

Maximum Efficiency Point Tracking Algorithm Using Oxygen Access Ratio Control for Fuel Cell Systems

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Abstract

The air flow supplied to a fuel cell system is one of the most significant factors in determining fuel efficiency. The conventional method of controlling the air flow is to fix the oxygen supply at an estimated constant rate for optimal efficiency. However, the actual optimal point can deviate from the pre-set value due to temperature, load conditions and so on. In this paper, the maximum efficiency point tracking (MEPT) algorithm is proposed for finding the optimal air supply rate in real time to maximize the net-power generation of fuel cell systems. The fixed step MEPT algorithm has slow dynamics, thus it affects the overall efficiency. As a result, the variable step MEPT algorithm is proposed to compensate for this problem instead of a fixed one. The complete small signal model of a PEM Fuel cell system is developed to perform a stability analysis and to present a design guideline. For a design example, a 1kW PEM fuel cell system with a DSP 56F807 (Motorola Inc) was built and tested using the proposed MEPT algorithm. This control algorithm is very effective for a soft current change load like a grid connected system or a hybrid electric vehicle system with a secondary energy source.

Key Words: Air flow control, Fuel cell system, Fuel efficiency, Maximum efficiency point, MEPT algorithm

I. INTRODUCTION

Fuel cells are drawing the attention of the governments all over the world, because they have a lot of excellent characteristics such as high efficiency, environment friendliness and so on[1]-[4]. Especially, proton exchange membrane (PEM) fuel cells have high power density and efficiency. Also, they operate at a low temperature and start up rapidly when compared to other fuel cells [5].

A fuel cell (FC) system has a movable operating point according to the output current of the FC, which determines the FC stack voltage represented as a voltage source. Since the consumption rate of hydrogen fuel is proportional to the output current[6], [7], the operating point determines the amount of fuel used. The controller in a FC system adjusts the compressor operation in order to regulate the humidified air supply for the required power generation. Fig. 1 shows an entire FC system diagram displaying the controlling parameter W_{air_ref} and the process.

The conventional method of controlling the air flow is to fix the oxygen supply at a constant rate as required for the

FC reaction. By the rule of thumb, the oxygen access ratio (λ_{O_2}) is typically recommended to be pre-set to the value 2[7]-[12]. However, the actual optimal point can deviate from the pre-set value due to various operating conditions such as very light or heavy load situations. In fact, the experimental measurements of the FC system in this paper show that the optimal supply rate varies very sensitively according to given operating condition changes, staying far away from a pre-set value λ_{O_2} , thus degrading the power generation performance. To compensate for this problem, recent literature has proposed a λ_{O_2} tracking control method using a linearized model[13]-[16]. However, the maximum ratio varies according to FC stack aging and environmental factors such as temperature and humidity variation directly affect the air pressure[17]. Also, an exact linearized re-model is necessary to apply the model-based tracking algorithm to another FC system. Hence an algorithm which maximizes the net power by supplying an amount of air for optimal control without any effects from those conditions must be developed[18].

In this paper, a maximum efficiency point tracking (MEPT) algorithm based on the perturbation and observation (P&O) method is proposed for finding the optimal air supply rate to maximize the net-power generation of an FC system. A MEPT algorithm using a 'variable' step size is proposed, and its performance is compared with a fixed step MEPT

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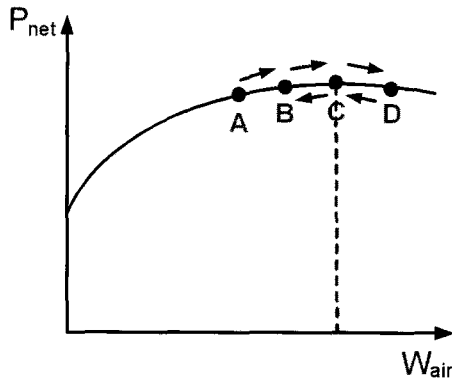


Fig. 5. Operation of the fixed step MEPT Algorithm.

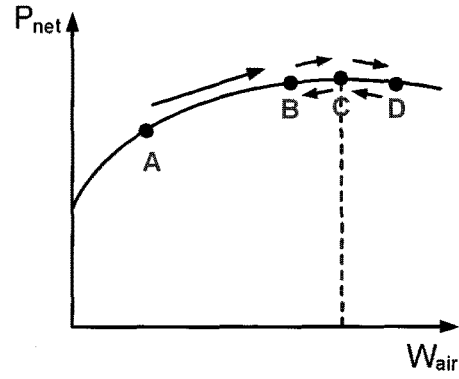


Fig. 7. Operation of the variable step MEPT Algorithm.

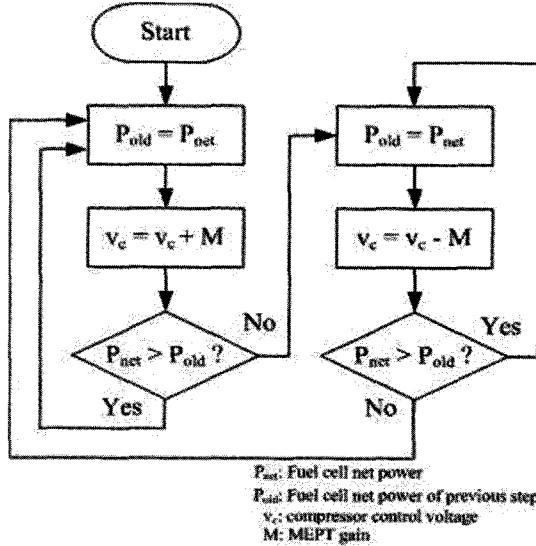


Fig. 6. Fixed step MEPT Algorithm flow chart.

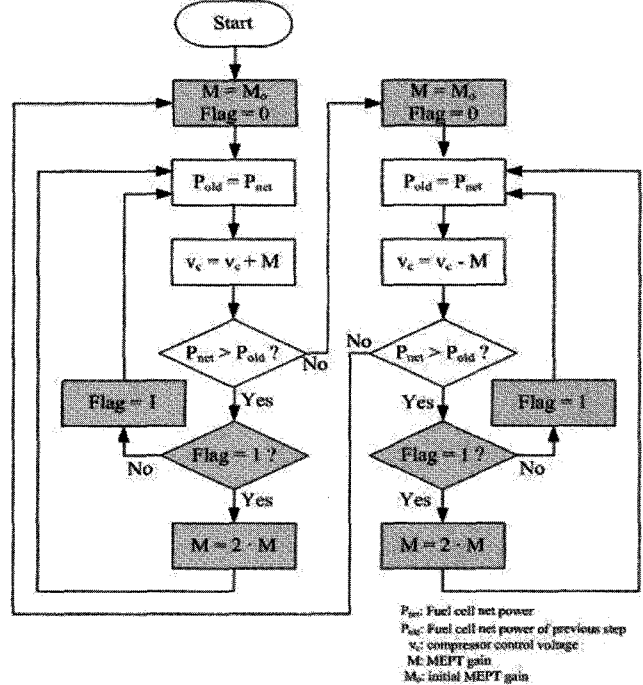


Fig. 8. Variable step MEPT Algorithm flow chart.

to maximize the net-power generation of FC systems.

A. Fixed step MEPT Algorithm

The most basic MEPT algorithm suggested in this paper is used for tracking the optimal efficiency point using a fixed step size (M). This tracking operation is shown in Fig. 5. The MEPT algorithm changes the amount of air supplied to the FC and then compares the current net power (P_{net}) with the previous one (P_{old}). It then alters the amount of air supplied to reach the greatest power-generation point. The amount of air supply is controlled by the air compressor reference voltage (v_c). A flow chart of the fixed step MEPT algorithm is shown in Fig. 6.

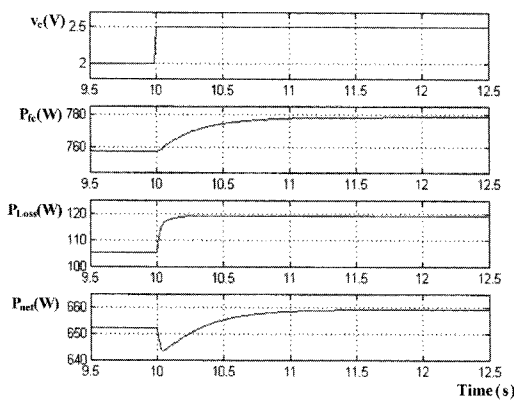
B. Variable step MEPT Algorithm

The fixed step algorithm has a slow dynamic in MEPT, especially when the initial operating point is far away from the optimal point, which affects the overall efficiency. Therefore, the variable step MEPT algorithm is proposed to compensate for this problem instead of the fixed one (see Fig. 7). The fundamental operation of the variable step MEPT algorithm is based on the previous one. As a result, the steady state operation is same as with the fixed step MEPT algorithm. However, the variable step MEPT algorithm increases the

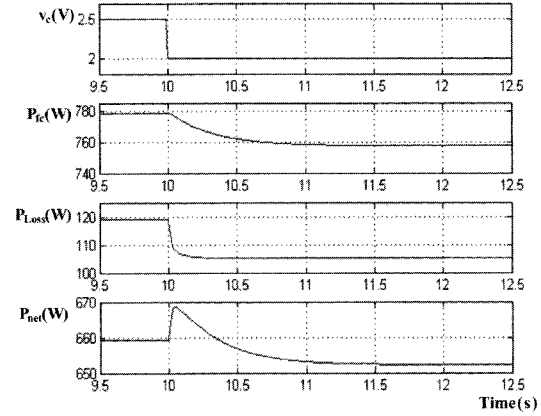
step size when the reference of the MEPT controller moves unidirectional for more than 2 sampling cycles, since it is assumed that the operating position is far from the maximum peak point. In this procedure, the parameter 'Flag' is used to determine the previous reference's direction. On the other hand, the MEPT controller resets the step size ' M_0 ' (the same as the fixed step MEPT algorithm gain) when current net power is smaller than the previous one. This operation is marked with a gray color in flow chart (see Fig. 8).

III. DYNAMIC ANALYSIS OF THE MEPT ALGORITHM

The operation of the proposed MEPT algorithm is based on the perturbation and observation (P&O) method which compares the net power before-and-after the air pressure reference update. The sampling period for the measurement of the net power should be long enough to obtain stable data from the system when the air supply changes. Fig. 9 shows the transient response of the stack and the net power when the air compressor reference is step-changed. The dissipated power of the compressor increases faster than the power generated in the FC stack. Therefore, the net power in the graph shows



(a) Air compressor reference step up.



(b) Air compressor reference step down.

Fig. 9. Dynamic analysis of fuel cell system.

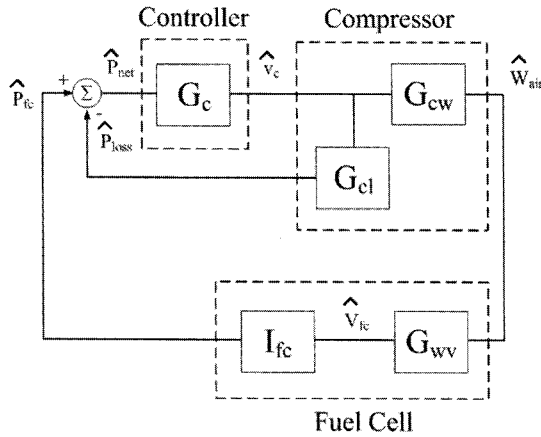


Fig. 10. Control block diagram of the FC power system for the proposed MEPT algorithm.

a decrease when the compressor reference increases stepwise. Therefore, an excessively high sampling frequency for the measurement of the algorithm results in an incorrect decision. The MEPT algorithm has a performance trade-off between the sampling period and the step size for stable operation. Therefore, the dynamic response analysis of the FC system including the air compressor should be considered when designing these two factors. Fig. 10 shows the small-signal transfer function model of an FC system with the MEPT algorithm.

A. Fuel cell transfer function

Using eq. (1), the transfer function from the partial pressure of the cathode to the FC output voltage is derived by the perturbation and linearization technique as follows:

$$\frac{\hat{v}_{fc}}{\hat{p}_{O_2}} = 8.75 \times K_{pO_2} \times (T_{fc} - 298.15). \quad (2)$$

Since oxygen makes up 21% of the total air supply, the transfer function from the air flow of the compressor to the partial pressure of the cathode can be easily derived by

multiplying the transfer function of the oxygen flow to the partial pressure of the cathode by 0.21.

$$\begin{aligned} \frac{\hat{p}_{O_2}}{\hat{w}_{air}} &= \frac{\hat{w}_{O_2}}{\hat{w}_{air}} \cdot \frac{\hat{p}_{O_2}}{\hat{w}_{O_2}} \\ &= 0.21 \cdot \frac{1}{k_{ca}} \cdot \frac{1}{\left(1 + \frac{s}{A_{O_2} \cdot k_{ca}}\right)} \end{aligned} \quad (3)$$

where $A_{O_2} = \frac{R_{O_2} \cdot T_{fc}}{V_{ca}}$

R_{O_2} : gas constants of oxygen (J/mol·K)

V_{ca} : cathode channel volume (m³)

k_{ca} : orifice constant.

Considering eq. (2) and (3), the total open-loop transfer function of the FC system G_{wv} is derived as follows:

$$\begin{aligned} G_{wv} &= \frac{\hat{v}_{fc}}{\hat{w}_{air}} = \frac{\hat{p}_{O_2}}{\hat{w}_{air}} \cdot \frac{\hat{v}_{fc}}{\hat{p}_{O_2}} \\ &= 1.84 \times K_{pO_2} \times (T_{fc} - 298.15) \times \frac{1}{k_{ca}} \cdot \frac{1}{\left(1 + \frac{s}{A_{O_2} \cdot k_{ca}}\right)}. \end{aligned} \quad (4)$$

B. Air compressor transfer function

The dynamic response of the air compressor is almost ten times faster than that of the FC system derived from the previous dynamic analysis. An approximation assuming that the transfer function of the air compressor is constant is allowed due to a fast dynamic response with a negligible error when the control loop design for the MEPT algorithm is used.

$$\begin{aligned} G_{cw} &= \frac{\hat{w}_{cp}}{\hat{v}_c} = K_w \\ G_{cl} &= \frac{\hat{P}_{Loss}}{\hat{v}_c} = K_l. \end{aligned} \quad (5)$$

C. Total transfer function (without the MEPT algorithm)

The total system transfer function, except the MEPT algorithm control loop using the previous transfer functions, is as

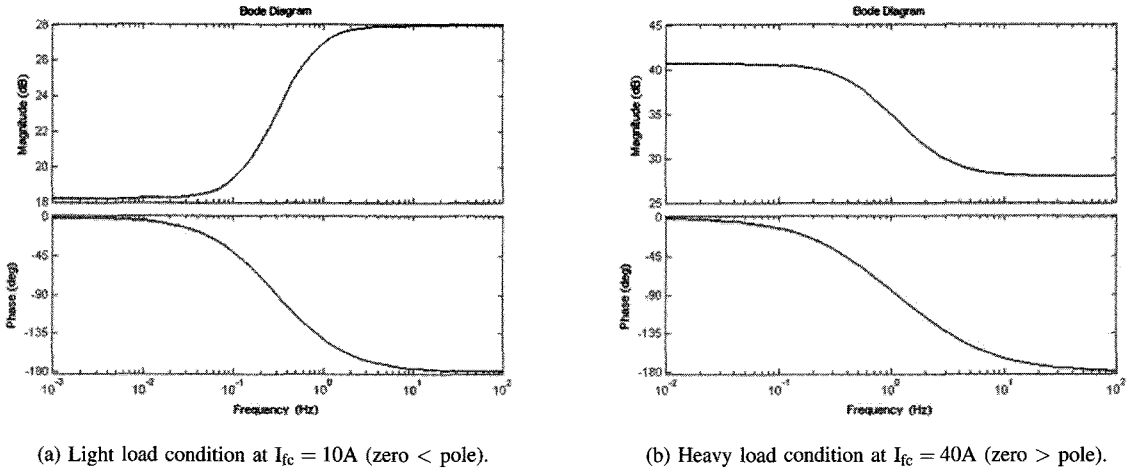


Fig. 11. Total transfer function without MEPT algorithm. $\left(\frac{\hat{P}_{net}}{\hat{v}_c}\right)$

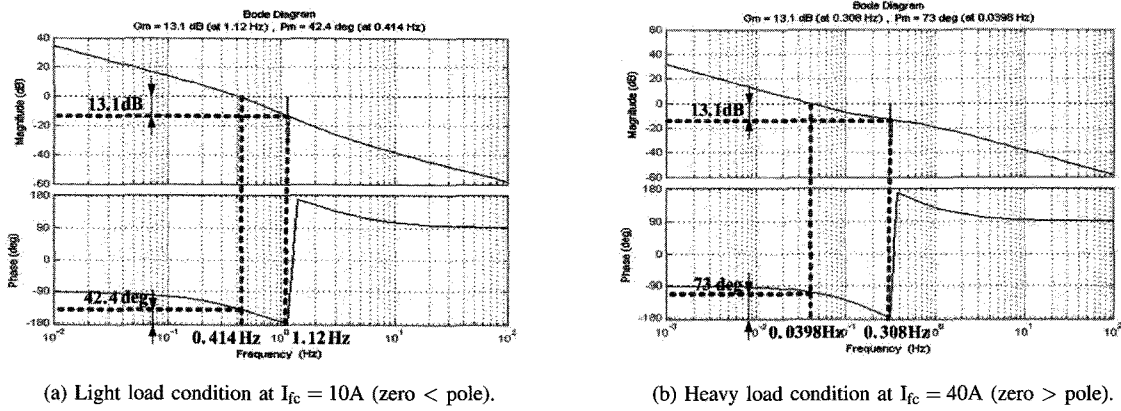


Fig. 12. Phase margin of MEPT algorithm (T_{mept}).

follows:

$$\begin{aligned} \frac{\hat{P}_{net}}{\hat{v}_c} &= I_{fc} \cdot G_{wv} \cdot G_{cw} - G_{cl} \\ &= \left(\frac{K_{fc} \cdot I_{fc}}{k_{ca}} - K_l \right) \cdot \frac{1 - \frac{s}{w_z}}{1 + \frac{s}{w_p}} \end{aligned} \quad (6)$$

$$\begin{aligned} w_z &= \left(\frac{K_{fc} \cdot I_{fc}}{K_l \cdot k_{ca}} - 1 \right) \cdot A_{O_2} \cdot k_{ca} \\ w_p &= A_{O_2} \cdot k_{ca} \end{aligned}$$

As shown in eq. (6), the transfer function has a left half-plane pole and a right half-plane (RHP) zero. Since the RHP zero moves according to the FC's output current and may lie within the range which affects the MEPT algorithm's behavior, the dynamic response should be carefully analyzed under heavy and light load conditions. Depending on the relative location of the pole and zero, the transfer function has different bode plots, which are shown in Fig. 11.

D. MEPT controller transfer function

The mathematical relation, under steady-state operation, of the two proposed MEPT algorithms can be established as

follows:

$$v_c(k+1) = v_c(k) + M \text{sgn} \left(\frac{\Delta P_{net}}{\Delta v_c} \right) \quad (7)$$

where M is the variation step size of the air compressor reference.

This relation can be expressed with an integrator including the sampling time of the control command update as follows[20]:

$$G_c = \frac{\hat{v}_c}{\hat{P}_{net}} = \frac{M}{T_s \cdot s} \quad (8)$$

where T_s : sampling time of the controller.

E. Design of the MEPT algorithm

Using the eq. (6) and (8), the closed loop gain of the total system including the MEPT control is derived as eq. (9). The loop gain also has different dynamic characteristics according to the relationship between the pole and the zero.

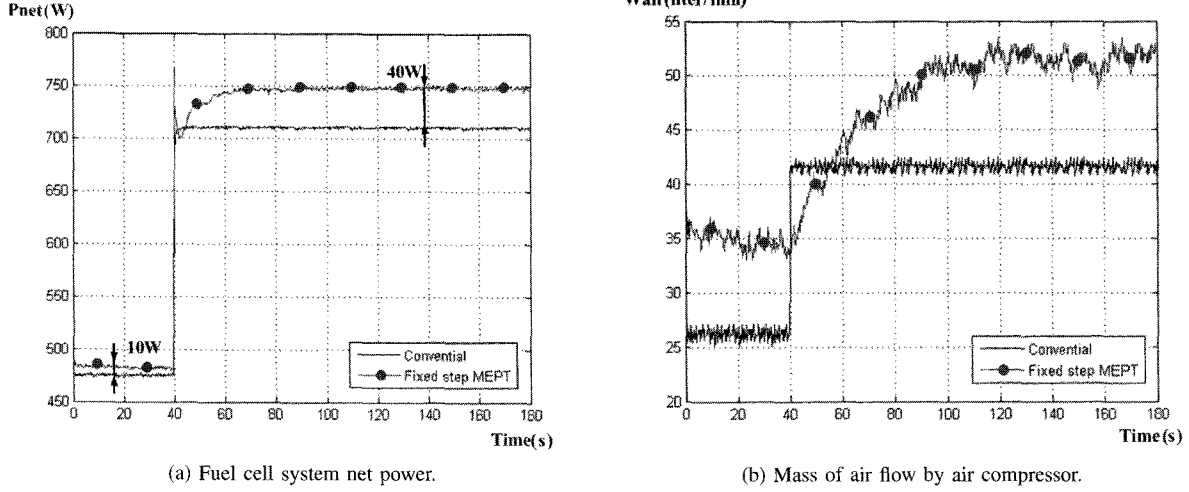


Fig. 13. Comparison of the experimental results between a conventional algorithm and the fixed step MEPT algorithm (15A to 25A load condition).

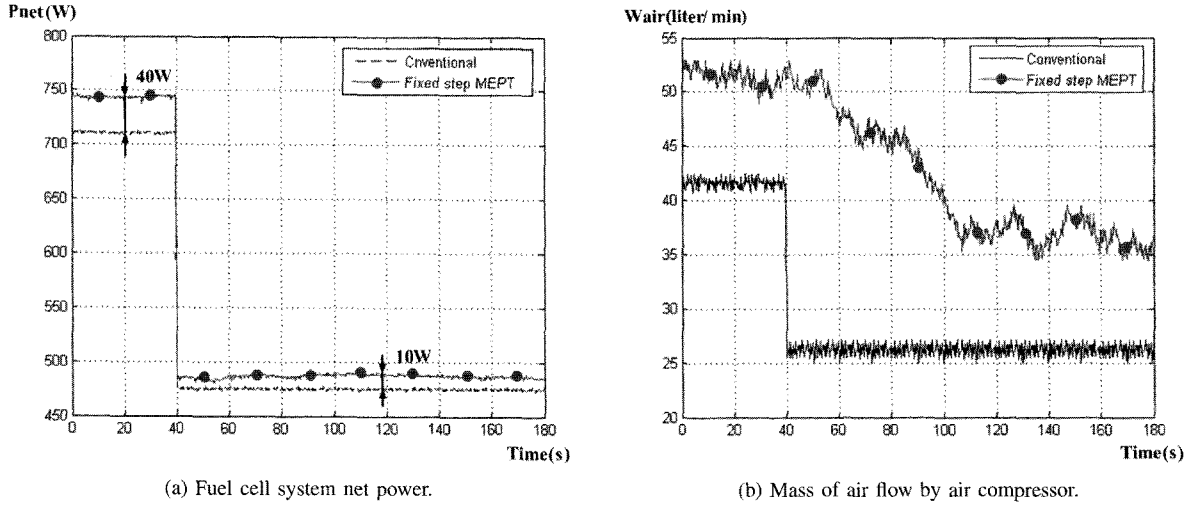


Fig. 14. Comparison of the experimental results between a conventional algorithm and the fixed step MEPT algorithm (25A to 15A load condition).

$$\begin{aligned}
 T_{mept} &= \frac{\hat{P}_{net}}{\hat{v}_c} \cdot \frac{\hat{v}_c}{\hat{P}_{net}} \\
 &= \left(\frac{K_{fc} \cdot I_{fc}}{k_{ca}} - K_l \right) \cdot \frac{M}{T_s} \cdot \frac{1}{s} \cdot \frac{1 - \frac{s}{w_z}}{1 + \frac{s}{w_p}} \quad (9)
 \end{aligned}$$

As shown in Fig.11., the zero dominantly affects the dynamic response and the stability when the right half-plane zero is located lower than the left half-plane pole in the bode plot, otherwise the pole dominates. For a phase margin that is greater than 45° , the following requirements should be satisfied [21],[22]:

$$\begin{aligned}
 \frac{M}{T_s} &< \frac{A_{O_2} \cdot k_{ca}}{K_l} \quad (\text{for } w_z < w_p) \\
 \frac{M}{T_s} &< \frac{A_{O_2} \cdot k_{ca}^2}{K_{fc} \cdot I_{fc} - K_l \cdot k_{ca}} \quad (\text{for } w_z < w_p) \quad (10)
 \end{aligned}$$

In this paper, the sampling time was 1 sec. in order to obtain a fast dynamic response. This leads to selecting 0.03

for the air-compressor step parameter M from eq. (10). The total system closed loop response is presented as shown in Fig. 12. The loop gain has about a 45° phase margin under the heavy load condition for control stability.

IV. EXPERIMENTAL RESULTS

In this paper, a 1kW PEMFC system is used to verify the MEPT algorithm. The system's output current and voltage operate between 0A(45V) to 40A(25V). A 16 bit digital signal processor 56F807 (Motorola Inc) is used as a system controller for the MEPT algorithm.

The experimental results with the FC system compare the performance of the two algorithms, which are the conventional control with a constant oxygen access ratio ($\lambda_{O_2} = 2$) and the fixed step MEPT. Fig. 13 shows the results of a 15A to 25A step up load current and Fig. 14 shows a 25A to 15A step down load current by electric load. The results show that the MEPT algorithm produces a higher net power than the conventional one by 10W at the 15A load condition

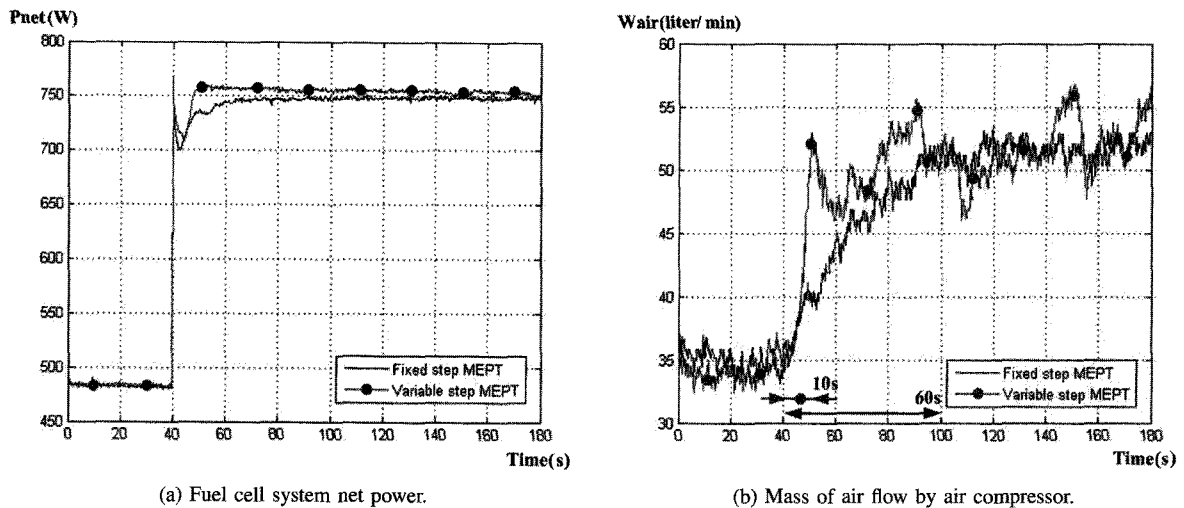


Fig. 15. Comparison of the experimental results between the fixed step MEPT and the variable step MEPT algorithm (15A to 25A load condition).

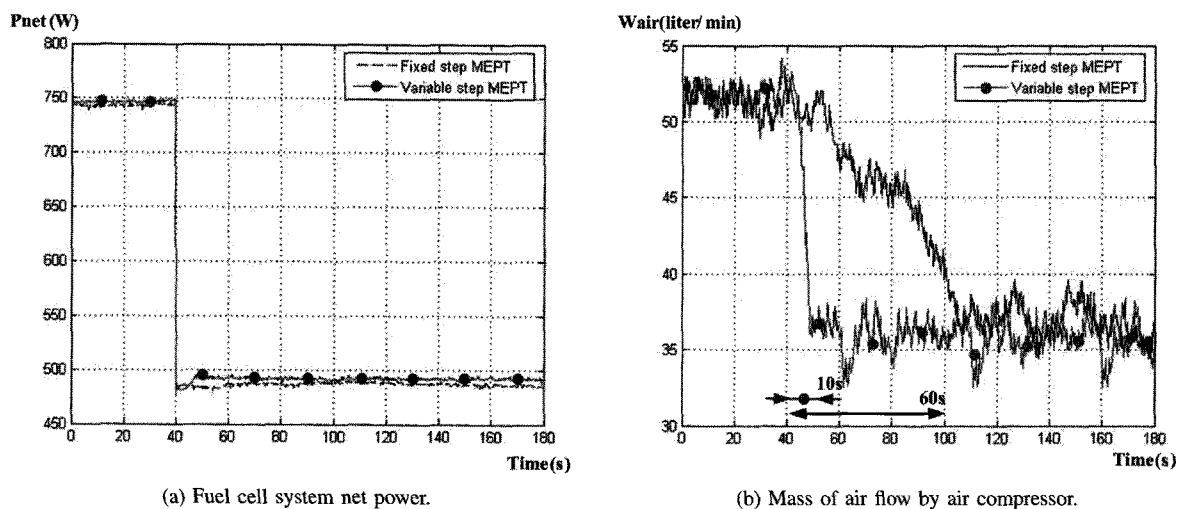


Fig. 16. Comparison of the experimental results between the fixed step MEPT and the variable step MEPT algorithm (25A to 15A load condition).

and by 40W at the 25A load condition. The net power and the amount of air supplied measured under the same load condition as the previous experiment is presented in Fig. 15 and 16 for a performance comparison between the fixed step MEPT algorithm and the proposed variable step MEPT algorithm. The fundamental operation of the variable MEPT algorithm is the same as that of the fixed step MEPT algorithm, so the steady state net power is same as the previous one. At a given load change, the results show that the variable step MEPT algorithm has a faster tracking speed with a settling time of 10s, compared to the fixed step MEPT algorithm with a settling time of 60s.

V. CONCLUSIONS

In this paper, optimal oxygen ratio tracking algorithms with a fixed step size and a variable step size are proposed for fuel cell systems. The variable step MEPT algorithm automatically adjusts the step size based on the distance between the maximal efficiency point and the current operating point of

the FC. Through small signal modeling, it is verified that the proposed algorithm is stable for all operating cases. For verification of the proposed algorithm, a 1kW fuel cell system with a DSP 56F807 was built and tested. The result shows that the proposed algorithm produces a higher net power than the conventional one by 10W at a 15A load condition and by 40W at a 25A load condition. Furthermore, the variable step MEPT algorithm has a faster tracking speed with a settling time of 10s, compared to the fixed step MEPT algorithm with a settling time of 60s. Since there exists the chance of optimizing the way to change the step size of a MEPT algorithm, the proposed variable step algorithm in this paper suggests a direction for improving the response.

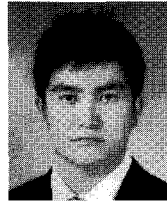
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