Development of Torsional Shear Testing System to Measure P-wave Velocity, S-wave Velocity and Pore Water Pressure Buildup on Fully and Partially Saturated Sands

포화 및 부분 포화 사질토의 V_p와 V_s 속도 및 과잉간극수압 측정을 위한 비틂전단 시험기의 개발

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Abstract

Laboratory tests have revealed that the liquefaction resistance of sands depends strongly upon the degree of saturation, which is expressed in terms of the pore pressure coefficient, B. The velocity of compression waves(i.e. P-waves), which have been known to be influenced largely by the degree of saturation and can be measured conveniently in the field, appears as an indicator of saturation. In this paper, the Stokoe type torsional shear(TS) testing equipment is modified to saturate the specimen and measure the velocities of P-wave and S-wave and pore pressure buildup. The velocities of P-wave and S-wave for Toyoura sand from Japan is measured and compared at the various B-value (degree of saturation) which are partially saturated to fully saturated conditions. Additionally, the variation of the pore water pressure induced during undrained TS tests at the various B-value is measured and analyzed.

Keywords : B-value, S-wave velocity, P-wave velocity, Torsional shear testing, Excess pore water pressure

요 지

사질토의 액상화에 대한 저항 강도는 포화도에 상당히 의존한다. 압축파 속도는 현장에서 쉽게 측정이 가능하고 포화도의 영향을 크게 받기 때문에 현장 지반의 포화도를 예측하고자 할 때 효율적으로 사용 될 수 있다 . 본 논문에서는 시료의 포화가 가능하고 전단파, 압축파 속도 측정 및 비배수 상태에서 비틂 전단 시험을 수행시 유발되는 과잉간극수압을 측정할 수 있는 비틂전단 시험기를 개발하였다. 토요라 모 래에 대해 전단파, 압축파 속도 측정이 수행되고, 비배수 비틂전단 시험을 실시하였다. 포화도(B값)에 따 른 시료의 전단파 속도 및 압축파 속도를 이론식과 비교하여 개발된 시험기를 검증하였으며, 여러 B값에 서 비배수 TS 시험동안 유발되는 과잉 간극수압의 변화를 측정·분석하였다.

주요어 : B값, 전단파 속도, 압축파 속도, 비틂전단 시험, 과잉간극수압

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1. Introduction

The liquefaction resistance of sand is closely related with the degree of saturation because the liquefaction resistance is evaluated from the buildup of excess pore water pressure in undrained condition which is much dependent on the degree of saturation. According to studies by Chaney (1978), Yoshimi et al. (1989) and Grzic et al. (1999, 2000), when the B-value drops to a level of about zero at the degree of saturation, Sr, of about 90%, the liquefaction resistance has been shown to increase roughly two times as much as that of fully saturated conditions.

It has been presented by recent studies that in-situ sand is partially saturated despite the deposit is located at several meters below the water table. Kokusho (2000) and Tsukamoto et. al.(2002) has reported that $V_{\rm p}$ of in-situ soils below a water table is lower than about 1500m/s which is V_p in pure water, and has the values of 800m/s to 1300m/s despite the soil is located below a water table. This means that the soil deposit several meters below the water table may be not fully saturated but partially saturated soil and the liquefaction resistance of in-situ sand below ground water table may be greater than the value normally evaluated at fully saturated condition in design practice. Therefore, the effect of the degree of saturation on the undrained behavior of sand and the evaluation of the degree of saturation for in-situ soil may have important role in the geotechnical earthquake engineering.

In laboratory tests, the B-value has been widely used to quantify the state of saturation, because this value is easily measured and accurate enough to indicate a state of partial saturation. It is well known that the pore water pressure coefficient, B, introduced by Skempton (1954) is given as ;

 $B = \Delta u / \Delta \sigma \tag{1}$

where $\Delta \sigma$ and Δu are the increments of the confining cell pressure and pore water pressure caused by $\Delta \sigma$ in undrained condition. However, it is practically impossible for the B-value to monitor the state of saturation of the soil in the field.

Nowadays, the velocities of shear wave, Vs, and longitudinal wave, Vp, have been measured at a lot of field sites for site investigation by field seismic tests such as the down-hole, cross-hole, up-hole tests and so on. The V_p is very sensitive on the state of saturation of soil because the compressibility of water is relatively very larger than that of soil skeleton (Kokusho, 2000; Tamura et. al., 2002; Tsukamoto, 2002). Therefore, V_p can be used as a convenient index for the evaluation of saturation. Also, the measurement of Vp has many advantages on the study on the relation between V_p and the saturation and the relation between these parameters and the undrained behaviors of sand, because it is possible to measure V_p in laboratory as well as in field.

The first objective of this paper is to develop the testing system to perform the saturation of a soil specimen and undrained tests and, at the same time, measure S-wave velocity(V_s) and P-wave velocity(V_p) of specimen. For this objective, the existing Stokoe-type torsional shear (TS) equipment is modified to saturate a soil specimen and measure excess pore water pressure buildup (Δu) during undrained TS tests. Also, the measurement system of S-wave velocity (Vs) and P-wave velocity (V_p) is added to the modified TS system. The second objective is to measure the value of V_p/V_s measured at various B-values and to compare the V_p/V_s with a existing theoretical formula using the modified equipment. The last objective is to study the effect of partial saturation on pore water pressure buildup(Δu) and deformation characteristics(G, D) of sand during undrained TS tests.



Fig. 1. Schematic Configuration of the Modified TS Equipment

2. Modifications of Torsional Shear Testing Equipment

(TS)Stokoe-type torsional shear testing equipment in this study has been widely used to investigate deformation characteristics (shear modulus and damping ratio) of soils at shear strains from $10^{-4}\%$ to 0.1% in geotechnical earthquake engineering. In this equipment, the bottom of the solid soil specimen is rigidly fixed against rotation at the base pedestal while the top (free end) is connected to a drive system that is used to excite and monitor motion as shown in Figure 1. Eddy-current type proximity transducers are used to measure the angle of twist of specimen while the voltage applied to the coils is calibrated to yield torque. TS tests were performed as stress-controlled cyclic tests because the torque of the TS equipment is in proportion to the voltage passing through the drive coils and the sinusoidal voltage having a constant amplitude is excited to coils. The maximum torque of this TS testing equipment is about 0.515 N-m.

The secant shear modulus is determined by the slope of the hysteresis loop and the equivalent damping ratio is determined on the basis of the area of the loop as shown Figure 2. Thus, the shear modulus and damping ratio are calculated from;

$$G = \tau_c / \gamma_c \tag{2}$$

$$D = A_L / (4\pi A_T) \tag{3}$$

where τ_c and γ_c are cyclic shear stress

amplitude and cyclic shear strain amplitude, A_L is the area enclosed by a hysteresis loop and $A_T=\tau c$ $\cdot \gamma_c/2$ is the peak strain energy stored during the cycle, and cyclic shear strain amplitude is calculated at 0.80 times the radius of the solid specimen (Chen and Stokoe, 1979).



Fig. 2. Measurement of shear modulus and damping ratio of torsional shear tests

In this study, the existing Stokoe-type torsional shear testing equipment is modified to saturate the specimen and to determine P-wave velocity (V_p) , S-wave velocity (V_s) and excess pore water pressure buildup (Δu) of saturated specimens during undrained TS tests.

2.1 Saturation of Soil Specimen and Measurement of Pore Water Pressure

The modification of TS equipment includes two new elements, which are 1) a quick connector (Swagelok SS-QM2-B 200, SS-QM2-D-2PM) attached to a top cap and 2) a back pressure system which consists of a pneumatic pressure regulator (Fairchild M 10 regulator), a burette system and a pore pressure transducer (RDP FDW 150psi) installed at bottom pedestal as illustrated in Figure 1.

The quick connector is attached at the upside of the top cap and consists of two parts of male and female as shown in Figure 3. It can connect and disconnect the pressure lines easily, and when disconnected, the male and female parts and the corresponding pressure lines are kept closed. After the preparation of a soil specimen, CO₂ gas and water are made to flow upward through the specimen under the pressure difference between top and bottom of the specimen using a quick connector. Once the air within a soil specimen is exchanged with water, the quick connector is disconnected and the top cap becomes closed. After that, a covering adaptor is fastened by 4 bolts to the top cap and sealed by O-ring to protect the remaining part of quick connector at the top cap from the compressed air in confining chamber and be coupled with the drive plate of a drive system.



Fig. 3. Picture of a male part and a female part of quick connector

A back pressure system makes pore water pressure high enough to diminish the size of air bubbles in the pore of the specimen and dissolve air bubbles in water. A pore water pressure transducer measures the back pressure and the excess pore water pressure generated during the undrained TS tests. A burette system converts pneumatic pressure to water pressure and transmit pressure to pore water in sands. Also, the burette system measures volume changes in the soil specimen after shear loading.

Because the confining pressure is applied by air pressure, the water bath is installed to provide the air-water interface and retard the air migration. Because the pore pressure buildup can be significantly affected by the degree of saturation, it is important to achieve the full saturation of the soil specimen and maintain the saturation during the testing. In this study, the saturation is checked by the B parameter, which is generally maintained above 0.99. An example of the variation in the B-value with time after the back pressure saturation is presented in Figure 4. It can be noticed that B-value is maintained above 0.99 for about 1 hour during which time the TS testing can be completed at a given confining pressure.



Fig. 4. Variations of B-values measured by modified TS testing system

2.2 Measurement of Shear Wave Velocity(V_s)

Bender elements are mounted on the top cap and bottom pedestal of the equipment to send and to receive shear waves. The bender element method is a simple technique to obtain the velocity of shear wave propagation through a sample. Bender elements used in this study were produced by Morgan-Electroceramics and made of Lead Zirconate Titanates (PZT 5H) with the following dimensions; 12.7mm length, 8mm width and 0.6mm thickness. The bender elements double-coated with a waterproofing material (Polyurethane) are placed in slots of the top cap and bottom pedestal and the gap around the bender element in the slot is filled with epoxy

resin to fix bender elements in slots. Then, the bender element to receive the signal is coated with conductive coating and grounded to avoid electromagnetic coupling and cross-talk. Figure 5 shows bender element mounted in top cap or bottom pedestal.(Soils and Waves, 2001)



Fig. 5. Bender element mounted in top cap or pedestal



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Fig. 6. Top cap and bottom pedestal attached bender elements and accelerometer to

A HP Function Generator Model 33120A is used to supply the input signal to the bender element in top cap and High resolution oscilloscope (HP 54624A) is used to record waveform from the receiving bender element in bottom pedestal. Rectangular signal is used as the input signal. The oscilloscope measures signal at the sampling rate of 1MHz and 2000 data samples are stored in a disk. The oscilloscope measures signals using smoothing technique without filter, and stores the average of 128 stacked signals in a personal computer.

2.3 Measurement of Compression Wave Velocity(V_p)

Accelerometers are used to determine P-wave velocity(V_p) of the soil specimen and mounted on the top cap and bottom pedestal as shown Figure 6. The model of accelerometer is PCB 353B16

produced by PCB Piezotronics, and it is small size type; the height of 14.5mm, the width of 7.1mm and the weight of 1.5g. The accelerometer has the resonant frequency of 70kHz and the frequency range for measurement from 0.7Hz to 18000Hz and it is very suitable to measure high frequency vibration accurately. The signals of accelerometers is measured by the same oscilloscope (HP 54624A) used for bender element.

To determine V_p of the specimens, a steel ball and a rod of 2mm in diameter are used as sources. P-wave is propagated from bottom pedestal through the soil specimen as impact by a steel ball or a rod. V_p is determined by the time difference of the first arrivals between the two accelerometers. The time difference has to be corrected by the equipment calibration constant, which is defined as the travel time, tc, from top cap to bottom pedestal in contact without a specimen. The calibration constant, tc, shows a constant value of about 0.0000285sec (28.5µsec) from repeated tests. Vp is calculated from the length of the specimen divided by the corrected travel time. In this study, V_p is determined by the average of all V_p by the steel ball and rod because V_p by the steel ball is similar to that by the rod irrespective of source difference.

2.4 Height-Change Monitoring System

The height changes of the soil specimens is measured to account for the changes in the length of the specimen during consolidation or swell. Because the change of the specimen length is directly correlated with the wave propagation length in determining V_s and V_p , the measurement of the height-change is very important. Also, the measurement of height-change is used to calculate change in the mass density and void ratio during thesting. The height-change monitoring system consists of a proximity transducer (Bently Nevada 3300XL) and the aluminum target installed on the upper side of the target for motion monitoring sensors as shown Figure 1. The output from the proximity transducer is read with a digital voltmeter and the height change is calculated from the output voltage combined with the calibration factor.

3. Testing Material and Procedure

3.1 Testing Material

The test material is Toyoura sand from Japan, widely used in geotechnical laboratory testing. Toyoura sand is classified as poorly graded clean sand without fines. The grain size distribution of Toyoura sand is shown in Figure 7 and the physical soil properties are summarized in Table 1.



Fig. 7. Grain Size Distribution of Test Material

Table	1.	Physical	Properties	of	Test	Material
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Sample	Toyoura Sand
Unified Soil Classification (USCS)	SP
Maximum Void Ratio (e _{max})	0.982
Minimum Void Ratio (e _{min})	0.617
Specific Gravity (Gs)	2.65
Curvature Coefficient (Cc)	1.00
Uniformity Coefficient (Cu)	1.29
Plasticity Index(PI)	NP
Median Particle Size D50, mm	0.199

3.2 Testing Procedure

Soil specimens of 50mm in diameter and 100mm in height were prepared by the method of air pluviation in which air-dried sand is poured in mold from the nozzle with a rectangular inner cross section of 1.5mm to 10mm while maintaining a constant drop-height throughout preparation. In this study, the drop-height was maintained by about 22cm to achieve the relative density of D_r =50%. Before the mold is disassembled, a vacuum pressure of 10kPa is applied to the specimen, subsequently, the mold is dismantled and then the vacuum pressure is raised to 20kPa to stand the specimen. In this study, since all tests are performed under target isotropic effective stress, σ_0' , of 30kPa, the vacuum pressure of 20kPa is applied to keep standing the specimen.

In case of tests with high B-value above 0.8, CO_2 gas is flowed to replace the air through the specimen under a low pressure difference between top and bottom of the specimen (less than 15kPa) to expel the air within the specimen for $15 \sim 30$ min. Then, the specimen is filled with de-aired water which is flowed for about $30 \sim 60$ min to displace and dissolving the CO₂. In case of tests with low B-value less than 0.8, the CO₂ gas is not flowed but the only water is circulated though the specimen. After the circulation. initial specimen height and diameter is measured and then the TS equipment is setup. The isotropic effective stresses of all tests in this study are kept 30kPa constantly and B-value (the degree of saturation) of partially saturated specimens is controlled by increasing back pressure step by step in the increment of 30kPa. It is known that the B-value increases with increasing back pressure. After applying the back pressure for about an 60 minutes, B-value is checked. If the B-value reaches the target value, the dimension of the specimen is measured, and then V_s and V_p are determined bender elements bv and two accelerometer respectively. Finally, TS test is performed in undrained condition.

The typical signals of the transmitted and received waves are shown in Figure 8. Figure 8a and 8b show the signals of shear wave and compression wave propagated through specimen of B=0.97 and B=0.67 respectively. In Figure 8a, the





b) Compression Wave Propagation

Fig. 8. Typical Signals of Transmitted and Received Waves

effect of compression wave propagated through pore water can be noticed in the early part of the received signal

The undrained TS test is performed at shear strain range from 0.0002% to 0.1%. First, 11 cycles of TS testing is performed at the smallest strain amplitude possible below about 0.001%. The sinusoidal torque having constant amplitude and a constant loading frequency of 0.5Hz is applied to the specimen. The excess pore water pressure remained during undrained TS test is drained after 11 loading cycles and next TS test is continued with increasing strain amplitude.

Sample preparation, testing conditions and testing procedure are summarized in Table 2.

4. Test Results

4.1 Test results of V_s and V_p measurements

The $V_s/F(e)$ determined by bender element test are plotted versus the B-value in Figure 9. To eliminate the effect of void ratio, the values of V_s are normalized by a function of void ratio, which

Tests	S-wave velocity	Input Signal	rectangular				
	(BE Test)	# of Staking	128				
	D wave velocity	Sources	Steel Ball, Rod				
	r-wave velocity	# of Staking	1				
	TS Test	Excitation Type	sinusoidal				
		Loading Frequency	0.5Hz				
		# of Loading Cycles	11				
		Shear Strain Range	$2 \times 10^{-4} \% \sim 10^{-1} \%$ or more				
Pore-Pressure	Relative Density	Initial Void Ratio e	Effective Stress	Drainge Condition			
B-value	D _r (%)	initial volu Ratio, e	Effective Stress, 00				
0.01	52.4	0.789		Undrain			
0.28	48.9	0.801					
0.40	49.6	0.799					
0.67	47.6	0.806	201/Pa				
0.83	50.9	0.794	50KI a				
0.90	52.2	0.789					
0.97	53.0	0.786					
0.99	50.6	0.798					
Sample Preparation \rightarrow Back Pressure, Cell Pressure \rightarrow Checking B-value \rightarrow							
Measurement of V_s (BE Test) \rightarrow Measurement of $V_p \rightarrow$ Undrained TS Testing							

Table 2. Sample Preparation, Testing Conditions and Testing Procedure

recommended by Hardin(1963):

$$F(e) = \frac{(2.17 - e)^2}{1 + e} \tag{4}$$

The maximum shear modulus (G_{max}) which is calculated by Eq.(5) is also shown in Figure 9, where ρ is the total mass density of the soil specimen.

$$G_{\rm max} = \rho V_s^{\ 2} \tag{5}$$

As shown in Figure 9, the V_s tends to decrease slightly with an increase of the B-value from a value V_s =174m/sec at B=0.01 to V_s =160m/sec at B=0.97. The G_{max} have a same trend with V_s .

Some researchers have demonstrated the $V_{\rm p}$ is very dependent on small change in B-value between B=0.8 and B=1.0 in their theoretical studies (Nishio, 1987 ; Kokusho, 2000). The small amount of air bubble contained in pore water



Fig. 9. V_s/F(e), $G_{max}/F(e)$ versus B-value (BE)

affects the correlation of V_p with B-value. As an example, the 0.1 percent of air bubbles in the water makes the bulk modulus of air-water mixture 0.0625 times of that of water, since the bubble-like structure of the pores is much more compressible than water itself. Consequently, this small volume of air bubbles (0.1%) in the

pore-water reduce the wave propagation velocity of the mixture to about 1/4.

Based on the theory of wave propagation through a poro-elastic medium, Kokusho (2000) Tsukamoto (2002)presented and theoretical formula for determining the V_p with the variation of B-value of partly saturated sand as indicated in Eq.(6). The theoretical formula, Eq. (6).expresses the ratio V_p/V_s in terms of the skeleton Poisson's ratio, ν_b and B-value. In this study, the modified testing system tried to be verified by comparing the test results obtained by modified system with the formula.

$$\left(\frac{V_p}{V_s}\right)^2 = \frac{4}{3} + \frac{2(1-\nu_b)}{3(1-2\nu_b)(1-B)}$$
(6)

The ratio of V_p/V_s computed from Eq.(6) for various assumed values of the skeleton Poisson's ratio and test results are plotted in Figure 10a. As the value of V_s in Eq.(6) is assumed by the average value of V_s determined from bender element test. The results of V_p and V_s measurements are plotted in Figure 10b.



a) V_p/V_s vs B-value



Fig. 10. $V_{\rm p}/V_{\rm s},~V_{\rm p}$ and $V_{\rm s}$ versus B-value

It is seen that the values of V_p tend to increase significantly with increase of B-value. Besides, it would be reasonable to assume that the skeleton Poisson's ratio, ν_b is 0.4 under relative density, D_r=50% and isotropic effective stress, σ_0 '=30kPa. According to Ishihara (1996), Poisson's ratio is related to the shear modulus and it is expected that ν_b may be affected by D_r, σ_0 ' and so on. Also, further tests are required for the various D_r and σ_0 ' on Toyoura sand .

4.2 Torsional Shear (TS) Test Results under Undrained Condition

The variations in the normalized pore water pressure, $\Delta u/\sigma_0^{'}$, which is the cyclic pore water pressure normalized by effective confining pressure, with cyclic shear strain amplitude, γ_c are plotted in Figure 11. The pore water pressure does not increase at strains below about 0.01% and above this strain, the $\Delta u/\sigma_0^{'}$ increases with the number of cycle.

The values of $\Delta u/\sigma_0$ versus $\log \gamma_e$ with different B-values are plotted in Figure 12. The $\Delta u/\sigma_0$ after 10 loading cycles increases as B-value



Fig. 11. Typical Variation in $\Delta {\rm u}/{\rm \sigma_0^{'}}$ with γ_c measured by undrained TS tests

increases. This means the liquefaction potential varies according to B-value. In this reason, the effect of the B-value on the soil behaviors at undrained conditions must be considered.



Fig. 12. Variation of $\Delta {\rm u}/\sigma_{\rm 0}$ versus $\log \gamma_c$ with Different B-value

The normalized shear modulus reduction $(G/G_{max}-\log \gamma_c)$ and damping ratio curve $(D-\log \gamma_c)$ with different B-values are displayed in Figure 13a and 13b, respectively. It can be noticed that the effects of B-value on G/G_{max} and D curves

are negligible. Based on this study, the applicability of developed TS testing system on the measurements of V_p , V_s and pore pressure buildup was verified and further studies are needed.



b) Damping Curve (D-log γ_c) Fig. 13. G/G_{max}, D versus log γ_c with Different B-value

4. Conclusions

In this study, the existing Stokoe-type torsional shear equipment is modified to determine V_p , V_s and Δu of partially and fully saturated specimens

during undrained TS tests. To develop the saturation and measurement of pore water pressure in TS equipment, a quick connector and back pressure system is added in TS equipment. The bender elements and two accelerometers are mounted on top cap and bottom pedestal to measure V_s and V_p , respectively. Also, the height-change monitoring device is added to correct the wave propagation length in determining V_s and V_p .

The bender element testing results indicate that the V_s and G_{max} tend to decrease slightly with the increase of the B-value. The V_p tends to increase significantly with increase of B-value. The results of this paper (D_r=50% and σ_0 '=30kPa) is compared with the theoretical equations with the skeleton Poisson's ratio(ν_b =0.25, 0.3, 0.35, 0.4) and matched to the equation of ν_b =0.4. The $\Delta u/\sigma_0$ ' in undrained TS tests increase as B-value increases and the effects of B-values on G/G_{max} and D curves are relatively smaller than the pore water pressure buildup.

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