25.26}$ We do not repeat the analysis here but want to stress that the angle $(\theta)$ dependence of the first derivative of the potential energy function (between $\mathrm{I}_{2}$ and Ne ) plays a key role in rotational state distributions of product $I_{2}$,

The rotational quantum number of the larger peak among the two maxima in rotational state distributions of $\mathrm{I}_{2}$ is denoted as $j_{p \text { pech. }}^{\prime}$. From Figure I, we note that the $j_{p_{0}^{\prime}, 0, k}^{\prime}$ is 20 from $(5,0,0), 20$ from $(10,0,0), 18$ from $(20,0,0)$, and 2 from ( $30,0,0$ ). We also see that the peak at small $j^{\prime}$ becomes larger and larger as $v_{1}$ increases from $v_{l}=5$ to 30 . And at $v_{1}=30$, the peak at small $j^{\prime}(=2)$ is eventually larger than the peak at large $j^{\prime}(=18)$. This observation can be expained in three folds. i) The predissociation reaction energy PE decreases as $v_{1}$ increases. Consequently the energy that the product $I_{2}$ can carry becomes smaller so that the rotational energy of $\mathrm{I}_{2}$ becomes naturally smaller. ii) Furthermore, the predissociation rate increases as $v_{1}$ increases. At high $v_{1}$, the dissociation occurs so fast that the orientation of the leaving $\mathrm{I}_{2}$ is not much different from that in the complex $\mathrm{I}_{2}-\mathrm{Ne}$ where the total rotational motion $(J)$ is zero. iii) Finally, based on Lee's analysis, ${ }^{3}$ the effective potential (averaged over the 1-1 distance coordinate $r$ ) that governs the dissociation becomes smoother as $v_{1}$ increases. Therefore the anisotropy of potential decreases, i.e., the potential becomes shallow over the angle


Figure 2. Rotational state distributions of $I_{2}\left(19 . j^{\prime}\right)$ from $I_{2}-$ $\mathrm{Ve}\left(20 . v_{2}, v_{\mathrm{i}}\right), \mathrm{I}_{2}\left(19 . j^{\prime}\right)+\mathrm{Ne}$ where $\left(v_{1}, v_{2} \cdot v_{3}\right)=(20.0 .0)$. (20.0. 1). or (20.0.2).


Figure 3. Rotational state distributions of $\mathrm{I}_{2}(19 . j)$ from $\mathrm{I}_{2}-$ $\mathrm{Ne}_{\mathrm{e}}\left(20, v_{2}, v_{3}\right) \rightarrow \mathrm{I}_{2}\left(19, j^{\prime}\right)$ । Ne where $\left(v_{1}, v_{2}, v_{3}\right)=(20,1,0)$, (20, l . 1). or (20. 1. 2).
coordinate $\theta$. It, of course, does not alter the rotational motion of the leaving $I_{2}$ significantly. The $j_{j}^{\prime}$ perd from various $\mathrm{I}_{2}-\mathrm{Ne}\left(y_{1}, 0,0\right)$ states are listed in Table 1.
The rotational state distributions of $\mathrm{I}_{2}\left(v^{\prime}=19, j^{\prime}\right)$ produced from the presissociation of various ( $20, v_{2}, v_{3}$ ) states are presented in Figures 2, 3, and 4. Again they exhibit the bimoal structures. We note that the distribution from $(20,0,0)$ is almost identical with that from $(20,1,0)$ or $(20,2,0)$. The same is true for the case from $(20,0,1)$ ) $(20,1,1) /(20,2,1)$ or $(20,0,2) /(20,1,2)(20,2,2)$. From this we learn that the change in van der Waals stretching mode does not alter the rotational state distributions of product $I_{2}$, as expected. But the change in bending mode drastically changes the distributions. For example, see the $(20,0,0)$. $(20,0,1)$ and ( $20,0,2$ ) distributions in Figure 2. The states in higher bending mode produce more rotationally hot $I_{2}$ diatomic molecules. That is, the maximum peak ( $j^{\prime}{ }^{\prime}$ colk $)$ appears at a higher rotational quantum number of $\mathrm{I}_{2}$. Naturally the large bending motion of Ne with respect


Figure 4. Rotational state distributions of $\mathrm{I}_{2}\left(19 . j^{\prime}\right)$ from $\mathrm{I}_{2}-$ $N c\left(20 . v_{2} . v_{3}\right) \times I_{-}(19 . j)-\operatorname{Ni}$ where $\left(v_{1} \cdot v_{2} \cdot v_{3}\right)=(20.2 .0) .(20.2$. 1). or (20. 2, 2).

Table 2. The $j_{p}^{\prime}$, , in rotational state distributions of product $\mathrm{I}_{2}\left(v_{1}-\right.$ 1) from $\mathrm{I}_{2}-\mathrm{Ne}\left(v_{1} . v_{2} \cdot v_{3}\right) \rightarrow \mathrm{I}_{2}\left(v_{1}-\mathrm{I}, j^{\prime}\right)-\mathrm{Ne}$

| $v_{1}$ | $\left(v_{1} 0.1\right)\left(v_{1} 0.2\right)\left(v_{1}, 1.0\right)\left(v_{1}, 1,1\right)\left(v_{1}, 1,2\right)\left(v_{1}, 20\right)\left(v_{1}, 2,1\right)\left(v_{1}, 2,2\right)$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 27 | 30 | 20 | 27 | 30 | 22 | 27 | 32 |
| 5 | 27 | 30 | 20 | 27 | 30 | 22 | 27 | 32 |
| 10 | 25 | 30 | 20 | 27 | 30 | 20 | 27 | 32 |
| 15 | 25 | 28 | 18 | 25 | 30 | 18 | 25 | 30 |
| 20 | 23 | 28 | 18 | 23 | 30 | 18 | 25 | 30 |
| 23 | 23 | 28 | 16 | 23 | 28 | 16 | 23 | 30 |
| 26 | 21 | 26 | 2 | 21 | 28 | 14 | 21 | 28 |
| 29 | 21 | 26 | 2 | 21 | 26 | 14 | 21 | 12 |
| 34 | 9 | 12 | 2 | 19 | 12 | 2 | 19 | 12 |
| 36 | 9 | 12 | 2 | 19 | 12 | 2 | 19 | 12 |
| 37 | 9 | 12 | 2 | 19 | 12 | 2 | 19 | 12 |
| 40 | 9 | 12 | 2 | 15 | 12 | 2 | 19 | 12 |
| 43 | closed | 12 | 2 | 11 | 12 | 2 | 17 | 12 |

to $I_{2}$ should bring about the high rotational motion of $I_{2}$.
We find the same trend in rotational state distributions of $\mathrm{l}_{2}$ from other van der Waals excited states of $\mathrm{l}_{2}-\mathrm{Ne}\left(v_{1}, \nu_{2}>\right.$ $0, v>0$ ) as listed in Table 2. As $v_{1}$ increases, the $j j^{\prime},{ }^{\prime}, k, k$ excited ( $v_{1}, v_{2}>0, v_{3}>0$ ) state decreases as the $j_{p}^{\prime}$ perak from ( $v_{1}, 0,0$ ) does. That is, the diatomic molecule $I_{2}$ produced from the predissociation of high ( $v$, is large) vibrational state is mostly in low rotational state.

So far our discussion is limited to the $\Delta v=-1$ channel, i.e.., $\mathrm{I}_{2}-\mathrm{Ne}\left(v_{1}, v_{2}, v_{3}\right) \rightarrow \mathrm{I}_{2}\left(v_{1}-1, j^{\prime}\right)+\mathrm{Ne}$. We have performed the same calculations for other channels, i.e., $\Delta v=-2$, and -3 . etc. It is found that the rotational state distributions of product $I_{2}$ through $\Delta v=-1$ channel are notably different from those through $\Delta v=-2$ channel. ${ }^{[4.24}$ But, here we do not present analyses on the distributions through higher channels because the $\Delta v=-2$ or up channels do not contribute much to the total predissociation rate. The predissociation rates for $\Delta v=-2$ are one or two orders of magnitude smaller than the $\Delta v=-1$, and the $\Delta v=-3$ rates are even smaller than the $\Delta v=-2 .^{24}$

## Summary and Conclusion

The direct vibrational predissociation of $\mathrm{I}_{2}(B)-\mathrm{Ne}\left(v_{1} . v_{3}, v_{3}\right)$ in ground and excited vibrational states has been theoretically investigated by using the fast and simple quantum mechanical VSCF-DWB-IOS method. The work concentrated on the rotational state distributions of $\mathrm{I}_{2}$ produced from various $\left(v_{1}, v_{3}, v_{3}\right)$ states. The summary of the work is as follows:
i) The vibrational levels of $\mathrm{I}_{3}(B)$ - $\mathrm{Ne}\left(v_{1}, v_{,}, v_{3}\right)$ are determined. The level structures are. in general. $\left(v_{1}, 0.0\right)<\left(v_{1}, 0.1\right)<$ $\left(v_{1} .0 .2\right)<\left(v_{1}, 1.0\right)<\left(v_{1}, 0.3\right)<\left(v_{1} .1,1\right)<\left(v_{1} .1 .2\right)<\left(v_{1}, 2.0\right)$ $<\left(v_{1}, 1.3\right)<\left(v_{1}, 2.1\right)<\left(v_{1} .2 .2\right)$ in the order of increasing energies. ii) The predissociation rates increase as the stretching motion ( $v_{1}$ ) of $\mathrm{I}_{2}$ increases. regardless of $v_{2}$ or $v_{3}$ (energy gap law). A similar energy gap law is found when the van der Waals bending motion changes, i.e.. the predissociation rates decrease as the van der Waals bending motion ( $v_{3}$ ) increases. But the predissociation rates increase as the van der Waals stretching motion ( $v$ ) between Ne and $\mathrm{I}_{2}$ increases. iii) The rotational state distributions of $\mathrm{I}_{2}$ produced from the vibrational predissociation of $\mathrm{I}_{2}-\mathrm{Ne}$ exhibit two distinct maximum peaks, i.e bimodal.

The above three fundings have been reported before and we verified them in this work. The new furdings are: iv) The change in van der Waals stretching mode does not alter the rotational state distributions of product $\mathrm{I}_{3}$. But the change in bending mode drastically changes the distributions. v) The maximum peak in rotational state distributions of product $\mathrm{I}_{2}$ moves to a lower rotational quantum number region as $v_{1}$ increases. That is, the $I_{2}$ produced from the predissociation of $\mathrm{I}_{3}(B)-\mathrm{Ne}\left(v_{1}, v_{2}, v_{3}\right)$ at high ( $v_{1}$ is large) vibrational state carries very little rotational energy.
The advantage of the proposed method lies in capability of exactly locating the transient complex's ( $\mathrm{I}_{2}(B)-\mathrm{Ne}$ in this work) vibrational level. It enables one to easily study the vibrational predissociation of the complex in vibrationally excited van der Waals mode that can not be easily investigated by using other theoretical methods.

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