Determination of Strongly Interacting Spin Exchange Paths in Cu₂(O₃PCH₂PO₃) on the Basis of Spin Dimer Analysis

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The magnetic properties of the organic/inorganic hybrid copper-methylenediphosphonate. Cu₂(O₃PCH₂PO₃) were examined by performing the spin dimer analysis based on the extended Hückel tight binding method. In Cu₂(O₃PCH₂PO₃) the CuO₃ chains made up of edge-sharing CuO₅ square pyramidal units are inter-linked by O-P-O bridges. The Cu-O-Cu superexchange interactions of the CuO₃ chains are negligibly weak compared with the Cu-O··O-Cu super-superexchange interactions that occur between the CuO₃ chains. The spin exchange interactions of Cu₂(O₃PCH₂PO₃) are dominated by three super-superexchange interactions, which leads to a three-dimensional antiferromagnetic spin lattice. The strongest spin exchange interactions form isolated spin dimers, which suggests that, to a first approximation, the magnetic properties can be described in terms of an isolated spin dimer model.

Key Words: Spin dimer analysis. Superexchange interaction. Super-superexchange interaction, Magnetic orbitals, Electronic structure calculations

Introduction

Organic/inorganic hybrid materials combine the unique characteristics of their components to provide novel solid state structures with composite or new properties. Metalorganophosphonates are a class of such materials with potential applications to catalysis, ion exchange, proton conductivity, photochemistry and intercalation chemistry. and have been studied extensively. 1-3 Copper-methylenediphosphonate, Cu₂(O₃PCH₂PO₃), prepared by hydrothermal method and structurally characterized.4 exhibits interesting magnetic properties with broad maximum at approximately 50 K. The magnetic susceptibility in the high temperature region were fitted by the Heisenberg linear antiferromagnetic chain model with g = 2.10, $J/k_B = -35.9$ K and the Curie-Weiss temperature $\theta = -55$ K. The latter shows the presence of a dominant antiferromagnetic (AFM) coupling. The deviation from the linear chain behavior was observed at low temperatures, which was attributed to the occurrence of a long-range three-dimensional (3D) ordering. 4 To properly interpret the magnetic properties of a given magnetic system, one needs to have a spin lattice model (i.e., the repeat patterns of strongly interacting spin exchange paths) with which to analyze the magnetic data and hence to evaluate the relative strengths of its spin exchange interactions.⁵⁻⁷ In a magnetic oxide of spin-1/2 Cu²⁻ ions, spin exchange interactions between adjacent ions are either superexchange (SE) involving Cu-O-Cu paths8 or supersuperexchange (SSE) involving Cu-O···O-Cu paths. 5.6 SSE interactions can be much stronger than SE interactions. 5.6.7a but have frequently been neglected without justifiable reasons. To find a spin lattice model relevant for a magnetic oxide, the relative strengths of both SE and SSE interactions should be evaluated on the basis of proper electronic

structure considerations. The spin dimer analysis based on extended Hückel tight binding (EHTB) calculations has been indispensable for deducing spin lattices of magnetic insulators, because it generally reproduces the relative strengths of spin exchange interactions determined from first principles electronic structure calculations. 5.10

The crystal structure of Cu₂(O₃PCH₂PO₃) consists of highly distorted CuO₅ square pyramid and methylene-diphosphonate units. The CuO₅ units form one-dimensional (1D) CuO₃ chains by sharing their edges, and these CuO₃ chains are cross-linked by the methylenediphosphonates leading to the three dimensional (3D) crystal structure of Cu₂(O₃PCH₂PO₃) (Figure 1)⁴ such that the spin exchange interactions can occur through both SE and SSE paths. The

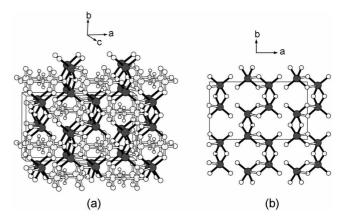


Figure 1. (a) Perspective view of the crystal structure of Cu₂(O₃PCH₂PO₃) and (b) projection view of the edge-sharing CuO₃ chain. The blue, yellow, cyan and large and small white circles represent Cu, P, C, O and H atoms, respectively. The black cylinders indicate the shortest four Cu-O bonds in CuO₅ square pyramidal unit.

observed magnetic susceptibility of Cu₂(O₃PCH₂PO₃) above 50 K has been described in terms of a 1D AFM Heisenberg chain model by considering only the SE interactions of the CuO₃ chains. However, the fitted magnetic susceptibility with this model deviates strongly from the experimental susceptibility below 50 K, and the reason of this poor fit is attributed to the occurrence of a long range magnetic ordering.4 It has been well established that the spin lattice of a magnetic solid does not necessarily have the same geometrical feature as does the arrangement of its magnetic ions or spin-carrying molecules, because magnetic orbitals are generally anisotropic in shape and because the strength of a spin exchange interaction between adjacent spin sites is determined by the overlap between their magnetic orbitals (i.e., singly occupied molecular orbitals). 56.11 In the present work, we examine the spin exchange interactions of Cuz-(O₃PCH₂PO₃) on the basis of EHTB calculations to evaluate its spin exchange interactions and hence identify the spin lattice responsible for its magnetic properties.

Spin Dimer Analysis

The strength of a spin-exchange interaction between two spin sites is described by a spin-exchange parameter $J = J_F - J_{AF}$, where J_F is the ferromagnetic (FM) term ($J_F > 0$) and J_{AF} is the AFM term ($J_{AF} < 0$). In most cases, J_F is very small so that the trends in the J values are well approximated by those in the corresponding J_{AF} values.^{5,6} For a spin dimer in which each spin site contains one unpaired spin. the J_{AF} term is approximated by⁵

$$J_{AF} = -\frac{(\Delta e)^{2}}{U_{eff}} \tag{1}$$

where U_{eff} is the effective on-site repulsion, which is essentially a constant for a given compound. If the two spin sites are equivalent, $\Delta \varepsilon$ is the energy difference $\Delta \varepsilon$ between the two magnetic orbitals representing the spin dimer. When

Table 1. Exponents ζ and valence shell ionization potentials H_{ii} of Slater-type orbitals χ_i used for extended Huckel tight-binding calculation"

Atom	X	$H_{u}\left(eV\right)$	ζ	Ç	ړ"،	C ¹
Cu	4s	-11.4	2.151	1.0		
Cu	4p	-6.06	1.370	1.0		
Cu	3d	-14.0	7.025	0.4473	3.004	0.6978
P	3s	-18.6	2.367	0.5836	1.499	0.5288
P	3р	-14.0	2.065	0.4908	1.227	0.5940
O	2s	-32.3	2.688	0.7076	1.675	0.3745
O	2p	-14.8	3.694	0.3322	1.659	0.7448
C	2s	-21.4	1.608	1.0000		
C	2p	-11.4	1.568	1.0000		
Н	ls	-13.6	1.300	1.0000		

" H_{ii} 's are the diagonal matrix elements $\lesssim \chi |H^{\rm eff}|\chi>$, where $H^{\rm eff}$ is the effective Hamiltonian. In our calculations of the off-diagonal matrix elements $H_0 = \lesssim \chi |H^{\rm eff}|\chi>$, the weighted formula was used. See: Ammeter, J.: Būrgi, H.-B.; Thibeault, J.; Hoffmann, R. J. Am. Chem. Soc. 1978, 100, 3686.

the two spin sites are nonequivalent, $(\Delta \varepsilon)^2 = (\Delta e)^2 - (\Delta e^0)^2$, where Δe^0 is the energy difference between the magnetic orbitals representing each spin site of the spin monomer (Δe^0 = 0 if the two spin sites are equivalent). In the tight binding approximation, the energy difference $\Delta \varepsilon$ is proportional to the overlap integral, S between the magnetic oribitals. Therefore, the antiferromagnetic term J_{AF} is related to $\Delta \varepsilon$ and S as $J_{AF} \propto -(\Delta \varepsilon)^2 \propto -S^{2,12.13}$ In the present work, the Δe and Δe^{0} values for various spin dimers are evaluated by performing EHTB calculations. 14.15 For a variety of magnetic solids of transition metal ions, it has been found that their magnetic properties are well described by the $(\Delta \varepsilon)^2$ values obtained from EHTB calculations, when both the d orbitals of the transition-metal ions and s/p orbitals of its surrounding ligands are represented by double- ζ Slater-type orbitals.16 Our calculations are carried out using the atomic parameters summarized in Table 1.

Results and Discussion

Each CuO₅ square pyramidal unit consists of four short and one long Cu-O distances (i.e., 1.934, 1.951, 1.966, 2.054 and 2.255 Å) as shown in Figure 2. It should be noted that the magnetic orbital of a spin monomer CuO₅ is contained in the basal plane of the square pyramid (Figure 2b). In each zigzag CuO₃ chain along the b-axis two adjacent CuO₅ units are connected by sharing their edges such that the Cu...Cu distances of 3.023 and 3.278 Å alternate (Figure 1b). These zigzag chains are linked by PO3C tetrahedra via the O-P-O bridges. Therefore, Cu₂(O₃PCH₂PO₃) has SE interactions in each CuO₃ chain through the edge-sharing dimers as well as SSE interactions between the adjacent CuO₃ chains through the O P O bridges. The spin exchange paths of Cu₂(O₃-PCH₂PO₃) are shown in Figure 3 and the geometrical parameters associated with them are summarized in Table 2. The SE path J_1 has Cu-O bond distances of 1.966 and 2.054 A, and unsymmetrical $\angle Cu$ -O-Cu bond angles 100.5 and 94.8°, while the SE path J_2 has unsymmetrical Cu-O bond distance 2.255 and 1.951 Å, and symmetrical ∠Cu-O-Cu bond angles 102.2° . The SSE path J_3 has O···O contact distance of 2.518 Å, which is shorter than the van der Waals distance, but the \(\negligcup Cu\)-O-Cu bond angles are highly unsymmetrical. The SSE path J_4 consists of two O···O contact distances of 2.526 and 2.534 Å, and the ∠Cu-O-Cu bond

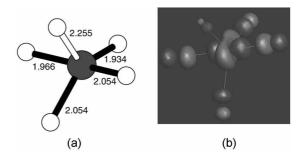


Figure 2. (a) Perspective view and (b) magnetic orbital of a distorted square pyramid CuO₃ in Cu₂(O₃PCH₂PO₃).

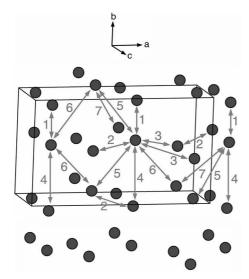


Figure 3. Schematic representation of the spin exchange paths in $Cu_2(O_3PCH_2PO_3)$. The numbers 1 through 7 refer to the spin exchange paths J_1 through J_2 , respectively.

Table 2. Geometrical parameters associated with the SE and SSE paths in Cu₂(O₃PCH₂PO₃)^a

(a) SE

Path	Cu···Cu	Cu-O	∠Cu-O-Cu
J_1	3.023	1.966, 1.966	100.5
		2.054, 2.054	94.8
J_2	3.278	2.255, 1.951	102.2
		1.951, 2.255	102.2

(b) SSE				
Path	Cu···Cu	OO	Cu-O	∠Cu-O…O
J_3	4.725	2.518	1.934, 1.966	141.4, 99.4
J_4	4.987	2.526	1.951, 1.951	129.1, 129.1
		2.534	1.934, 1.934	129.3, 129.3
J_5	5.081	2.526	2.255, 1.951	96.3, 129.1
J_{6}	6.115	2.518	1.966, 1.934	159.5, 141.4
J_{7}	6.249	2.533	2.054, 1.951	162.4, 142.4

[&]quot;The bond distances are in unit of angstrom and the bond angles are in unit of degree.

angles are highly symmetrical. The O···O contact distance of the SSE path J_5 consists of the long Cu-O bond that does not contain the magnetic orbitals, and the \angle Cu-O-Cu bond angles are unsymmetrical and close to 90°. The O···O contact distance of the SSE path J_6 is slightly shorter than that of the SSE path J_7 , but the \angle Cu-O-Cu bond angles of the SSE path J_7 are a little more opened compared with those of the SSE path J_6 .

Spin-exchange interactions in magnetic oxides of spin-1/2 Cu^{2-} ions are strongly governed by the arrangement of their $\text{Cu}O_4$ square planes containing the magnetic orbitals. ^{5,60,7} In the magnetic orbital of a $\text{Cu}(O_{eq})_4$ square plane (the oxygen atoms forming the $\text{Cu}O_4$ square plane are referred to as O_{eq}). the $\text{Cu}(3d_{x^2,y^2})$ orbital makes σ antibonding with the 2p orbitals of the four O_{eq} atoms. A crucial factor determining

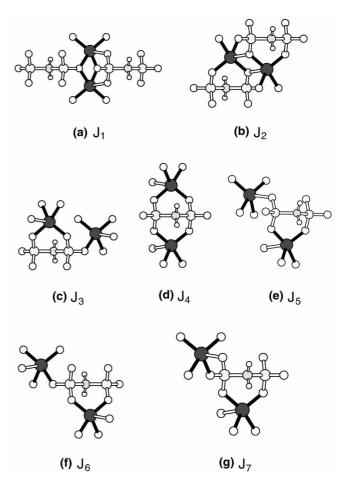


Figure 4. Spin dimers associated with the spin exchange paths J_1 through J_7 in $Cu_2(O_3PCH_2PO_3)$.

the strength of a spin-exchange interaction between Cu²⁻ ions is not the Cu 3d_{x²-y²} orbitals but the O 2p orbitals of their magnetic orbitals (i.e., the "tails of the magnetic orbitals) because the spin exchange between two adjacent Cu²⁺ ions depends on the overlap between their magnetic orbitals, which is, in turn, determined by the overlap between their tails. 5,6c,6e,7 Therefore, from the viewpoint of the magnetic orbital, one might expect that the spin exchange interactions through the SSE paths J_4 , J_6 and J_7 are stronger than those J_3 and J_5 , since the overlap increases as both ∠Cu-O···O bond angles become larger and as the O···O distance becomes shorter and lies within the van der Waals distance and the strength of the SSE interaction is proportional to the overlap S.5,6,12.13 However, it is hard to predict the relative strengths of spin exchange interactions between the SE and SSE paths without electronic structure calculations.

Results of spin dimer analyses for the spin dimers shown in Figure 4 are summarized in Table 3, which shows that the SSE interactions J_4 , J_6 and J_7 are stronger than the SSE interactions J_3 and J_5 , while the SE interactions J_1 and J_2 are negligibly weak. The strongest spin exchange interactions J_4 form isolated spin dimers (Figure 5a), and these dimers interact through the second strongest spin exchange interactions J_6 (with $J_6/J_4 = 0.53$) to form the corrugated two-

Table 3. Values of $(\Delta \varepsilon)^2$ calculated for the SE and SSE interactions of $Cu_2(O_3PCH_2PO_3)$

Path	$(\Delta \varepsilon)^{2 a,b}$	Relative value
J_1	630	0.02
J_2	60	0.00
J_3	890	0.03
J_4	27960	1.00
J_{5}	2600	0.09
J_6	14860	0.53
J_7	8030	0.29

The values of $(\Delta \varepsilon)^2$ are in units of $(\text{meV})^2$. $^6\Delta e^6 = 0$ because the two spin sites are equivalent.

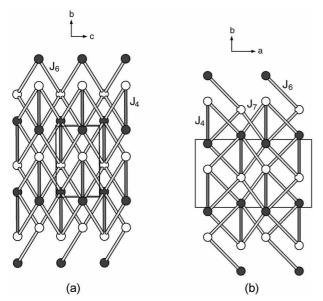


Figure 5. Schematic representation of the AFM spin lattices expected for $Cu_2(O_3PCH_2PO_3)$. (a) 2D AFM lattice made up of J_4 and J_6 , and (b) 3D AFM lattice made up of the 2D AFM lattices connected by J_2 . The red, cvan and yellow cylinders represent the paths J_4 , J_6 and J_5 , respectively, and the gray and white circles indicate spin up and down spin states of Cu^{2+} ion sites, respectively.

dimensional (2D) AFM spin lattice in which each spin site to four adjacent spin sites connected by J_6 . These 2D AFM lattices are connected by the third strongest spin exchange interactions J_7 (with $J_7/J_4 = 0.29$) to form the 3D AFM spin lattice (Figure 5b). All other spin exchange interactions are negligible. For the SSE interactions between two spin sites i and j, we also calculated the overlap integrals S_{ii} between the magnetic orbitals. Note that the magnetic orbital of a spin site is the singly occupied molecular orbital of the spin monomer representing the spin site. In general, the $(\Delta \varepsilon)^2$ values are proportional to the $(S_{ij})^2$ values, which are listed in Table 4. The $(S_0)^2$ values of the SSE paths J_4 , J_6 and J_7 are stronger than the SSE path J_3 and J_5 , which is consistent with the result of the spin dimer analyses. The trend in the relative strengths of overlap integrals can be understood by considering the nature of the magnetic orbital (Figure 2b) and the SSE paths (Figure 4). For the SSE path J_4 , the porbital tails of the magnetic orbitals have a σ -type overlap

Table 4. Values of S_{θ}^2 calculated for the SSE interactions of $Cu_2(O_3PCH_2PO_3)$

Path	$S_{ij}^2 \times 10^6$	Relative value
J_3	4	0.08
J_4	49	1.00
J_5	0.3	0.00
J_6	25	0.51
J_7	16	0.33

through the O···O contacts. For the SSE path J_5 , however, there is no overlap between the magnetic orbitals. Thus, the overlap integral of the SSE path J_4 is much stronger than that of the path J_5 . For the paths J_6 and J_7 , there is only one O···O contact between the magnetic orbitals, so their overlap integrals are weaker than that of the path J_4 . Thus, our spin dimer analysis suggests that, to a first approximation, the magnetic properties can be described in terms of an isolated spin dimer by considering only the strongest spin exchange interaction. This explains the occurrence of a broad maximum (around 50 K) in the magnetic susceptibility of Cu₂-(O₃PCH₂PO₃), and also suggests that Cu₂(O₃PCH₂PO₃) should exhibit a spin gapped character. 7b,17 The latter view is consistent with the fact that the magnetic susceptibility decreases rapidly with decreasing temperature below 50 K.4 The observed magnetic susceptibility does not show a spin gap, but this might be due to the presence of a minute amount of magnetic impurities.

Concluding Remarks

In $Cu_2(O_3PCH_2PO_3)$ the CuO_3 chains made up of edgesharing CuO_5 square pyramidal units are inter-linked by O-P-O bridges. The present work shows that the SE interactions of the CuO_3 chains are negligibly weak compared with the SSE interactions that occur between the CuO_3 chains. The spin exchange interactions of $Cu_2(O_3PCH_2PO_3)$ are dominated by three SSE interactions J_4 , J_6 and J_7 , which leads to a 3D AFM spin lattice. The strongest spin exchange interactions J_4 form isolated spin dimers (Figure 5a), which suggests that, to a first approximation, the magnetic properties can be described in terms of an isolated spin dimer. This in turn suggests that $Cu_2(O_3PCH_2PO_3)$ might be a spin gapped system. Further experimental studies are necessary to verify this prediction.

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