

# 내부자에 의한 위장 공격을 방지하는 개선된 ID 기반 그룹 인증 및 키 합의 프로토콜\*

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## Improved ID-based Authenticated Group Key Agreement Secure Against Impersonation Attack by Insider\*

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### 요약

인터넷에 존재하는 많은 그룹 기반 시스템들은 안전한 통신을 위해 그룹 인증 및 키 합의 (AGKA)를 필요로 한다. 1984년에 Shamir가 ID 기반 암호시스템을 제안한 이후 이 시스템의 공개키 관리 연산 감소를 이용한 ID 기반 AGKA 프로토콜이 지속적으로 연구되고 있다. 이와 관련해서 2006년에 Zhou 등은 두 번의 라운드를 가지면서 통신 및 연산에서 매우 효율적인 ID 기반 AGKA 프로토콜을 제안하였다. 본 논문에서는 이 프로토콜이 임시 그룹 비밀 정보를 소유하고 있는 악성 내부자에 의한 위장 공격에 취약하다는 것을 보이고 이를 개선한 ID 기반 AGKA 프로토콜을 제안한다. 제안된 프로토콜은 악성 공격자가 임시 그룹 비밀 정보를 알고 있더라도 각 구성원의 개인 키를 포함하는 서명을 사용하여 위장 공격이 불가능하도록 설계되었다. 또한 Zhou 등의 프로토콜에서 수행되었던 불필요한 연산을 감소하여 성능 또한 향상시켰다.

### ABSTRACT

Many conference systems over the Internet require authenticated group key agreement (AGKA) for secure and reliable communication. After Shamir [1] proposed the ID-based cryptosystem in 1984, ID-based AGKA protocols have been actively studied because of the simple public key management. In 2006, Zhou *et al.* [12] proposed two-round ID-based AGKA protocol which is very efficient in communication and computation complexity. However, their protocol does not provide user identification and suffers from the impersonation attack by malicious participants. In this paper, we propose improved ID-based AGKA protocol to prevent impersonation attack from Zhou *et al.*'s protocol. In our protocol, the malicious insider cannot impersonate another participants even if he knows the ephemeral group secret value. Moreover, our protocol reduces the computation cost from Zhou *et al.*'s protocol.

**Keywords:** AGKA, group key agreement, ID-based, Impersonation

## 1. Introduction

In many conference systems or applications, the communication between the conference participants is exchanged through insecure channel like the Internet. According to this property of the systems, not only

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honest but malicious users can easily eavesdrop or interrupt the communication. Therefore, the conference participants need their private communication to be secure and reliable, and many solutions for the secure conference system have been proposed so far. Group key agreement (GKA) is one solution for secure communication that more than two entities establish a shared secret key for their communication. Since users can encrypt or decrypt the messages with this established key, the secure and reliable communication can be achieved. In GKA, no participant can pre-determine the value of the established session key. Additionally, GKA with authentication mechanism is called authenticated group key agreement (AGKA) and provides mutual key authentication during group key agreement process.

After Shamir proposed ID-based cryptosystem [1], ID-based AGKA protocols [8-10,12,14,15] have been proposed with the advantage of simple public key management. ID-based cryptosystem uses an identity information as a public key, so it does not need public key infrastructure. Also, Burmester and Desmedt [2] proposed constant-round GKA protocol over the broadcast channel. Communication time is always constant in this protocol because the participants are only required to broadcast once when they want to send a message to all the other participants. Many researchers recently address the above two approaches to design their GKA protocols.

In this paper, we review and analyze Zhou *et al.*'s two-round ID-based constant round AGKA protocol [12] because their protocol is considered to be one of the most efficient ID-based AGKA protocol comparing with the previous protocols. After that, we propose an improved ID-based constant-round AGKA protocol. Our protocol

prevents impersonation attack on Zhou *et al.*'s protocol. We also prove the security of our protocol under DBDH and CDH problems.

Our paper organized as follows: In Section II, we review previous ID-based AGKA protocols. After introducing preliminaries in Section III, we review Zhou *et al.*'s two-round AGKA protocol and suggest how to do impersonation attack by malicious participants in Section IV. We present our improved ID-based AGKA protocol in Section V, and analyze in Section VI. We finally conclude our paper in Section VII.

## II. Related Work

In this section, we briefly review some recent papers about ID-based constant-round AGKA protocols. Choi *et al.* [8] proposed two-round ID-based AGKA protocol based on Burmester and Desmedt's GKA protocol in 2004. However, two papers showed impersonation attacks on this protocol: replay attack by Zhang and Chen [7] and insider colluding attack by Shim [13].

The protocol proposed by Kim *et al.* [9] requires only one communication round, but suffers from replay attack or passive attack because the equation for key computation can be computed from any other users.

Shi *et al.* [10] also proposed one-round AGKA protocol that used different type of ID-based public/private key pair with other protocols; however, Zhou *et al.* [12] showed insider attack that malicious insider can get the session key of any execution on this protocol.

Two AGKA protocols was proposed by Zhou *et al.*: one requires one communication round (ZSM-1) and the other requires two rounds (ZSM-2). ZSM-1 protocol requires much computation per each user and has key control problem. ZSM-2 protocol is efficient in computation, but suffers from

impersonation attack by insider. We discuss the security of the ZSM-2 protocol in Section 4.

In 2008, Choi *et al.* [14] proposed an improved protocol from the previous one. This protocol can prevent passive attack or impersonation by additional signature and session identifiers.

Yao *et al.*'s AGKA protocol [15] requires 3 communication rounds, and each round is for identity authentication, key agreement, and key confirmation. This protocol also can prevent passive attack or impersonation.

### III. Preliminaries

#### 3.1 Security Model and Notions

Our security model follows Katz and Yung's [6] formal security model, which is extended version of Bresson *et al.*'s [4] model. Detailed definitions are described in [6].

**Participants and Initialization.** Each user  $U_i$  in a fixed, polynomial-size set  $P = \{U_1, \dots, U_n\}$  of potential participants have the unique identity  $ID$ . We denote instance  $s \in N$  of player  $U_i$  as  $\Pi_i^s$ .

In this model, an initialization phase occurs before the protocol runs at first. Then each participant  $U_i$  gets public/private keys  $(Q_i, S_i)$  by running an algorithm  $\mathcal{G}(1^k)$ .

**Adversarial Model.** We assume that an adversary  $A$  can control all communications and ask an instance to release session key or long-term key. An adversary's queries are modeled by the following oracles.

*Send*( $U, i, M$ ): Send message  $M$  to instance  $\Pi_U^i$  and outputs the reply generated by this instance.

*Execute*( $U_1, \dots, U_n$ ): Execute the protocol between the players  $U_1, \dots, U_n$  and outputs the transcript of execution.

*Reveal*( $U, i$ ): Output the session key  $sk_U^i$ .

*Corrupt*( $U$ ): Output the long-term secret key  $S_i$ .

*Test*( $U, i$ ):  $A$  asks any of the above queries, and then asks *Test* query only once. This query outputs a random bit  $b$ ; if  $b=1$ , the adversary can access  $sk_U^i$ , and if  $b=0$  he can only access random string.

A passive adversary can ask *Execute*, *Reveal*, *Corrupt*, *Test* queries and an active adversary can ask all above queries including *Send* query.

**Protocol Security.** The advantage of an adversary  $A$  in attacking protocol is defined as

$$Adv_A(k) = |2Pr[Suc] - 1|,$$

where *Suc* is the event that  $A$ 's guess  $b'$  satisfies  $b=b'$  for *Test* query.

The GKA protocol is said to be secure if  $Adv_A(k)$  is negligible for all probabilistic polynomial time (PPT) adversary  $A$ .

#### 3.2 Bilinear Pairing

$G_1$  is a cyclic additive group and  $G_2$  is a cyclic multiplicative group with same order  $q$ . Assume that discrete logarithm problem (DLP) is hard in both  $G_1$  and  $G_2$ . A mapping  $e: G_1 \times G_1 \rightarrow G_2$  which satisfies the following properties is called a bilinear pairing from a cryptographic point of view:

1) Bilinearity:  $e(aP, bQ) = e(P, Q)^{ab}$  for all  $P, Q \in G_1$  and  $a, b \in \mathbb{Z}_q^*$ .

2) Non-degeneracy: If a generator  $P \in G_1$ , then  $e(P, P)$  is a generator of  $G_2$ ; that is,  $e(P, P) \neq 1$ .

3) Computable: There exists an efficient

algorithm to compute  $e(P, Q)$  for all  $P, Q \in G_1$ .

**CDH Problem:** A Computational Diffie-Hellman (CDH) parameter generator  $IG_{CDH}$  is a PPT algorithm takes a security parameter  $1^k$  and outputs additive group  $G_1$  with an order  $q$ .

When an algorithm  $A$  solves CDH problem with an advantage  $\epsilon$ , the advantage is

$$\epsilon = \Pr [A(G, P, aP, bP) = abP],$$

where  $P \in G_1$  and  $a, b \in Z_q^*$ .

**DBDH Problem:** A Bilinear Diffie-Hellman (BDH) parameter generator  $IG_{BDH}$  is a PPT algorithm takes a security parameter  $1^k$  and outputs  $G_1$  and  $G_2$  and bilinear map  $e$ .

When an algorithm  $A$  solves Decisional BDH (DBDH) problem with an advantage  $\epsilon$ , the advantage is

$$\left| \Pr [A(P, aP, bP, cP, e(P, P)^{abc}) = 1] - \Pr [A(P, aP, bP, cP, e(P, P)^d) = 1] \right| \leq \epsilon,$$

where  $P \in G_1$  and  $a, b, c, d \in Z_q^*$ .

## IV. ZSM-2 Protocol

### 4.1 Description

Here we focus on the two-round ID-based AGKA protocol, namely ZSM-2 protocol. Before the session starts, ID-based system setup [5] is done as follows:

**Set Up.**  $G_1$  and  $G_2$  are cyclic groups with order  $q$ .  $e$  is a bilinear pairing,  $P$  is an arbitrary generator of  $G_1$ , and  $H$  denotes a hash function, where  $H: \{0, 1\}^* \rightarrow Z_q^*$ . Key Generation Center (KGC) chooses a random  $s \in Z_q^*$  as the secret master key, and computes  $P_{pub} = sP$ .

$$param = \langle G_1, G_2, q, e, P, P_{pub}, H \rangle$$

**Extraction.** KGC generates the public/private key pair,  $\langle Q_i = H(ID_i), S_i = sQ_i \rangle$ .

There are  $n$  users, from  $U_1$  to  $U_n$ , in a group who want to share a common secret key.  $U_1$  is assumed to be an initiator of the group. Their protocol uses three hash functions,  $H_4: G_2 \rightarrow \{0, 1\}^n$ ,  $H_5: \{0, 1\}^n \rightarrow Z_q^*$ , and  $H_6: G_1 \rightarrow \{0, 1\}^n$ . The protocol works as follows.

**Round 1. Initiator  $U_1$ :**

Pick  $\delta \leftarrow G_2, r \leftarrow \{0, 1\}^n, k_1 \leftarrow Z_p^*$

Compute  $P_i = r \oplus H_4(e(S_1, Q_i) \cdot \delta)$ ,

where  $2 \leq i \leq n$ ,

Compute & broadcast  $D_1$

$$D_1 = \langle \delta, P_2, \dots, P_n, X_1 = H_5(r)k_1P, Y_1 = k_1P_{pub}, L \rangle,$$

where  $L$  is a label containing users' association information.

**Round 2.  $U_i (2 \leq i \leq n)$ :**

Find appropriate  $P_i$  from  $D_1$ .

Then compute  $r' = H_4(e(S_i, Q_i) \cdot \delta) \oplus P_i = r$ ,

Choose  $k_i \leftarrow Z_p^*$  randomly.

Compute & broadcast  $D_i$

$$D_i = \langle X_i, Y_i \rangle = \langle H_5(r)k_iP, k_iP_{pub} \rangle.$$

**Key Computation.** Each user computes

$$z_i = H_6(r)^{-1} X_i (1 \leq i \leq n)$$

Then verify the following equation. If fails, then the protocol halts.

$$e(P, \sum_{j=1}^n Y_j) = e(P_{pub}, \sum_{j=1}^n z_j)$$

**Session Key.**  $K = K_i = H_6(z_1) \oplus \dots \oplus H_6(z_n)$

### 4.2 Impersonation Attack

In ZSM-2 protocol, they did not consider about the existence of malicious participants. Also, their batch verification only executes if the message is correctly

generated with secret value  $r$ , not if the message is sent by correct user. Therefore, the malicious insider who knows the secret value  $r$  can impersonate the other users, that is, impersonation attack by the insider will happen. The following is an attack on the protocol that the legitimated user  $U_m$  impersonates the user  $U_i$ .

Round 2. Malicious insider  $U_m (i \neq m)$  :

Inject the message which is sent to  $U_i$ .

Find appropriate  $P_m$  from  $D_1$ .

Compute  $r' = H_1(e(S_m, Q_1)) \cdot \delta \oplus P_m = r$

Random  $k_i \leftarrow Z_q^*$ ,  $k_m \leftarrow Z_q^*$

Compute & broadcast  $D_i, D_m$

$$D_i = \langle X_i, Y_i \rangle = \langle H_5(r)k_i P, k_i P_{pub} \rangle$$

$$D_m = \langle X_m, Y_m \rangle = \langle H_5(r)k_m P, k_m P_{pub} \rangle$$

Key Computation. All users succeed to verify  $D_i$

$$e(P, \sum_{j=1}^n Y_j) = e(P_{pub}, \sum_{j=1}^n z_j).$$

Session Key.  $K = K_i = H_6(z_1) \oplus \dots \oplus H_6(z_n)$

In Round 2 of the protocol, malicious user  $U_m$  can compute  $\langle X_i, Y_i \rangle$  pair using  $r$  because the computation does not need any private information of  $U_i$ . Then all the other users believe that they agreed session group key with legitimate user  $U_i$  even though  $U_i$  does not exist. This attack can also occur with colluding of several malicious users.

## V. Our Scheme

The impersonation attack by insider on the protocol is possible because their batch verification is not enough to identify each user and only depends on secret value  $r$ . Therefore, we improve the protocol that modify the batch verification in the protocol

to include user's private key  $S_i$  so malicious users cannot impersonate the  $U_i$  even though they get  $r$ . Our protocol uses new hash functions,  $H_1 : G_2 \rightarrow \{0,1\}^{|q|}$ ,  $H_2 : \{0,1\}^{|q|} \rightarrow Z_q^*$ , and  $H_3 : G_1 \rightarrow \{0,1\}^{|q|}$ . The other notations are the same in ZSM-2 protocol. Our protocol runs as follows:

Round 1. Initiator  $U_i$ :

Pick  $\delta, k_i \leftarrow Z_q^*$ ,  $r \leftarrow \{0,1\}^{|q|}$

Compute  $P_i = r \oplus H_1(e(\delta S_i, Q_i))$ ,

where  $2 \leq i \leq n$ ,

Compute & broadcast  $D_1$

$$D_1 = \left\langle \delta, P_2, \dots, P_n, X_1 = H_2(r \| L)k_1 P, \right. \\ \left. Y_1 = k_1 P_{pub} + H_2(r \| L)S_1, L \right\rangle.$$

where  $L$  is a label containing the session information, such as the concatenation of all the user ID's.

Round 2.  $U_i (2 \leq i \leq n)$ :

Find appropriate  $P_i$  from  $D_1$ .

Then compute  $r' = H_1(e(\delta S_i, Q_i)) \oplus P_i = r$ ,

Choose  $k_i \leftarrow Z_q^*$  randomly.

Compute & broadcast  $D_i$

$$D_i = \langle X_i, Y_i \rangle = \langle H_2(r \| L)k_i P, k_i P_{pub} + H_2(r \| L)S_i \rangle.$$

Key Computation. Each user computes

$$z = H_2(r \| L)^{-1} \sum_{i=1}^n X_i = \sum_{i=1}^n k_i P$$

Then verify the following equation. If fails, then the protocol halts.

$$e(P, \sum_{j=1}^n Y_j) = e(P_{pub}, z + H_2(r \| L) \sum_{j=1}^n Q_j)$$

Session Key.  $K = K_i = H_3(z)$

In our AGKA protocol, three points are improved from ZSM-2 protocol. (i) We define  $\delta \leftarrow Z_q^*$  and change the encryption of secret value  $r$  in round 1 that  $\delta$  is multiplied by  $S_i$  in  $G_1$  group. The multiplication in  $G_2$  group takes much more time than in  $G_1$  group in practice so we can reduce the time to

encrypt  $r$  in our protocol. (ii) Multiplication of  $z$  is combined in our protocol to reduce the computation overhead. In key computation process, we use hash function so key control of specific user is still impossible. (iii) The most important feature is that we modify the batch verification. In our protocol, each user broadcasts  $\langle X_i, Y_i \rangle = \langle H_2(r\|L)k_iP, k_iP_{pub} + H_2(r\|L)S_i \rangle$  to verify users. This computation includes the private key of each users so malicious user cannot make this value arbitrary. The batch verification in our protocol can be done with the following equation.

$$\begin{aligned} e(P, \sum_{j=1}^n Y_j) &= e(P, \sum_{j=1}^n (k_j P_{pub} + H_2(r\|L)S_j)) \\ &= e(P, \sum_{j=1}^n (k_j sP) + \sum_{j=1}^n (H_2(r\|L)S_j)) \\ &= e(P_{pub}, \sum_{j=1}^n (k_j P) + \sum_{j=1}^n (H_2(r\|L)Q_j)) \\ &= e(P_{pub}, z + H_2(r\|L)\sum_{j=1}^n Q_j) \end{aligned}$$

## VI. Analysis

In this section, we analyze our ID-based AGKA protocol from the security and performance points of view.

### 6.1 Security

Our goal is to show that our protocol is secure against all types of adversary under DBDH and CDH assumptions. We show the security proof of our protocol in two: encryption and signature schemes.

#### 6.1.1 Encryption

We first assume that an adversary  $A$  gains an advantage from attacking the encryption scheme  $r \oplus H_1(e(\delta S_i, Q_i))$  without forging a signature.

**Theorem 1.** *The encryption scheme in above protocol is secure under the DBDH assumption in the Random Oracle Model (ROM). Namely:*

$$Adv_A \leq 2q_{ex} Adv_G^{DBDH}$$

*Proof.* Let  $A$  be an active adversary and get advantage in attacking the encryption. We consider that  $A$  makes *Execute* query. The distribution of the transcript  $T$  and session group key  $K$ , where  $2 \leq i \leq n$ , is given by:

$$Real = \left[ \begin{array}{l} \delta, k_1 \leftarrow Z_q^*, r \leftarrow \{0,1\}^{q_1}; \\ P_i = r \oplus H_1(e(\delta S_i, Q_i)); \\ r' = H_1(e(\delta S_i, Q_i)) \oplus P_i; \\ X_i = H_2(r\|L)k_iP, Y_i = k_iP_{pub} + H_2(r\|L)S_i; \\ T = \langle \delta, P_2, \dots, P_n, X_1, \dots, X_n, Y_1, \dots, Y_n \rangle; \\ K = H_3(z) \end{array} \right]$$

Consider the distributions *Fake* defined as follows:

$$Fake = \left[ \begin{array}{l} \delta, k_1, b_1, b_i \leftarrow Z_q^*, r \leftarrow \{0,1\}^{q_1}; \\ P_i = r \oplus H_1(e(\delta b_1 P_{pub}, b_i P)); \\ r' = H_1(e(\delta b_1 P_{pub}, b_i P)) \oplus P_i; \\ X_i = H_2(r\|L)k_iP, Y_i = k_iP_{pub} + H_2(r\|L)S_i; \\ T = \langle \delta, P_2, \dots, P_n, X_1, \dots, X_n, Y_1, \dots, Y_n \rangle; \\ K = H_3(z) \end{array} \right]$$

Let  $\epsilon = Adv_G^{DBDH}$  and  $q_{ex}$  is the number of *Execute* queries issued by  $A$ . When choosing  $(T, K)$  pair randomly to ask *Test* query and getting  $b$ ,  $A$  can distinguish  $e(\delta S_1, Q_1)$  and  $e(\delta b_1 P_{pub}, b_1 P)$ , and get bit  $b'$  from guessing with probability  $\epsilon' (\leq \epsilon)$  because he can obtain  $b_1 P, \dots, b_n P$  and  $P_{pub} = sP$  is public. Therefore, we obtain the following equation:

$$\epsilon' = \left| \frac{\Pr [T \leftarrow Real; K \leftarrow Real; A(T, K) = 1]}{\Pr [T \leftarrow Fake; K \leftarrow Fake; A(T, K) = 1]} \right| \leq \epsilon$$

There is a  $H$ -list which contains all the messages that  $A$  queried before. Let  $Ask$  be the event that what  $A$  makes to the *Hash* query is on the  $H$ -list when  $A$  asks *Test* query. The advantage of  $A$  in correctly guessing the session key and breaking the encryption is:

$$\begin{aligned}
 Adv_A(k) &= |2\Pr[Suc] - 1| = |2\Pr[b = b'] - 1| \\
 &= 2\Pr[b = b' | \neg Ask] \Pr[\neg Ask] \\
 &\quad + 2\Pr[b = b' | Ask] \Pr[Ask] - 1 \\
 &= 2\Pr[b = b' | \neg Ask] + 2\Pr[b = b' | Ask] - 1 \\
 &= 2\Pr[b = b' | Ask] \\
 &= 2q_{ax} \epsilon'
 \end{aligned}$$

$A$  cannot gain the advantage without asking for it in ROM, so  $2\Pr[b = b' | \neg Ask] - 1 = 0$ . By adapting a standard hybrid argument, we can have the result that the advantage of  $A$  breaking the encryption as follows:

$$Adv_A \leq 2q_{ax} Adv_G^{DBDH} \quad \square$$

### 6.1.2 Signature

Second, we assume that  $A$  gains an advantage with forging a signature. In our protocol, we use an ID-based signature scheme  $\Sigma$  defined as follows:

**Extract.** Given an identity  $ID$ , compute public key  $Q_{ID} = H(ID)$  and private key

$$S_{ID} = sQ_{ID}.$$

**Sign.** Compute  $Y = kP_{pub} + hS_{ID}$ , where  $k \in \mathbb{Z}_q^*$ ,

$$h = H_2(r\|L); \langle kP, Y \rangle \leftarrow \Sigma_{\geq n}(S_{ID}).$$

**Verification.** Verify  $e(P, Y) = e(P_{pub}, kP + hQ_{ID})$ ,

$$\text{where } h = H_2(r\|L);$$

$$True \text{ or } False \leftarrow \Sigma_{ver}(Q_{ID}, \langle kP, Y \rangle).$$

Here we show the signature scheme  $\Sigma$  is secure against existential forgery on adaptively chosen ID attack as in the following theorem. The proof follows from [8,11].

**Theorem 2.** *Let the hash functions  $H$  and  $H_2$  be random oracles and  $F_0$  be a forger which performs an existential forgery under an adaptively chosen ID with running time  $t_0$ . The forger  $F_0$  can ask queries to the  $H, H_2, Extract$  and  $Sign$  at most  $q_H, q_{H_2}, q_E$ , and  $q_S$  times, respectively. Suppose the advantage of  $F_0$  is  $\epsilon_0 \geq 10q_H(q_{S+1})(q_S + q_{H_2})/(q-1)$ . Then*

*there exists an attacker  $F$  that can solve the CDH problem within the expected time  $t_2 \leq 120686q_H t_0 / \epsilon_0$ .*

We can prove Theorem 2 by proving the following Lemmas.

**Lemma 1.** *Let the hash functions  $H$  be random oracle and  $F_0$  be a forger for an adaptively chosen ID with running time  $t_0$  and advantage  $\epsilon_0$ . Suppose  $F_0$  can ask queries to the  $H$  at most  $q_H$  times. Then a forger  $F$  for a given ID has advantage  $\epsilon_1 \leq \epsilon_0(1-1/q)/q_H$  with running time  $t_1 \leq t_0$ .*

*Proof.*  $F$  is given  $ID^*$ , and we assume that  $F_0$  makes  $H, Extract$  and  $Sign$  queries at most once.  $F$  maintains a list  $L_H$  of  $\langle ID_i, Q_i \rangle$  and interacts with  $F_0$  after choosing  $\alpha \in \{1, \dots, q_H\}$ .

- When  $F_0$  makes  $\alpha$ -th  $H$  query on  $ID$ ,  $F$  returns  $Q^*$  with  $H$  query for  $ID^*$  and inserts  $\langle ID, Q^* \rangle$  into  $L_H$  if  $ID = ID^*$ . Otherwise,  $F$  returns result for  $ID$ , and inserts  $\langle ID, Q \rangle$  into  $L_H$ .
- $F_0$  issues an  $Extract$  query on  $Q_i$ . If  $Q_i = Q^*$ , then  $F$  outputs FAIL; otherwise,  $F$  returns  $S_i$  to  $F_0$  as the result of  $Extract$  query.
- When  $F_0$  issues  $H_2$  query on  $r\|L$ ,  $F$  returns the result  $H_2(r\|L)$ .
- When  $F_0$  makes  $Sign$  query on  $ID_i$ ,  $F$  returns  $\langle ID_i, kP_i, Y_i \rangle$  to  $F_0$ .
- $F_0$  finally outputs  $\langle ID, kP, Y \rangle$  then  $F$  finds  $\langle ID, Q \rangle$  in  $L_H$ . If  $Q = Q^*$ ,  $F$  outputs  $\langle ID^*, kP, Y \rangle$ , otherwise it fails.

Here,  $F$  succeeds the simulation with probability  $1/q$  if  $Q \neq Q^*$  and  $\langle ID, Q \rangle$  is not in  $L_H$  because the output  $\langle ID, kP, Y \rangle$  is independent of the information  $F_0$  accumulated from the previous queries in this case. Therefore, the probability that  $F$  does

not fail the simulation is  $1/q_H(1-1/q)$ .

**Lemma 2.** *Let the hash function  $H$  and  $H_2$  be random oracles and  $F_0$  be a forger for a given  $ID$  who has advantage  $\epsilon_1 \geq 10(q_S+1)(q_S+q_{H_2})/q$  with running time  $t_1$ . Suppose  $F_0$  can ask queries to the  $H, H_2, Extract$  and  $Sign$  at most  $q_H, q_{H_2}, q_E$ , and  $q_S$  times, respectively. Then there exists an attacker  $F$  can solve the CDH problem within expected time  $t_2 \leq 120686q_{H_2}t_1/\epsilon_1$ .*

*Proof.*  $F$  sets the system parameters  $param = \langle G_1, G_2, e, P, P_{pub}, ID, H, H_2 \rangle$ , where  $P_{pub} = xP$ , and gives it to  $F_0$ . Given  $P, xP$ , and  $yP$ ,  $F$ 's goal is to compute  $xyP$  as CDH problem.  $F$  maintains two lists  $L_H = \langle ID_i, a_i, Q_i \rangle$  and  $L_Y = \langle ID_j, k_jP \rangle$ , and interacts with  $F_0$  as follows:

- When  $F_0$  makes  $H$  query on  $ID$ ,  $F$  returns  $Q^* = yP$  for  $ID^*$ ; otherwise  $F$  picks  $a_i \in \mathbb{Z}_q^*$  randomly, adds  $\langle ID_i, a_i, Q_i \rangle$  to  $L_H$ , and returns  $Q_i = a_iP$ .
- $F_0$  issues an  $Extract$  query on  $Q_i$ , if  $Q_i = Q^*$  then  $F$  fails; otherwise,  $F$  finds  $\langle ID_i, a_i, Q_i \rangle$  from  $L_H$  and returns  $S_i = a_iP_{pub} = xQ_i$  to  $F_0$ .
- When  $F_0$  issues  $H_2$  query on  $r||L$ ,  $F$  picks  $h_i \in \mathbb{Z}_q^*$  randomly and returns it.
- When  $F_0$  makes  $Sign$  query on  $ID_i$ ,  $F$  picks  $k_i \in \mathbb{Z}_q^*$  randomly, computes  $k_iP$ ,

and adds  $\langle ID_i, k_iP \rangle$  to  $L_Y$ . Then  $F$  finds  $\langle ID_i, a_i, Q_i \rangle$  from  $L_H$ , computes  $Y_i = k_i xP + h_i a_i xP = k_i P_{pub} + h_i S_i$  and returns  $\langle ID_i, k_iP, h_i, Y_i \rangle$  to  $F_0$ .

Finally,  $F_0$  outputs a valid tuple  $\langle ID^*, kP, h, Y \rangle$  where  $\langle ID^*, kP \rangle$  is not in  $L_Y$  without accessing any oracles except  $H_2$ . If  $F$  replays with the same random tape but different choices of  $H_2$  as in the *forking lemma* [3], then  $F_0$  outputs two valid tuples  $\langle ID^*, kP, h, Y \rangle$  and  $\langle ID^*, kP, h', Y' \rangle$ , where  $h \neq h'$ .

Here,  $F$  can compute  $(Y - Y')/(h - h') = xyP$  as CDH problem if both of them are expected; otherwise, it fails. Therefore, the time for  $F$  is equal to the time for *forking lemma* and the time  $t_2$  is bounded by  $120686q_{H_2}t_1/\epsilon_1$ .

Combining Lemmas 1 and 2, we can obtain Theorem 2 with that the advantage of forger  $F$  in our protocol is negligible.  $\square$

## 6.2 Performance

Table 1 shows communication and computation cost of our protocol comparing with other ID-based AGKA protocols. We use the following notations:

- $n$ : Number of group members
- $\#R$ : Total number of rounds
- $\#U$ : Total number of unicast
- $\#B$ : Total number of broadcast
- $\#Exp$ : Total number of exponentiation

(Table 1) Comparison of Performance

	[8]	[9]	[10]	[12]-1*	[12]-2**	[14]	[15]	Ours
$\#R$	2	1	1	1	2	2	3	2
$\#U$	0	0	$(n-1)^2$	0	0	0	0	0
$\#B$	$2n$	$n$	0	$n$	$n$	$2n$	$3n$	$n$
$\#Exp$	$n(n-1)$	0	0	0	0	$n(n-1)$	0	0
$\#G_1 - M$	$8n$	$n(n+4)$	$n^2$	0	$n(n+3)$	$11n$	$2n(n+3)$	$7n-1$
$\#G_2 - M$	$n(n-1)$	0	0	$2n(n-1)$	$2(n-1)$	$n(n-1)$	0	0
$\#Pair$	$4n$	$n(4n-3)$	$n$	$2n(n-1)$	$3n$	$6n$	$n(n+5)$	$3n$

\*: ZSM-1

\*\* : ZSM-2



# $G_1$ - $M$ : Total number of  $G_1$  multiplication

# $G_2$ - $M$ : Total number of  $G_2$  multiplication

# $Pair$ : Total number of pairings

Our protocol has less multiplication cost than ZSM-2 protocol, and shows even the most efficient protocol in Table 1. Therefore, our proposed protocol can improve both the security and performance of ZSM-2 protocol.

## VII. Conclusion

In this paper, we suggested a deterministic attack on the ZSM-2 protocol that a malicious insider who knows the secret value can impersonate the other user. To prevent this attack, we proposed an improved AGKA protocol which prevents impersonation attack by insider and reduces the computation cost. In our protocol, we used signature including user's private key, so an insider who even gets secret value cannot impersonate other users. Moreover, our protocol reduces multiplication cost in encryption and batch verification. An open problem is to provide perfect forward secrecy if all the previous transcripts and user's private keys are exposed, then the previous session key can be exposed. Except this problem, our protocol improve the security and performance of the previous protocol.

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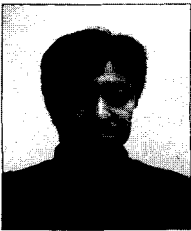
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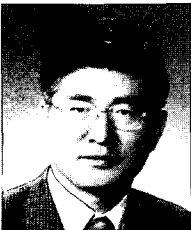
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