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# Throughput Maximization for Cognitive Radio Users with Energy Constraints in an Underlay Paradigm

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#### Abstract

In a cognitive radio network (CRN), cognitive radio users (CUs) should be powered by a small battery for their operations. The operations of the CU often include spectrum sensing and data transmission. The spectrum sensing process may help the CU avoid a collision with the primary user (PU) and may save the energy that is wasted in transmitting data when the PU is present. However, in a time-slotted manner, the sensing process consumes energy and reduces the time for transmitting data, which degrades the achieved throughput of the CRN. Subsequently, the sensing process does not always offer an advantage in regards to throughput to the CRN. In this paper, we propose a scheme to find an optimal policy (i.e., perform spectrum sensing before transmitting data or transmit data without the sensing process) for maximizing the achieved throughput of the CRN. In the proposed scheme, the data collection period is considered as the main factor effecting on the optimal policy. Simulation results show the advantages of the optimal policy.

Index Terms: Cognitive radio, Data collection period, Energy constraints, Maximizing throughput, Optimal policy

## I. INTRODUCTION

In cognitive radio network (CRN) [1, 2], to avoid interference with the operation of the primary users (PUs), the cognitive radio users (CUs) often follow one of two paradigms, underlay or overlay paradigms. In the overlay paradigm, the CU is allowed to access the channel only when the PU signal is absent. The underlay paradigm allows the CU to access to the licensed channel, if the interference causes the PU to be below a given threshold.

Due to the limited power supply, energy efficiency becomes an essential part of cognitive radio users and it attracts many researchers such as in [3, 4]. In the CRN, a longer sensing time may consume more energy and reduce the transmission time in a time-slotted manner, which degrades the achieved throughput of the CRN. Therefore, spectrum sensing does not always provide better throughput to the CRN. Most previous studies that have investigated how to improve energy efficiency of the CRN consider spectrum sensing as a requirement before data transmission [5, 6]. The optimal sensing time for maximizing throughput is presented in [6]. In [7, 8], the scheme for finding an optimal action policy, including sleeping to save energy or active (i.e., perform spectrum sensing) to take an opportunity to transmit data, is proposed. The proposed scheme applies the partially observable Markov decision process (POMDP) [9, 10] to determine that optimal action policy.

In most previous works, the data collection period (i.e., within the period, the data needs to be transmitted to the receiver) was not considered to decide the action for energy efficiency. However, the data collection period is common

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in real world applications. For example, talking or alarm data require immediate transmission; and environment information such as location, humidity and temperatures require being transmitted within a certain period. In this paper, we consider the data collection period as a main factor for determining an optimal operation policy in order to maximize the throughput of the CRN with energy constraints in an underlay paradigm. We classify the operations of the CRN as two types: spectrum sensing before data transmission and data transmission without spectrum sensing. It is expected that the proposed scheme will provide the CRN an improved throughput in comparison with conventional systems.

## **II. SYSTEM MODEL**

We consider a PU network, which is assumed to operate in a time-slotted manner, and a CRN with a pair of CUs, a CU transmitter (CUtx) and a CU receiver (CUrx). The system model is shown in Fig. 1. The probabilities of absence and presence of the PU signal are defined as  $p_0$  and  $p_1$ , respectively. In this paper, we assume that the distance between the CUtx and CUrx is small compared to the distance between the CUtx and the PU receiver (PUrx), and then the CUtx is able to adjust its transmission power in order to not affect the PU link while still delivering data to the CUrx. This means that the CRN follows the underlay paradigm for the operations.

The CUtx is powered by a battery with a capacity  $E_c$  in units of energy and always has data to transmit to the CUrx. However, the CUrx only accepts the incoming data within a data collection period  $n_{s_r}$ . We define  $e_s$  and  $e_t$  as the energy consumed for spectrum sensing and data transmitting in a time unit, respectively. The transmission energy  $e_t$  is the energy that the CUtx spends to transmit data in order to maintain the received signal-to-noise ratio (SNR) level (SNR<sub>CU</sub>) at the CUrx.

The CUtx utilizes an energy detector to monitor the activity of the PU. The Gaussian noise is considered in the sensing channel. When the number of sensing samples is relatively large (e.g.,  $M \ge 200$ ), the received signal energy *xE* from the detector can be closely approximated as a Gaussian random variable under both hypotheses of the PU signal [11]. So that, we have,

$$xE \square \begin{cases} N(M, 2M) & H_0 \\ N(M(\gamma+1), 2M(2\gamma+1)) & H_1 \end{cases},$$
(1)

where  $\gamma$  is the signal-to-noise ratio (SNR) of the sensing channel between the CUtx and the PU transmitter (PUtx), *M* is the number of samples over a sensing interval,  $H_0$  and  $H_1$ 



Fig. 1. System model of the proposed scheme.

are the absence and presence hypothesis of the PU signal, respectively.

According to the received signal energy xE, the decision on the PU status can be made as follows:

$$\begin{cases} G = 1 \text{ (the PU signal is presence)}, & \text{If } xE \ge \lambda \\ G = 0 \text{ (the PU signal is presence)}, & \text{otherwise,} \end{cases}$$
(2)

where  $\lambda$  is the energy threshold for a local decision.

The sensing performance of the CUtx can be evaluated by the probability of detection  $(p_d)$  and the probability of false alarm  $(p_f)$ , which are given, respectively, as [11]:

$$p_{d} = Q\left(\frac{\lambda - M\left(\gamma + 1\right)}{\sqrt{1M\left(2\gamma + 1\right)}}\right),\tag{3}$$

and

$$p_f = Q\left(\frac{\lambda - M}{\sqrt{2M}}\right). \tag{4}$$

When the CUtx transmits data and the PU is absence, the CUtx-CUrx link can achieve the throughput

$$C_0 = \log_2\left(1 + SNR_{CU}\right),\tag{5}$$

where  $SNR_{CU}$  is the SNR in the CUtx-CUrx link.

On the other hand, when the CUtx transmits concurrently

with the PUtx, the signal that the CUrx receives from the PUtx will be considered as noise. In this case, the CUtx-CUrx link can achieve the throughput

$$C_1 = \log_2\left(1 + \frac{SNR_{CU}}{1 + SNR_{PU}}\right),\tag{6}$$

where  $SNR_{PU}$  is the SNR in the PUtx-CUrx link.

It can be seen that the appearance of the PU signal may reduce the achieved throughput of the CUtx-CUrx link, meaning that  $C_I$  is always smaller than  $C_0$ .

#### **III. AN OPTIMAL POLICY FOR CU OPERATION**

In this section, we consider the data collection period as the main factor for deciding an optimal operation policy of the CRN. The operations of the CRN will be classified into two types. First, the CUtx performs spectrum sensing; if the sensing result is "the PU signal is absent", the CUtx will transmit data; otherwise, the CUtx will keep silent and wait for the next time slot. The first operation type may avoid a collision with the PUtx, making energy use more efficient. However, it must wait for a free time slot to transmit data that may take a long time, allowing the data collection period to potentially end. Second, the CUtx transmits data immediately during the entire time slot without a sensing process. This operation type may guarantee to transmit data within a short data collection period, but collisions with the PU network may occur, which reduces the received SNR at the CUrx. This may result in the achieved throughput of the CRN being reduced. In this paper, we propose a scheme to determine an optimal policy for CU operations that can maximize the total achieved throughput of the system during the data collection period.

We define the operations of the CR network as  $\Theta \in \{SS\_DT, DT\}$ , where  $\Theta = SS\_DT$  is the first operation type; the CUtx performs spectrum sensing before deciding to transmit data or not, and  $\Theta = DT$  is the second operation type; the CUtx transmits data in whole time slot without sensing process. According to the operation types, the CR network can achieve different throughput and consume different energy.

# A. The First Operation Type: The CU Performs Spectrum Sensing before Deciding Transmit Data or Not (Θ = SS\_DT)

If the CR network executes this operation type, it will achieve the average throughput as

$$TH(SS_DT) = \left(\frac{T - t_s}{T}\right) \left(C_0 \left(1 - p_f\right) p_0 + C_1 \left(1 - p_d\right) p_1\right), (7)$$

where *T* is length of a time slot,  $t_s$  is the sensing time,  $p_0$  and  $p_1$  are the probability of absence and presence of the PU signal, respectively.

The average energy consumption can be given as,

$$E(SS_DT) = e_s t_s + e_t t_t \left( (1 - p_f) p_0 + (1 - p_d) p_1 \right), (8)$$

where  $t_t = T - t_s$  is the transmission time.

The expected lifetime (i.e., the maximum number of time slots that the CR network can be powered by the battery) of the CR network can be computed as,

$$ns(SS\_DT) = \frac{E_c}{E(SS\_DT)}.$$
(9)

# B. The Second Operation Type: The CU Transmits Data in whole Time Slot without Sensing Process (Θ = DT)

In this operation type, the CR network transmits data in whole time slot T. Therefore, the average throughput will be given as

$$\mathrm{TH}(DT) = C_0 p_0 + C_1 p_1.$$
(10)

The average energy consumption can be given as

$$E(DT) = e_t T. \tag{11}$$

Subsequently, the expected lifetime of the CR network can be computed as

$$ns(DT) = \frac{E_c}{E(DT)}.$$
(12)

#### C. Problem Formulation

Due to the data collection period of the CR network, only the data arrives the CUrx within  $n_{s,r}$  time slots is eligible. Other data arrival late will not be accepted. Therefore, the total achieved throughput of the CR network for the first operation type and second operation type can be given, respectively, as

$$R(SS\_DT) = TH(SS\_DT)(I(ns(SS\_DT), n_{s\_r})n_{s\_r} + I(n_{s\_r}, ns(SS\_DT))ns(SS\_DT)),$$
(13)

and

$$R(DT) = TH(DT)(I(ns(DT), n_{s_r})n_{s_r} + I(n_{s_r}, ns(DT))ns(DT)),$$
(14)

where I(a, b) is defined as,

$$I(a,b) = \begin{cases} 1, \text{ if } a \ge b \\ 0, \text{ otherwise.} \end{cases}$$
(15)

The optimal policy of the CU operation can be determined as

$$\Theta_{opt} = \underset{\Theta \in \{SS\_DT, DT\}}{\arg \max} \left( R(\Theta) \Big| E_c, e_t, p_0, n_{s\_r} \right).$$
(16)

The solution of the optimization problem in Eq. (16) can be found by using numerical method [12].

In order to evaluate complexity of the proposed scheme, we mentioned that the proposed scheme needs to calculate the expected throughput of the first and second operations while the conventional scheme which just fixes the operation as the first or second one without any mathematical cost. Hence, if it is assumed that the complexity of the conventional scheme is O(N), the complexity of the proposed scheme will be O(N+2).

#### **IV. SIMULATION RESULTS**

In this section, we present the simulation results to prove the efficiency of the proposed scheme. The performances of the first operation type, the second operation type and the random policy are also shown for references. The random policy will randomly perform the second operation type with the probability  $p_0$ . We consider SNR of the CUtx-CUrx link as  $SNR_{CU} = 10$  dB, and the interference of the PUtx-CUrx link will be  $SNR_{PU} = 10$  dB.

Fig. 2 shows the total achieved throughput of the considered schemes according to the probability of absence  $(p_0)$  of the PU signal. Actually, all of the schemes have better performance when  $p_0$  increases. It can be seen that the random policy is the worst scheme with the least total achieved throughput. On the other hand, the proposed scheme has the best performance. When  $p_0$  is low (i.e.,  $p_0 \leq 0.4$ ), the second operation type can obtain a higher total achieved throughput than that of the first operation type. However, when  $p_0 \geq 0.4$ , the first operation type obtains better performance.

Fig. 3 shows the effects of the data collection period  $(n_{s_{-}})$  on the total achieved throughput of the schemes. When the CR network has a longer time to transmit data (i.e., a higher data collection period  $n_{s_{-}}$ ), it may have chance to improve the total achieved throughput with the same capacity of battery  $(E_c)$ .



**Fig. 2.** Total achieved throughput versus the probability of absence  $(p_o)$  when  $E_c$ =400,  $e_s$ =1,  $e_r$ =3 and  $n_{s_s}$ = 10000.



**Fig. 3.** Total achieved throughput versus the data collection time  $(n_{s_c})$  when  $E_c$ =400,  $e_s$ =1,  $e_r$ =3 and  $p_o$ =0.5.



Fig. 4. Total achieved throughput versus transmission energy (e\_i) when  $E_c$ =300,  $e_s$ =1,  $p_c$ =0.5 and  $n_{s_s}$ = 10000.



**Fig. 5.** Total achieved throughput versus capacity of the battery ( $E_c$ ) when  $e_s=1$ ,  $e_r=3$ ,  $p_c=0.5$  and  $n_{s_s I} = 10000$ .

The higher  $n_{s_r}$  (i.e.,  $n_{s_r} \ge 7000$ ) gives better performance to the first operation type in comparison with the second type. On the other hand, the second operation type obtains better performance than the first type when  $n_{s_r} < 7000$ .

The relations between transmission energy  $(e_i)$  and the total achieved throughput is shown in Fig. 4. Higher transmission energy may reduce the total achieved throughput of the schemes. However, the proposed scheme always has the best performance in comparison with the other considered schemes.

The capacity of the battery ( $E_c$ ) strongly effects on the performance of the schemes, which is shown in Fig. 5. A higher  $E_c$  may help the network to obtain higher throughput. Among the first and the second operation types, the first one achieves better performance when  $E_c < 450$ , otherwise the second one is better.

#### V. CONCLUSION

In this paper, we proposed a scheme to find an optimal policy for CU operation to maximize the achieved throughput in a certain data collection period of the CR network. The optimal policy can choose an operation type for the CU including sensing before transmitting data or transmitting data without sensing process. The data collection period plays a main role in switching between the first and second operation type of the CU. The proposed scheme also considers the effects of the capacity of the battery, the condition of the data channel and the probability of absence of the PU signal on the optimal policy. The simulation results shows that adaptive switching between the first and second operation type can help the proposed scheme achieve the outstanding performance.

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