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# A Solid State Controller for Self-Excited Induction Generator for Voltage Regulation, Harmonic Compensation and Load Balancing

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#### **ABSTRACT**

This paper deals with the performance analysis of static compensator (STATCOM) based voltage regulator for self-excited induction generators (SEIGs) supplying balanced/unbalanced and linear/ non-linear loads. In practice, most of the loads are linear. But the presence of non-linear loads in some applications injects harmonics into the generating system. Because an SEIG is a weak isolated system, these harmonics have a great effect on its performance. Additionally, SEIG's offer poor voltage regulation and require an adjustable reactive power source to maintain a constant terminal voltage under a varying load. A three-phase insulated gate bipolar transistor (IGBT) based current controlled voltage source inverter (CC-VSI) known as STATCOM is used for harmonic elimination. It also provides the required reactive power an SEIG needs to maintain a constant terminal voltage under varying loads. A dynamic model of an SEIG-STATCOM system with the ability to simulate varying loads has been developed using a stationary d-q axes reference frame. This enables us to predict the behavior of the system under transient conditions. The simulated results show that by using a STATCOM based voltage regulator the SEIG terminal voltage can be maintained constant and free from harmonics under linear/non linear and balanced/unbalanced loads.

**Keywords:** Self-excited induction generator, static compensator, voltage regulation, load balancing, harmonic elimination.

#### 1. Introduction

Due to global environmental concern, increased emphasis is being given to non-conventional energy sources to provide electricity. These non-conventional energy sources have great potential to act as prime movers for the generating systems. An externally driven induction machine operates as a self-excited induction generator (SEIG), with its excitation requirements being met by a capacitor bank connected across its terminals. The SEIG has advantages [1] like simplicity, being maintenance free, absence of DC, being brushless, etc. as compared to a conventional synchronous generator.

Considerable literature exists on steady state and transient analysis of SEIG's under balanced/unbalanced resistive, reactive and motor loads<sup>[1-5]</sup>. In<sup>[3-5]</sup> d-q axes modeling is reported for the transient analysis of an SEIG.

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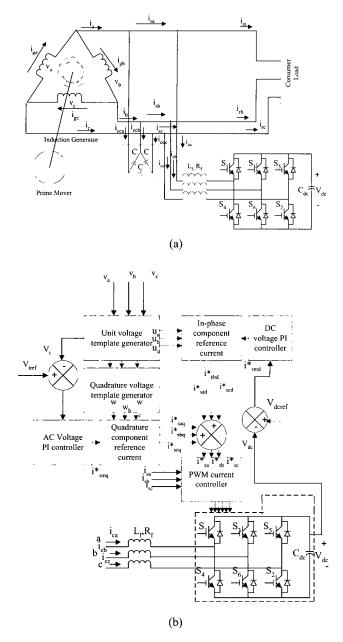


Fig. 1 Schematic Diagram of SEIG-STATCOM

Wang and Deng<sup>[6]</sup> have presented the transient performance of an SEIG under an unbalanced excitation system. Jain et al. <sup>[7]</sup> have given a generalized model for the transient analysis of an SEIG under symmetrical and asymmetrical conditions.

A major disadvantage of an SEIG is its poor voltage regulation. It requires a variable capacitance bank to maintain constant terminal voltage under varying loads. Attempts have been made to maintain constant terminal voltage using fixed capacitor and thyristor controlled

reactors (TCR)<sup>[8]</sup>, saturable-core reactors<sup>[9]</sup> and short-shunt connections<sup>[10]</sup>. The voltage regulation provided by these schemes is discrete but these inject harmonics into the generating system. However, with the invention of solid-state commutating devices, it is possible to make a static, noiseless voltage regulator which is able to regulate continuously variable reactive power to keep the terminal voltage of an SEIG constant under varying loads. This system, called STATCOM, has specific benefits compared to conventional SVC's<sup>[11]</sup>. Schauder and Mehta<sup>[12]</sup> have derived governing equations of STATCOM to determine its response to negative sequences and harmonic voltage components in the transmission line.

Singh and Shilpakar <sup>[13]</sup> have proposed an analysis of a solid-state voltage regulator for an SEIG with balanced loads. Miranda et al. <sup>[14]</sup> have proposed a static VAR compensator for an electrical pumping system driven by an induction generator. Kuo and Wang [15], [16] have described a method of voltage control of an SEIG under non-linear loads.

In general, electrical loads are linear in nature. However, due to the extensive use of solid-state controllers in different appliances, they draw harmonic current from AC sources and behave as non-linear loads. Adjustable speed drives used in pumps, compressors, airconditioner and other domestic appliances such as TV's, computers, SMPS's, and UPS's consist of either threephase or single-phase rectifiers at the front-end. These non-linear loads draw non-sinusoidal currents from the generating system, therefore injecting harmonics into the system. An SEIG is an isolated system, which is small in size, and the injected harmonics pollute the generated voltage. The STATCOM eliminates the harmonics, provides load balancing and supplies the required reactive power to the load and the generator. In this paper, the authors present a simple mathematical model for the transient analysis of the SEIG-STATCOM system under balanced/unbalanced, linear/non-linear loads (R, R-L and rectifier with capacitor filter and R load). Simulated results show that the SEIG-STATCOM system behaves as an ideal generating system under these conditions.

#### 2. System Configuration and Control Scheme

The schematic diagram of an SEIG with excitation

capacitor, STATCOM, load and control scheme is shown in Fig.1. Excitation capacitors are selected such that the SEIG generates rated voltage at rated speed under no load. The additional demand for reactive power is fulfilled using the STATCOM under varying loads. The STATCOM acts as a source of lagging or leading current to maintain the constant terminal voltage despite variations in load. The STATCOM consists of a three-phase IGBT based current controlled voltage source inverter, a DC bus capacitor and AC inductors. The output of the inverter is connected through the AC filtering inductor to the SEIG terminals. The DC bus capacitor is used as an energy storage device and provides the self-supporting DC bus of the STATCOM.

The control technique is used to regulate the terminal voltage of the SEIG is based on the generation of source currents. (They have two components, in-phase and quadrature, with AC voltage.) The in-phase unit vectors (u<sub>a</sub>, u<sub>b</sub> and u<sub>c</sub>) are three-phase sinusoidal functions, computed by dividing the AC voltages v<sub>a</sub>, v<sub>b</sub> and v<sub>c</sub> by their amplitude V<sub>t</sub>. Another set of quadrature unit vectors (wa, wb and wc) are sinusoidal functions obtained from inphase vectors (u<sub>a</sub>, u<sub>b</sub> and u<sub>c</sub>). To regulate the AC terminal voltage (V<sub>t</sub>), it is sensed and compared with the reference voltage. The voltage error is processed in the PI controller. The output of the PI controller  $(I_{smq}^*)$  for the AC voltage control loop determines the amplitude of the reactive current to be generated by the STATCOM. Multiplication of quadrature unit vectors (wa, wb and wc) with the output of the PI based AC voltage controller (I<sub>smq</sub>\*) yields the quadrature component of the reference source currents (i<sub>saq</sub>\*, i<sub>sbq</sub>\* and i<sub>scq</sub>\*). To provide a self-supporting DC bus for STATCOM, its DC bus voltage is sensed and compared with the DC reference voltage. The error voltage is processed in another PI controller. The output of the PI controller (I<sub>smd</sub>\*) determines the amplitude of the active current. Multiplication of in-phase unit vectors (ua, u<sub>b</sub> and u<sub>c</sub>) with the output of the PI controller (I<sub>smd</sub>\*) yields the in-phase component of the reference source currents (i<sub>sad</sub>\*, i<sub>sbd</sub>\*and i<sub>scd</sub>\*). The instantaneous sum of quadrature and in-phase components gives the reference source currents (isa\*, isb\* and isc\*), which are compared with the sensed line current (isa, isb and isc). These current error signals are amplified and compared with the triangular carrier wave. If the amplified current error signal is equal

to or greater than the triangular carrier wave, the lower device of the inverter phase is turned on and the upper device turned off. If the amplified current error signal is equal to or less than the triangular carrier wave the lower device of the inverter phase is turned off and the upper device turned on.

A non-linear load draws non-sinusoidal currents which causes harmonics to be injected into the generating system. Under unbalanced load conditions, SEIG currents may be unbalanced which may cause the machine to be derated. STATCOM is able to filter out the harmonics and balance the unbalanced load resulting in balanced and sinusoidal currents and voltages in the generator.

#### 3. Modeling of SEIG-STATCOM System

The mathematical model of the SEIG-STATCOM system contains the modeling of an SEIG and STATCOM as follows.

#### 3.1 Modeling of control scheme of STATCOM

Different components of the SEIG-STATCOM system shown in Fig. 1 are modeled as follows.

From the three-phase voltages at the SEIG terminals ( $v_a$ ,  $v_b$  and  $v_c$ ), their amplitude ( $V_t$ ) is computed as:

$$V_{t} = \{ (2/3) (v_{a}^{2} + v_{b}^{2} + v_{c}^{2}) \}^{1/2}$$
 (1)

It (V<sub>t</sub>) is filtered to eliminate ripples if there are any present.

The unit vector in phase with  $v_a$ ,  $v_b$  and  $v_c$  are derived as:

$$u_a = v_a/V_t; \quad u_b = v_b/V_t \quad ; \quad u_c = v_c/V_t$$
 (2)

The unit vectors in quadrature with  $v_a$ ,  $v_b$  and  $v_c$  may be derived using a quadrature transformation of the in-phase unit vectors  $u_a$ ,  $u_b$  and  $u_c$  as:

$$w_a = -u_b / \sqrt{3} + u_c / \sqrt{3}$$
 (3)

$$w_b = \sqrt{3} u_a / 2 + (u_b - u_c) / 2\sqrt{3}$$
 (4)

$$w_c = -\sqrt{3} u_a / 2 + (u_b - u_c) / 2\sqrt{3}$$
 (5)

### 3.1.1 Quadrature component of reference source currents

The AC voltage error  $V_{er(n)}$  at the  $n^{th}$  sampling instant is:

$$V_{er(n)} = V_{tref(n)} - V_{t(n)}$$
(6)

where  $V_{tref(n)}$  is the amplitude of the reference AC terminal voltage and  $V_{t(n)}$  is the amplitude of the sensed three-phase AC voltage at the SEIG terminals at the  $n^{th}$  instant. The output of the PI controller  $(I^*_{smq(n)})$  for maintaining constant AC terminal voltage at the  $n^{th}$  sampling instant is expressed as:

$$I*_{smq(n)} = I*_{smq(n-1)} + K_{pa} \{ V_{er(n)} - V_{er(n-1)} \} + K_{ia} V_{er(n)} (7)$$

where  $K_{pa}$  and  $K_{ia}$  are the proportional and integral gain constants of the proportional integral (PI) controller.  $V_{er\,(n)}$  and  $V_{er(n-1)}$  are the voltage errors at the  $n^{th}$  and  $(n-1)^{th}$  instant and  $I^*_{smq(n-1)}$  is the amplitude of the quadrature component of the reference source current at the  $(n-1)^{th}$  instant. The quadrature components of the reference source currents are computed as:

$$i^*_{saq} = I^*_{smq} w_a; \quad i^*_{sbq} = I^*_{smq} w_b; \quad i^*_{scq} = I^*_{smq} w_c$$
 (8)

### 3.1.2 In-phase component of reference source currents

The error in the DC bus voltage of the STATCOM  $(V_{dcer(n)})$  at the  $n^{th}$  sampling instant is:

$$V_{dcer(n)} = V_{dcref(n)} - V_{dc(n)}$$
(9)

where  $V_{\text{dcref(n)}}$  is the reference DC voltage and  $V_{\text{dc(n)}}$  is the sensed DC link voltage of the STATCOM. The output of the PI controller for maintaining the DC bus voltage of the STATCOM at the  $n^{\text{th}}$  sampling instant, is expressed as:

$$I^*_{smd(n)} = I^*_{smd(n-1)} + K_{pd} \{V_{dcer(n)} - V_{dcer(n-1)}\} + K_{id} V_{dcer(n)} (10)$$

 $I*_{smd(n)}$  is considered to be the amplitude of the active source current.  $K_{pd}$  and  $K_{id}$  are the proportional and integral gain constants of the DC bus PI voltage controller. The in-phase components of the reference source currents are computed as:

$$i*_{sad} = I*_{smd} u_a;$$
  $i*_{sbd} = I*_{smd} u_b;$   $i*_{scd} = I*_{smd} u_c$  (11)

#### 3.1.3 Total reference source currents

The total reference source currents are the sum of the inphase and quadrature components of the reference source currents as:

$$i^*_{sa} = i^*_{saq} + i^*_{sad}$$
 (12)

$$i^*_{sb} = i^*_{sbq} + i^*_{sbd}$$
 (13)

$$i^*_{sc} = i^*_{scq} + i^*_{scd}$$
 (14)

#### 3.1.4 PWM current controller

The total reference currents ( $i*_{sa}$ ,  $i*_{sb}$  and  $i*_{sc}$ ) are compared with the sensed source currents ( $i_{sa}$ ,  $i_{sb}$  and  $i_{sc}$ ). The ON/OFF switching patterns of the gate drive signals to the IGBTs are generated from the PWM current controller. The current errors are computed as:

$$i_{\text{saerr}} = i *_{\text{sa}} - i_{\text{sa}} \tag{15}$$

$$i_{\text{sberr}} = i^*_{\text{sb}} - i_{\text{sb}} \tag{16}$$

$$i_{\text{scerr}} = i *_{\text{sc}} - i_{\text{sc}} \tag{17}$$

These current error signals are amplified and then compared with the triangular carrier wave. If the amplified current error signal is greater than the triangular wave signal switch  $S_4$  (lower device) is ON and switch  $S_1$  (upper device) is OFF, and the value of the switching function SA is set to 0. If the amplified current error signal corresponding to  $i_{\text{saerr}}$  is less than the triangular wave signal, switch  $S_1$  is ON and switch  $S_4$  is OFF, and the value of SA is set to 1. Similar logic applies to the other phases.

#### 3.2 Modeling of STATCOM

The STATCOM is a current controlled VSI and is modeled as follows:

The derivative of its DC bus voltage is defined as:

$$pv_{dc} = (i_{ca} SA + i_{cb} SB + i_{cc} SC)/C_{dc}$$
 (18)

Where SA, SB and SC are the switching functions for the ON/OFF positions of the VSI bridge switches S<sub>1</sub>-S<sub>6</sub>.

The DC bus voltage reflects the output of the inverter in the form of the three-phase PWM AC line voltage  $e_{ab}$ ,  $e_{bc}$  and  $e_{ca}$ . These voltages may be expressed as:

$$e_{ab} = v_{dc} (SA-SB)$$
 (19)

$$e_{bc} = v_{dc} \text{ (SB-SC)}$$
 (20)

$$e_{ca} = v_{dc} (SC - SA)$$
 (21)

The volt-amp equations for the output of the voltage source inverter (STATCOM) are:

$$v_a = R_f i_{ca} + L_f p i_{ca} + e_{ab} - R_f i_{cb} - L_f p i_{cb}$$
 (22)

$$v_b = R_f i_{cb} + L_f p i_{cb} + e_{bc} - R_f i_{cc} - L_f p i_{cc}$$
 (23)

$$i_{ca} + i_{cb} + i_{cc} = 0$$
 (24)

The value of  $i_{cc}$  from eqn (24) is substituted into eqn. (23) which results in:

$$v_b = R_f i_{cb} + L_f p i_{cb} + e_{bc} + R_f i_{ca} + L_f p i_{ca} + R_f i_{cb} + L_f p i_{cb}$$
(25)

Rearranging the eqn. (22) and eqn. (25) results in:

$$L_f pi_{ca} - L_f pi_{cb} = v_a - e_{ab} - R_f i_{ca} + R_f i_{cb}$$
 (26)

$$L_f pi_{ca} + 2 L_f pi_{cb} = v_b - e_{bc} - R_f i_{ca} - 2 R_f i_{cb}$$
 (27)

Hence, the STATCOM current derivatives are obtained by solving eqns. (26) and (27) as:

$$pi_{ca} = \{(v_b - e_{bc}) + 2(v_a - e_{ab}) - 3R_f i_{ca}\}/(3L_f)$$
 (28)

$$pi_{cb} = \{(v_b - e_{bc}) - (v_a - e_{ab}) - 3 R_f i_{cb}\}/(3L_f)$$
 (29)

#### 3.3 Modeling of SEIG

The dynamic model of the three-phase SEIG is developed a using stationary d-q axes references frame, whose voltage-ampere equations with usual notation are [3].

$$[v] = [R][i] + [L]p[i] + w_g[G][i]$$
 (30)

from which, the current derivatives can be expressed as:

$$p[i] = [L]^{-1} \{ [v] - [R] [i] - w_g [G] [i] \}$$
 (31)

where  $[v] = [v_{ds} \ v_{qs} \ v_{dr} \ v_{qr}]^T$ ;  $[i] = [i_{ds} \ i_{qs} \ i_{dr} \ i_{qr}]^T$ 

$$[R] = diag [R_s R_s R_r R_r]$$

$$[L] = \begin{bmatrix} L_{ss} & 0 & L_{m} & 0 \\ 0 & L_{ss} & 0 & L_{m} \\ L_{m} & 0 & L_{rr} & 0 \\ 0 & L_{m} & 0 & L_{rr} \end{bmatrix} [G] = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 - L_{m} & 0 & L_{rr} \\ L_{m} & 0 & L_{rr} & 0 \end{bmatrix}$$
(32)

Where 
$$L_{ss} = L_{ls} + L_m$$
 and  $L_{rr} = L_{lr} + L_m$ 

The electromagnetic torque balance equation of the SEIG is defined as:

$$T_{\text{shaft}} = T_e + J(2/P) p w_g$$
 (33)

The derivative of the rotor speed of the SEIG from eqn. (33) is:

$$pw_g = \{P/(2J)\} (T_{shaft} - T_e)$$
 (34)

where the developed electromagnetic torque of the SEIG is expressed as [3]:

$$T_e = (3P/4) L_m (i_{qs} i_{dr} - i_{ds} i_{qr})$$
 (35)

The shaft torque of the prime mover is considered a function of speed as:

$$T_{\text{shaft}} = (k_1 - k_2 w_g)$$
 (36)

where  $T_{shaft}$  is the shaft torque which is decided by the drooping characteristic of the prime-mover. Constants  $k_1(3370)$  and  $k_2$  (10) are fixed for a particular type of prime mover. The SEIG operates in the saturation region and its magenetizing characteristic is non-linear in nature. Therefore, the magnetizing current should be calculated at each step of integration in terms of the stator and the rotor dq axes currents as:

$$I_{m} = \{(i_{ds} + i_{dr})^{2} + (i_{qs} + i_{qr})^{2}\}^{1/2} / \sqrt{2}$$
(37)

Magnetizing inductance is calculated from the magnetization characteristic expressed using the curve between  $L_m$  and  $I_m$ . The relation between  $L_m$  and  $I_m$  is obtained by a synchronous speed test for the SEIG under test [13] and can be written as:

$$L_{m}=0.205+0.0053I_{m}-0.0023\ I_{m}^{2}+0.0001I_{m}^{3}$$
(38)

### 3.4 AC Line Voltage at the Point of Common Coupling

Direct and quadrature axis currents of the SEIG ( $i_{ds}$  and  $i_{qs}$ ) are converted into three-phases (a, b and c). The derivative of the AC terminal voltage of the SEIG is defined as:

$$p V_a = \{(i_a - i_{ra} - i_{ca}) - (i_b - i_{rb} - i_{cb})\} / (3 C)$$
 (39)

$$p V_b = \{(i_a - i_{rc} - i_{ca}) + 2(i_b - i_{rb} - i_{cb})\} / (3 C)$$
 (40)

$$v_a + v_b + v_c = 0. (41)$$

where i<sub>a</sub>, i<sub>b</sub> and i<sub>c</sub> are the SEIG stator line currents, i<sub>ra</sub>,

 $i_{rb}$  and  $i_{rc}$  are the 3-phase load line currents and  $i_{ca}$ ,  $i_{cb}$  and  $i_{cc}$  are the STATCOM currents. C is the per phase excitation capacitor, which is connected across the SEIG terminals.

#### 3.5 Modeling of Loads

The mathematical modeling of linear and non-linear loads is divided into the following three categories.

#### 3.5.1 Three-phase resistive load

The line currents  $i_{ra}$ ,  $i_{rb}$  and  $i_{rc}$  in delta connected loads are obtained as:

$$i_{ra} = (v_a - v_c)/R_L \tag{42}$$

$$i_{rb} = (v_b - v_a)/R_L \tag{43}$$

$$i_{rc} = (v_c - v_b)/R_L \tag{44}$$

#### 3.5.2 Three-phase resistive-inductive load

The derivative of phase currents of the delta connected resistive-inductive loads are defined as:

$$p i_{na} = (v_a - R_L i_{na})/L_L$$
 (45)

$$p i_{bb} = (v_b - R_L i_{bb})/L_L$$
 (46)

From these load phase currents, the line currents of this delta connected resistive-inductive load are:

$$i_{ra} = (i_{pa} - i_{pc}); \quad i_{rb} = (i_{pb} - i_{pa}); \quad i_{rc} = (i_{pc} - i_{pa}); \quad (48)$$

## 3.5.3 Three-phase rectifier with capacitive filter and resistive load

In a practical uncontrolled diode bridge rectifier, an electrolytic capacitor is used at the DC output for filtering to feed DC load. An uncontrolled diode bridge rectifier has two operating modes: conducting and non-conducting. Small source impedance ( $R_{sL}$ ,  $L_{sL}$ ) is considered at the input of the rectifier. When the diodes are in conduction, the line-line voltage of the AC source is connected to the load and the basic DC side equation is given by:

$$v_s = 2 R_{SL} i_d + 2 L_{SL} p i_d + v_d$$
 (49)

In the current derivative form, the above equation can be expressed as:

$$p i_d = (v_s - v_d - 2 R_{SL} i_d) / (2L_{SL})$$
(50)

where  $v_d$  and  $i_d$  are the diode rectifier output DC voltage and current, voltage  $v_s$  is the input line voltage segment which is determined by the conducting diode pair of the rectifier.

The AC load currents in all three phases ( $i_{ra}$ ,  $i_{rb}$  and  $i_{rc}$ ) of the AC source are calculated by using the magnitude of  $i_d$  and the direction (sign) corresponding to the conduction pairs of diodes, which is the same as shown in Table 1.

Moreover, the charging/discharging equation of the DC load filter capacitor is expressed as:

$$pv_d = (i_d - i_r) / C_{RL}$$
 (51)

Where  $C_{RL}$  is the load capacitance on the DC side,  $v_s$  is the maximum line voltage of the generator  $(v_a, v_b, v_c, -v_a, -v_b)$  and  $-v_c$ ,  $v_d$  is the instantaneous voltage across the capacitor and  $i_r$  is the resistive load current  $(v_d / R_{RL})$ . When neither of the diode pair is conducting then the charged capacitor would discharge through the load resistance  $(R_{RL})$ .

Table 1 Three-phase non-linear AC load currents

S. No.	Maximum voltage	i <sub>ra</sub>	i <sub>rb</sub>	i <sub>rc</sub>
1	Va	i <sub>d</sub>	-i <sub>d</sub>	0
2	-v <sub>a</sub>	-i <sub>d</sub>	i <sub>d</sub>	0
3	V <sub>b</sub>	0	i <sub>d</sub>	-i <sub>d</sub>
4	-v <sub>b</sub>	0	-i <sub>d</sub>	i <sub>d</sub>
5	V <sub>c</sub>	-i <sub>d</sub>	0	i <sub>d</sub>
6	-v <sub>c</sub>	i <sub>d</sub>	0	-i <sub>d</sub>

### 3.5.4 Single-phase rectifier with resistivecapacitive load

The single-phase rectifier with capacitive filter and resistive load has two operating modes: conducting and non-conducting. When the diodes are conducting, the AC source is connected to the load and the basic equation is expressed as:

$$v_s = R_{SL}i_d + L_{SL}pi_d + v_d$$
 (52)

In the current derivative form, the above equation can be expressed as:

$$p i_d = (v_s - v_d - R_{SL}i_d) / (L_{SL})$$
 (53)

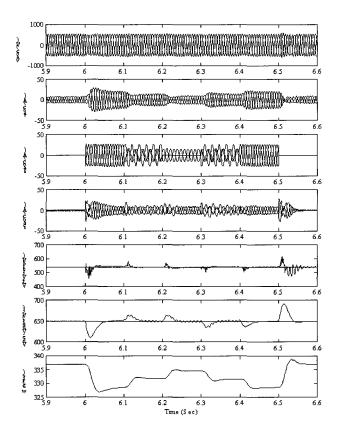


Fig. 2 Transient waveforms of three-phase SEIG-STATCOM system supplying resistive load at no-load to 3-ph(15kW) to 2-ph(10kW) to 1-ph(5kW)to 2-ph(10kW) to 3-ph(15kW) to no load

and the charging /discharging equation of the DC load filter capacitor is:

$$pv_d = (i_d - i_r) / C_{RL}$$
(54)

When neither of the diode pair is conducting then the charged capacitor would discharge through the load resistance ( $R_{RL}$ ). The rectifier AC currents will be the same as mentioned in Table 1 and they will be zero in the non-conducting phase.

#### 4. Results and Discussion

The SEIG-STATCOM system feeding linear/non-linear and balanced/unbalanced loads are simulated and results are shown in Figs. 2-6. For this study, a 15 kW, 381/440V, 30A, 4-pole machine was used as a generator and the parameters of the generator are given in the Appendix.

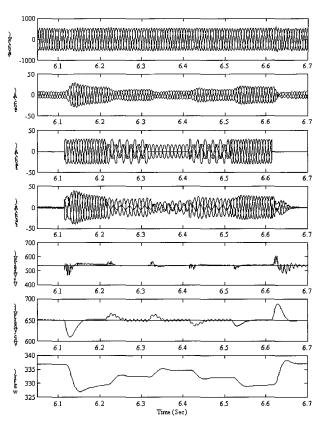


Fig. 3 Transient waveforms of three-phase SEIG-STATCOM system supplying lagging(0.8) pf load at no-load to 3-ph(15kW) to 2-ph(10kW) to 1-ph(5kW) to 2-ph(10kW) to 3-ph(15kW) to load

## 4.1 Performance of SEIG-STATCOM System Feeding Resistive Loads

A resistive load is considered to be a linear load. Fig. 2 shows the transient waveforms of the 3-phase generator voltages (vabc), generator currents (iabc), three-phase load currents (i<sub>ra</sub>, i<sub>rb</sub> and i<sub>rc</sub>), three-phase STATCOM currents  $(i_{ca},\,i_{cb}$  and  $i_{cc})$ , the amplitude of the SEIG terminal voltage and its reference value (Vt-Vtref), the DC bus voltage and its reference value (V<sub>dc</sub>- V<sub>dcref</sub>) and the generator speed (wg). It demonstrates the response of the STATCOM for regulating the SEIG terminal voltage while a pure resistive load is being applied. At 0.6 sec a three-phase 15 kW resistive load is switched on. A dip in the prime mover speed of the SEIG is observed at the sudden application of the 15 kW load due to the drooping characteristic of the prime mover. A small dip in the DC bus voltage of STATCOM is also observed, but it recovers quickly due to the corrective action of the PI controller. At 6.1-sec.

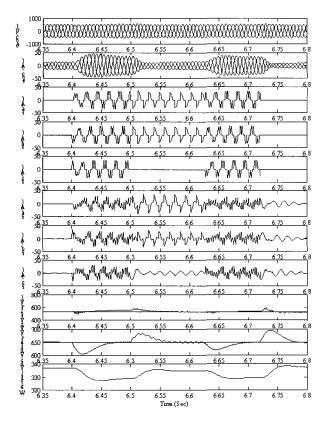


Fig. 4 Transient waveforms of three-phase SEIG-STATCOM system supplying non-linear load at no-load to 3-ph(15kW) to 1-ph(5.8kW) to 3-ph to no load

one-phase of the load is disconnected from the generator and the generated power is reduced to 10 kW. It is observed that the STATCOM is able to regulate the SEIG terminal without any surge. At 6.2-sec. two phases of the load are disconnected from the generator (resulting in only 5kW generated power). When the load phases are disconnected from the generator, its currents decrease to show the lesser burden on the SEIG. At 6.3-sec. one-phase of the load is connected to the SEIG-STATCOM system and at 6.4-sec. the second phase of the load is connected. At 6.5-sec the three-phase load is disconnected from the SEIG-STATCOM system. An over-shoot and an undershoot in the DC bus voltage are observed, respectively, at the disconnecting and connecting of the load. Charging and discharging of the DC bus capacitor of the STATCOM is clearly observed when the load is unbalanced. This shows the load balancing aspect of the STATCOM. The total harmonic distortion (THD) of the generator voltage and current, as shown in Table 2, is

Table 2 Generator voltage and current and load current THD under three-phase and single-phase loads

Type of Load	Generator Voltage	Generator Current	Load Current
Three-phase R load	0.167%	0.084%	0.05%
Single-phase R load	0.375%	0.433%	0.143%
Three-phase R-L load	0.285%	0.151%	0.10%
Single-phase R-L load	0.336%	1.09%	0.11%
Three-phase rectifier load	0.185%	0.197%	56.37%
Single-phase rectifier load	0.80%	1.024%	51.81%

below 5% for both a three-phase and even a single-phase (severely unbalanced) resistive load.

### 4.2 Performance of SEIG-STATCOM System Feeding Resistive-inductive Loads

A resistive-inductive load is considered to be another linear load. Fig.3 shows the transient waveforms of a three-phase SEIG-STATCOM system supplying lagging pf (0.8) load. The three-phase generator voltages (v<sub>abc</sub>), generator currents (iabc), three-phase load currents (irabc), three-phase STATCOM currents (icabc), amplitude of the SEIG terminal voltage and its reference value (V<sub>1</sub>-V<sub>tref</sub>), the DC bus voltage and its reference value (V<sub>dc</sub>-V<sub>dcref</sub>) and the generator speed (wg) are illustrated in the figure to show the voltage regulation and load balancing concept. At 6.115-sec. a three-phase lagging pf load of 15 kW is applied resulting in increased generator currents, load currents, and STATCOM currents due to supplying active and reactive power to the load. At 6.215-sec. one-phase of the load is disconnected from the generator and at 6.315sec. the second phase is disconnected; the generated power is reduced to 10 kW and 5 kW, respectively. The total harmonic distortion (THD) of the generator voltage and current for the three-phase balanced case and the singlephase unbalanced case is mentioned in Table 2 and it is observed that the THD is less than 5%. At 6.415-sec. one phase of the load is reconnected and at 6.515-sec. the second phase is reconnected. At 6.615-sec. the total threephase load is removed from the SEIG terminals. It is

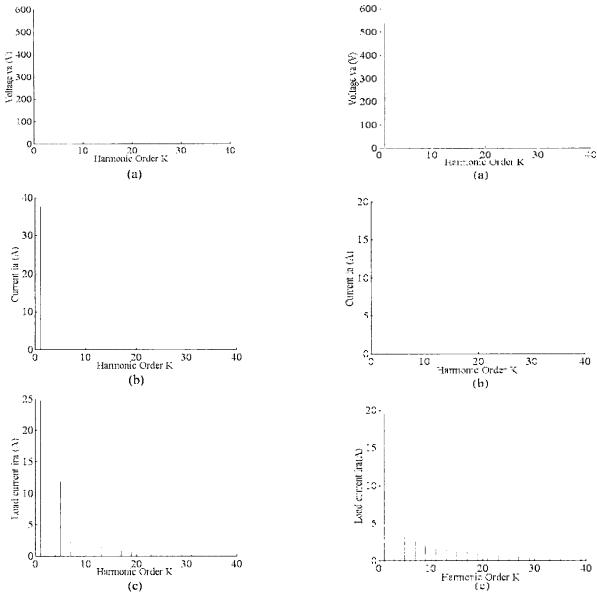


Fig. 5 Harm onic spectrum of generator voltage, cureent and three-phase nonlinear load current

Fig. 6 Harm onic spectrum of generator voltage, cureent and single-phase nonlinear load current

observed that the generator voltage remains constant under balanced and even unbalanced lagging pf loads. Variations in generator speed are observed with the change in load due to the drooping characteristic of the prime mover.

# 4.3 Performance of SEIG-STATCOM Feeding Non-Linear load

Three-phase and single-phase rectifiers with capacitive filter and resistive load are considered as non-linear loads. Fig.4 shows the transient waveforms of all the performance quantities of the three-phase SEIG-STATCOM system supplying three-phase rectifier with capacitive filter and DC load. At 6.4 sec it is changed to a single-phase rectifier load. In the case of a single-phase rectifier, due to the DC link capacitor of the rectifier, the AC current of the rectifier is highly discontinuous. The discontinuous AC current injects harmonics into the system. The STATCOM eliminates harmonics so that the generator voltages and currents are free from harmonics as can be observed from Figs. 5-6 and Table-2. Figs. 5a, 5b

and 5c show the harmonic spectrum of the generator voltage, current and load current, respectively, under a three-phase rectifier load. Fig. 6a, Fig. 6b and Fig. 6c show the harmonic spectrum of the generator voltage, current and load current under a single-phase rectifier load. It is observed from the harmonic spectrum shown in Figs. 5-6 and Table-2 that the THD in the generator voltage and current is less than 5% in spite of the 52% THD of the rectifier load current. The generator voltage and current remain constant and sinusoidal under three-phase and single-phase rectifier loads. Therefore, in this case, STATCOM is acting as a voltage regulator, load balancer and harmonic eliminator. Under the single-phase rectifier load, the generator speed of the SEIG is higher, which shows the light load on the generator.

#### 5. Conclusion

It is observed that the developed dynamic model of the three-phase SEIG-STATCOM is capable of simulating its performance while feeding linear/non-linear, balanced / unbalanced loads under transient conditions. From these results, it is found that the SEIG terminal voltage remains constant and sinusoidal under a three-phase or a singlephase rectifier load. When a single-phase rectifier load is connected, the STATCOM balances these unbalanced load currents so that the generator currents and voltages remain sinusoidal, balanced and constant and, thus, STATCOM acts as a load balancer. A rectifier based non-linear load generates harmonics, which are also eliminated by STATCOM. Therefore, it is concluded that the STATCOM acts as a voltage regulator, a load balancer and a harmonic eliminator. Although different aspects of uncontrolled rectifiers have been modeled as non-linear loads here, the developed model can easily be modified to simulate a compensating controlled rectifier as a nonlinear load.

#### **Appendices**

#### 1) STATCOM Control Parameters

 $L_f$ = 1.2 mH,  $R_f$  = 0.045  $\Omega$  and  $C_{dc}$  = 4000 $\mu$ F. AC voltage PI controller:  $K_{pa}$  =0.05,  $K_{ia}$  = 0.04. DC bus voltage PI controller  $K_{pd}$  = 0.7,  $K_{id}$  =0.1 Carrier frequency = 20 kHz

#### 2) Parameters of Rectifier Load

Three-phase rectifier  $L_{sL}$ =0.1mH,  $R_{SL}$  = 1  $\Omega$ ,  $R_{RL}$  = 22  $\Omega$ , and  $C_{RL}$  = 470 $\mu$ F. Single-phase rectifier  $L_{SL}$ =0.1mH,  $R_{SL}$  = 1  $\Omega$ ,  $R_{RL}$ =75  $\Omega$  and  $C_{RL}$ =150 $\mu$ F

#### 3) Machine Parameters

The parameters of the 15 kW, 381/440V, 30A, 50 Hz, 4-pole induction machine are given below.

$$R_s = 0.69~\Omega,~R_r = 0.74\Omega,~L_{ls} = L_{lr} = 1.1~mH,~J = 0.23$$
 kg/m²,  $L_{ss} = L_{ls} + L_m$  and  $L_{rr} = L_{lr} + L_m$ .

4) Terminal capacitor

 $C = 57 \mu F / \text{ phase}$ 

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